

1 **Energy requirements during sponge cake baking:**
2 **experimental and simulated approach.**

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8 **Abstract**

9 Baking is a high energy demanding process, which requires special attention in order to
10 know and improve its efficiency. In this work, energy consumption associated to sponge
11 cake baking is investigated. A wide range of operative conditions (two ovens, three
12 convection modes, three oven temperatures) were compared. Experimental oven energy
13 consumption was estimated taking into account the heating resistances power and a
14 usage factor. Product energy demand was estimated from both experimental and
15 modeling approaches considering sensible and latent heat. Oven energy consumption
16 results showed that high oven temperature and forced convection mode favours energy
17 savings. Regarding product energy demand, forced convection produced faster and
18 higher weight loss inducing a higher energy demand. Besides, this parameter was
19 satisfactorily estimated by the baking model applied, with an average error between
20 experimental and simulated values in a range of 8.0 to 10.1 %. Finally, the energy
21 efficiency results indicated that it increased linearly with the effective oven temperature
22 and that the greatest efficiency corresponded to the forced convection mode.

23 Keywords: Baking, Energy demand, Efficiency, Sponge cake.

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Nomenclature

C_p	Specific heat, $\text{J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
f	Usage factor, dimensionless
h_c	Effective heat transfer coefficient, $\text{W m}^{-2} \text{ }^\circ\text{C}^{-1}$
k	Thermal conductivity, $\text{W m}^{-1} \text{ }^\circ\text{C}^{-1}$
m	Product mass, kg
N_p	Power, W
OE_C	Specific oven energy consumption, kJ kg^{-1}
PE_D	Specific product energy demand, kJ kg^{-1}
r	Radius, m
SE_C	Specific energy cost, $\text{\$ kg}^{-1}$
t	Process time, s or min
T	Temperature, $^\circ\text{C}$
WL	Weight loss, %
x	Mass fraction

Subscripts

0	Initial
<i>app</i>	Apparent
<i>ave</i>	Average
<i>b</i>	Baking
<i>eff</i>	Effective
<i>exp</i>	Experimental
<i>fan</i>	Fan
<i>heat</i>	Heating
<i>i</i>	Component
<i>lat</i>	Latent
<i>oven</i>	Oven
<i>sen</i>	Sensible
<i>sim</i>	Simulated
<i>water</i>	Evaporated

Greeks symbols

ε	Average absolute relative error, %
---------------	------------------------------------

ρ	Global density, kg m^{-3}
λ	Latent heat of vaporization of water at oven pressure, J kg^{-1}
η	Efficiency of the baking process, %

25

26 **1. Introduction**

27 During the last years energy costs have been rising significantly simultaneously with
 28 international legislation that forces manufacturers to reduce their carbon footprint in
 29 order to mitigate climate change fears. These factors are encouraging greater
 30 understanding of high-energy processes [1]. Particularly in the bakery industry, [2]
 31 discussed energy management systems, energy efficiency measures and the strategies to
 32 reduce energy consumption. Even though the study was based on USA bakery products
 33 its findings can be generalized to bakeries internationally. Authors identified four major
 34 processes (fermentation, baking, cooling and freezing, and cleaning) that consume the
 35 vast majority of purchased energy. In this sense, the implementation of energy
 36 efficiency measures for these systems can reduce energy costs and lessen the impacts of
 37 volatile energy prices. Also, as bakery involves massive consumption products, there
 38 was developed specific technology in order to improve the efficiency of the process. To
 39 achieve this goal there has been of significant importance the research and innovation
 40 focused on process efficiency with special concern on product quality [3].

41 Among all the stages involved in the bakery industry (ingredients selection, mixing,
 42 storage/dosing, baking, cooling, packing, storage, distribution and commercialization)
 43 the baking process itself is crucial. It is estimated that the energy demand during this
 44 stage is in the range of 3 - 5 MJ kg^{-1} .

45 The energy requirement of the baking process depends on two different aspects: the
 46 energy needed to achieve the complete product transformation and the actual oven
 47 energy consumption. The ratio between both values provides a direct and simple

48 measure of the process energy efficiency [4]. Besides, the difference between the oven
49 energy consumption and the product energy demand is the amount of energy absorbed
50 by the oven trays and walls and the energy lost to the ambience. Therefore, improving
51 oven design and optimizing the process conditions (temperature, convective heat
52 transfer and baking time) leads to energy savings; and for this purpose mathematical
53 modeling of the baking process is a powerful tool.

54 Le Bail et al. [5] compared the energy consumption of two bread baking processes.
55 Authors used a macroscopic approach that includes product and oven energy
56 requirements to estimate an energy efficiency index which showed that part frozen
57 baking had higher energy consumption than conventional baking. Alamir et al. [6]
58 studied energy savings using jet impingement during French bread baking. Authors
59 proposed a mechanistic heat and mass transfer model, which was able to estimate
60 product energy demand and the potential energy savings. Paton et al. [7] analysed the
61 energy requirements in a continuous industrial oven using a macroscopic balance and
62 proposed a CFD scheme to study the influence of the operative conditions. In addition,
63 Khatir et al. [1] combined the CFD model of the oven with a multi-objective
64 optimization methodology to develop an oven design tool. Ploteau et al. [8] compared in
65 terms of energy consumption, conventional bread baking with baking performed under
66 short infrared emitters (IR). Authors ensure the same kinetics of crust development and
67 quality criterion maintaining baking time and lowering oven temperature for IR baking.
68 IR technology allowed reducing 20% of the total energy consumption.

69 It is noticeable that all the mentioned works focused on energy management during
70 bread baking being difficult to find precedents on other kind of bakery product. In
71 consequence the aim of this article is to estimate energy requirements during sponge
72 cake baking. For this goal, oven energy consumption was calculated and both

73 experimental and modeling approaches were performed to calculate the product energy
74 demand. Additionally, the process efficiency was evaluated relating the oven energy
75 consumption and the product energy demand.

76 **2. Materials and Methods**

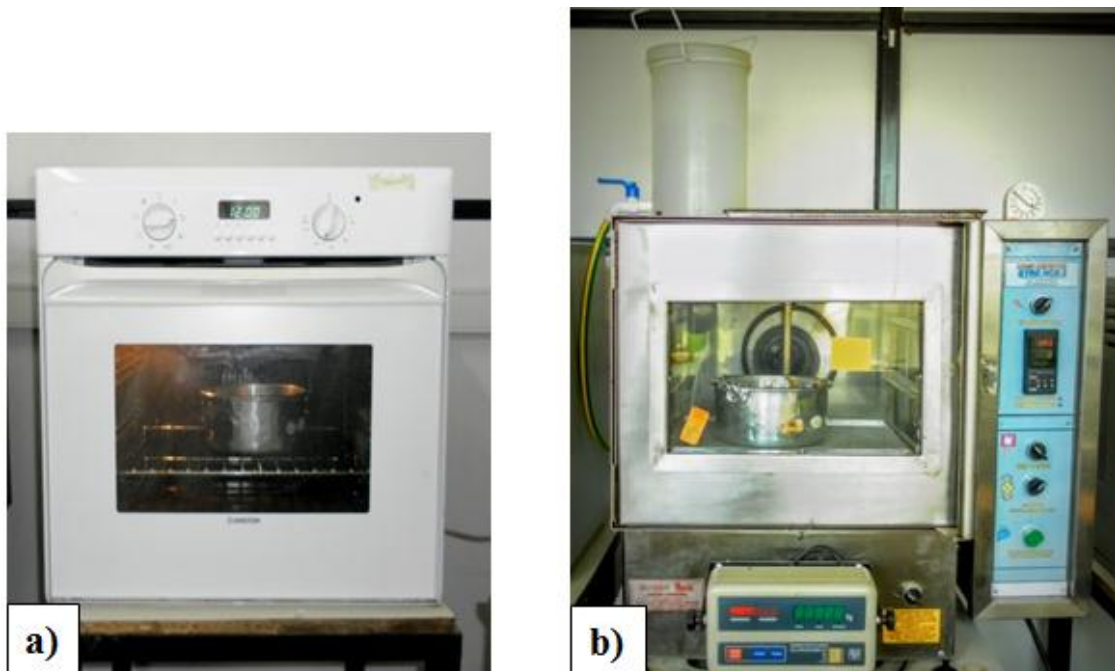
77 **2.1 Experimental baking tests**

78 For this study two batch-type electric ovens were used (Figure 1): a domestic oven
79 (Ariston FM87-FC, Italy), and a semi-industrial convective oven (Multiequip HCE-
80 3/300, Argentine). The first one was used for natural convection (NC) baking tests (with
81 the upper and lower resistances on) while the second one has the heating resistance and
82 a fan installed on the back wall, which propelled the air at 2.8 m/s (fixed air velocity)
83 allowing to operate under forced convection mode (FC). Also, this equipment enables to
84 perform steam-assisted forced convection mode (SFC). A connection pipe allows water
85 input into the chamber, which evaporates instantaneously; each test consumed
86 approximately 600 ml of water to generate steam. For all the tests, the samples were
87 placed over a tray, in the middle of the oven chambers.

88 The nominal oven temperature was set at 140, 160 and 180 °C for the three different
89 baking modes (9 total baking conditions). The oven was preheated until it reached the
90 pre-set temperature before every test. Table 1 shows the experimental characteristics
91 and the labels used to reference each condition. The measurement of effective
92 temperature (T_{eff}) is detailed in [9]. [Additional experiments were performed to](#)
93 [characterize both ovens in permanent mode at high temperature \(nominal temperature](#)
94 [equal to 185 °C\), without samples inside the oven. In these cases \$T_{eff}\$ were higher than](#)
95 [the one obtained with the baking sample, being 206 and 196 °C for NC and FC modes.](#)

96 Sponge cake batter was made mixing 270 g whole fresh eggs for 2 min at a 240 rpm in a
97 multifunction food processor (Rowenta Universo 700, France), then adding 360 g dry
98 premix, Satin Cake Premix (Puratos, Argentine) and mixing 2 min more. The batter
99 composition resulted: 45.6 % carbohydrates, 9.4 % proteins, 9.0 % fat, and 36.0 %
100 water. Finally 500 g of batter were dosed in an aluminium cake pan (18 cm diameter, 7
101 cm height), which gives an initial batter height of 2.5 cm.

102



103

104 **Figure 1.** Ovens used for the baking experiences a) domestic oven and b) semi-
105 industrial convective oven.

106

107 For sample and oven temperatures recording, T-type thermocouples (Omega, USA)
108 connected to a data logger (Keithley DASTC, USA), were used. Cake temperature
109 profile was obtained from three thermocouples fixed to the pan before filling it with the
110 batter (without interfering with cake development). Their positions were carefully
111 selected according to previous published results to ensure that the coldest region inside
112 the product was monitored. Thus, two of them were positioned in the axial axis of the

113 sample ($r = 0$) at 7.5 cm ($T1$) and at 5.5 cm ($T2$) from the pan bottom (being outside the
 114 sample at the beginning of the process and covered while expansion occurred). The
 115 third one ($T3$) was positioned near the pan wall ($r = 7.5$ cm), 2 cm from its bottom
 116 (inside the sample during the whole experiment). On the other hand, oven temperature
 117 (T_{oven} , °C) was recorded by placing two thermocouples in the middle of the oven
 118 chamber, near the sample. Two replicates were performed for each baking condition.

119

120

Table 1. Experimental conditions of the baking tests.

	Set temperature (°C)		
	140	160	180
Natural convection			
	NC1	NC2	NC3
T_{eff} (°C)	145.4 ± 4.5	161.4 ± 4.7	185.8 ± 4.1
t_b (min)	51.4 ± 0.3	42.6 ± 1.2	32.3 ± 1.6
Forced convection			
	FC1	FC2	FC3
T_{eff} (°C)	150.2 ± 6.9	175.6 ± 4.9	194.0 ± 5.5
t_b (min)	40.3 ± 0.6	32.1 ± 0.8	29.7 ± 1.0
Steam assisted forced convection			
	SFC1	SFC2	SFC3
T_{eff} (°C)	151.2 ± 6.3	166.2 ± 6.1	183.5 ± 6.7
t_b (min)	40.0 ± 0.5	31.8 ± 1.2	28.0 ± 0.4

121

122 The baking time, defined as the instant when the minimal internal temperature reaches
 123 95 °C [9], is also informed in Table 1. In spite of the wide range of baking times
 124 detailed in Table 1, the thorough analysis of the quality characteristics of the baked
 125 sponge cakes indicates that the colour kinetic parameters strongly depends on the
 126 baking condition. However, the final crust colour, measured by a browning index, was
 127 always in the range [100 - 110]. Additionally, no significant differences among baking
 128 conditions in crust thickness or crumb structure were found [10]. To account for the
 129 process yield, the sample weight was monitored during the whole process. Then, the

130 weight loss ($WL(t)$) was calculated as a function of the initial cake weight (m_0) and the
131 weight at time t ($m(t)$):

132

$$133 \quad WL(t) = \frac{m_0 - m(t)}{m_0} 100 \quad (1)$$

134

135 **2.2 Oven energy consumption**

136 The oven energy consumption depends on the electrical resistances heating power
137 ($N_{p,heat}$), the fan power ($N_{p,fan}$, only in FC and SFC modes) and the effective heating time
138 [11,12]. Both ovens used in this work have an ON/OFF control system, that is the
139 heating resistances were turned on if the oven temperature was lower than the set value,
140 when the set temperature was reached the heating resistances turned off and energy
141 consumption stopped, and so on. Thus, the oven energy consumption was intermittent.
142 Therefore, the specific oven energy consumption (OEC) was expressed according to Eq.
143 (2):

144

$$145 \quad OEC = \frac{I}{m_0} (N_{p,heat} f + N_{p,fan}) t_b \quad (2)$$

146

147 $N_{p,heat}$ was measured with the oven empty working at the maximum temperature, using a
148 clamp tester (SEW ST-300, Taiwan), values of 1.98 and 1.8 kW were obtained for
149 Ariston and Multiequip ovens, respectively. The fan power was much lower than the
150 heating one (0.05 kW), notwithstanding this contribution was considered in the
151 estimation of OEC .

152 On the other hand, the usage factor f , which represents the effective heating time,
153 depends on cooking temperature and on the product load. In the present work the

154 product load was the same in all the experimental tests, thus the f value only depends on
155 oven temperature and was calculated as the ratio between the total heating time and the
156 baking time t_b . The total heating time was estimated from the oven temperature profile,
157 adding all the periods with increasing oven temperature. The usage factor of the empty
158 oven in permanent mode and high temperature was 0.46 and 0.47 for NC and FC ovens,
159 respectively.

160 Once the oven energy consumption was calculated, the baking specific energy cost
161 (SEC) was estimated on the basis of 160 working hours per month. Both variable and
162 fixed costs were taken into account (reference price from the local energy distribution
163 company [13]). The monthly fixed cost (medium commercial use) was 27.7 \$/month,
164 and the variable one was 0.042 \$/kWh.

165

166 2.3 Experimental product energy demand

167 In the present study the experimental specific product energy demand (PED_{exp}) was
168 defined considering sensible and latent heat contributions, assuming that water is the
169 only component that evaporates during sponge cake baking, the latent heat can be
170 expressed in function of the enthalpy of water vaporization (λ , $2257 \times 10^3 \text{ J kg}^{-1}$) and the
171 amount of evaporated water:

172

$$173 \quad PED_{exp}(t) = \frac{m_0 C_{p, sen} (T_{ave}(t) - T_0) + \lambda (m_0 - m(t))}{m_0} \quad (3)$$

174

175 In order to evaluate the sensible specific heat (Eq. (8) detailed later), Choi & Okos [14]
176 approach was employed with an average temperature $T_{ave}(t)$, estimated from the
177 experimental ones ($T1$, $T2$ and $T3$).

178 As it can be seen the difference between Eq. (2) (OEC) and Eq. 3 (PED_{exp}) comprises
179 the energy needed to heat the oven components (walls, tray, etc.) and mainly the heat
180 loss through the oven walls to the ambient.

181 The efficiency of the process (η) is defined as the ratio of the energy demand of the
182 product to the energy consumption of the equipment [5], with PED_{exp} calculated at the
183 baking time t_b .

184

$$185 \quad \eta = 100 \frac{PED_{exp}}{OEC} \quad (4)$$

186

187 **2.4 Simulated product energy demand**

188 Usually, there can be found in the literature many mathematical models that describe the
189 baking process in terms of energy conservation laws [15,16]; only a few of them have
190 the intrinsic capacity to predict the product energy demand [1,7].

191 In the present study, a mathematical model previously developed for sponge cake
192 baking [9] was used to estimate the product energy demand. This model comprises
193 product expansion considering the simulation domain (Ω) as a continuous and
194 homogeneous geometry that expands [9]. The energy balance in this domain is
195 expressed as follows:

196

$$197 \quad \rho C p_{app} \frac{\partial T}{\partial t} = \nabla(k \nabla T), \forall \Omega \quad (5)$$

198

199 Water evaporation is considered through the thermal properties. Global density (Eq. (6))
200 was expressed according to Baik et al.[17]; the apparent specific heat (Eq. (7))

201 considered both sensible and latent heat contributions [18]; and the thermal conductivity
 202 (Eq. (10)) was evaluated with Rask [19] expression.

203

$$204 \quad \rho = \begin{cases} 1013 - 6.13T & T < 100 \\ 400 & T \geq 100 \end{cases} \quad (6)$$

$$205 \quad Cp_{app} = Cp_{sen} + Cp_{lat} \quad (7)$$

$$206 \quad Cp_{sen} = \sum_i x_i Cp_i \quad (8)$$

$$207 \quad Cp_{lat} = \frac{\lambda m_{water}}{\Delta T} \quad (9)$$

$$208 \quad k = \begin{cases} 0.27 + 0.1810^{-2} T & T < 100 \\ 0.2 & T \geq 100 \end{cases} \quad (10)$$

209

210 In Eq. (8) the components are water, carbohydrates, proteins, fat and ashes, being
 211 $Cp_{water} = 4180$; $Cp_{CH} = 1547$; $Cp_{prot}=1711$; $Cp_{fat}=1928$; $Cp_{ash}= 908$. In Eq. (9) m_{water}
 212 represents the total mass of water evaporated during baking and ΔT is the temperature
 213 interval of this phase change (5 °C).

214 Particularly in the numerical simulation, the domain was defined as the half cross-
 215 sectional area of the cake using axisymmetric 2D geometry. Regarding the boundary
 216 conditions of the energy balance (Eq. (5)), axial symmetry was considered in ($r = 0$).
 217 Besides, convective heat transfer at the cake top, and mould bottom and wall was
 218 assumed, using an effective heat transfer coefficient (h_c) (Eq. (11)):

219

$$220 \quad k\nabla T = h_c (T_{eff} - T) \quad (11)$$

221

222 The effective heat transfer coefficient was measured with a heat flux sensor (Omega
223 HFS4, USA) considering an average value of h_c for the entire sample surface, being 15,
224 25 and 20 for NC, FC and SFC baking modes, respectively [9].

225 To take into account the product expansion, mesh deformation was applied assigning a
226 prescribed displacement velocity to the top surface of the cake, being this parameter
227 derived from experimental height evolution data analysis [9].

228 The prediction of the specific product energy demand (PED_{sim}) was coupled to the
229 baking model. Thus, the simulated product energy demand at a given time can be
230 expressed in terms of the local energy in the whole domain:

231

$$232 \quad PED_{sim}(t) = \frac{1}{m_0} \int_0^t \left(\int_{\Omega} \rho C_p \frac{\partial T}{\partial t} d\Omega \right) dt \quad (12)$$

233 The baking model was solved with the finite element method using COMSOL
234 Multiphysics 3.5 coupled with MATLAB 7.8.0 [9].

235 Finally, the model prediction accuracy was assessed by the average absolute relative
236 error (ε) between the experimental and predicted specific product energy demand:

237

$$238 \quad \varepsilon = \frac{100}{n} \sum_{i=1}^n \left(\frac{|PED_{exp} - PED_{sim}|}{PED_{exp}} \right)_i \quad (13)$$

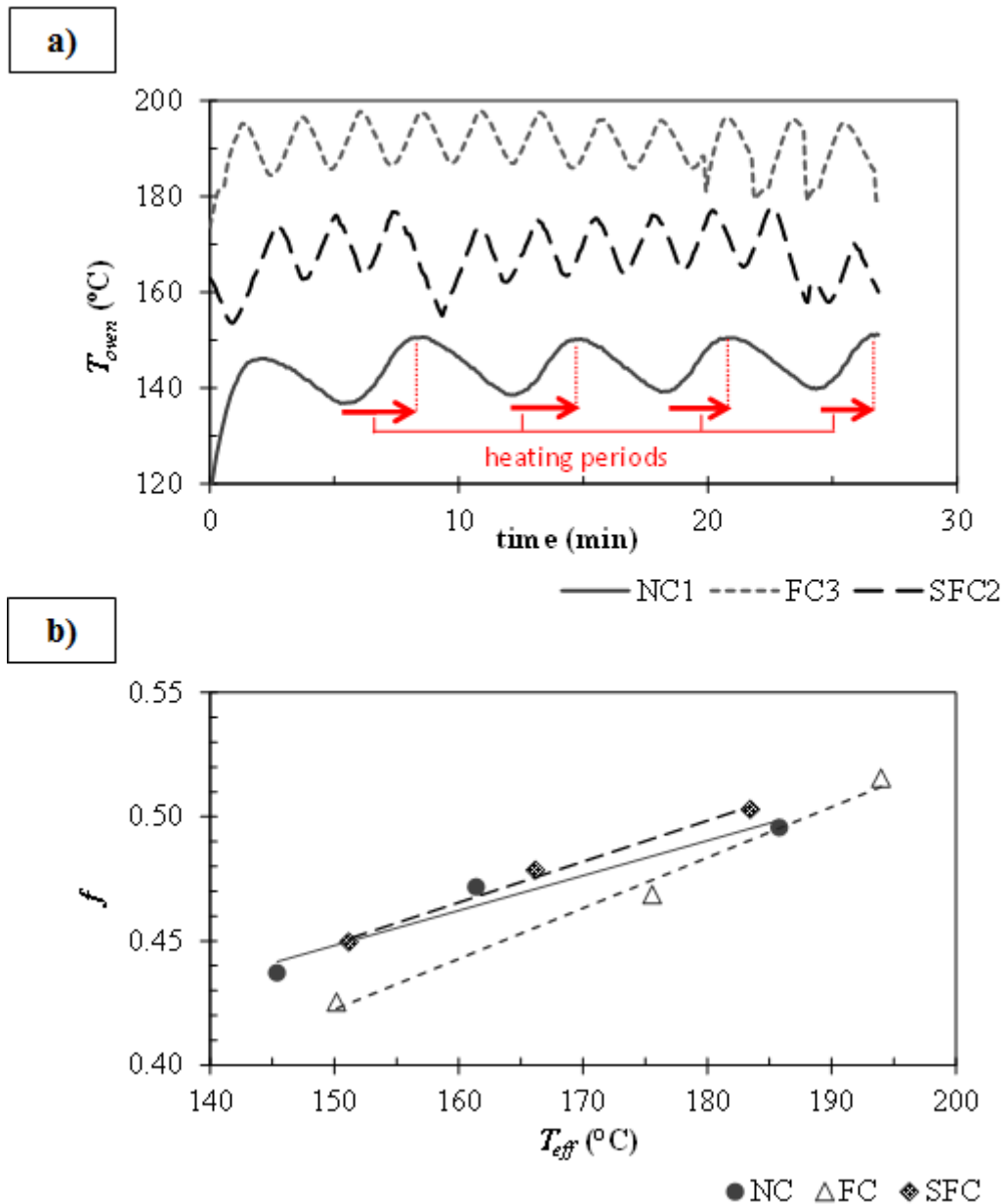
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240 **3. Results and Discussion**

241 **3.1 Oven performance**

242 In order to determine the energy consumption during the process it is essential to study
243 and describe the oven performance. In this sense, oven temperature recordings during

244 27 minutes are shown in Figure 2a. Only three of the nine tested conditions are shown,
 245 one of each convection mode. In general their evolution was quite repetitive (different
 246 oven temperature, same convection mode). All conditions showed an oscillatory
 247 behaviour, typical of an ON/OFF control system as described in Section 2.2.
 248



249
 250 **Figure 2.** a) Experimental oven temperature (T_{oven} , °C) recordings of some baking
 251 conditions and b) usage factor (f) values vs. effective temperature (T_{eff} , °C) for each
 252 convection mode.

253

254 In the case of natural convection mode, there was observed a regular wave with smaller
255 amplitude than the other two modes. Forced convection mode also presented a regular
256 variation with a shorter period wave. On the contrary, vapour injection produced a non-
257 regular oscillation making more difficult the temperature control. Therefore, each
258 condition was characterized with an effective temperature as it was informed in Table 1.
259 Also, in Figure 2a the intervals of time where the oven temperature increases are
260 highlighted in order to obtain the total heating time to calculate the f factor. This way,
261 with oven temperature profile and baking times informed in Table 1, f was calculated.
262 Figure 2b shows these values as a function of T_{eff} for each baking mode. It is evident
263 that f increases with oven temperature, while there is not a clear dependence with the
264 convection mode. Thus, a higher operative temperature requires longer effective heating
265 times during the baking test, no matter the convection mode.

266 Calculated OEC values are presented in Table 2, these results are in the same range
267 reported by [5], in particular the authors informed an average value of 5.34 MJ/kg of
268 bread considering fourteen electrical ovens. Also these values are comparable to the
269 ones presented by [20] who measured the specific energy consumption in an industrial
270 bakery, considering only the percentage of energy used in the baking process, the
271 authors reported 1.27 kWh/kg processed flour for products baked in electrical oven, the
272 average value of our results is 1.86 in the same basis. It was found that higher operative
273 temperature favours energy savings and in addition, when comparing between
274 convection modes, NC requires higher energy than the other modes. Even though f
275 increases with oven temperature, smaller baking times are associated with higher oven
276 temperatures which lead to lower energy consumption.

277

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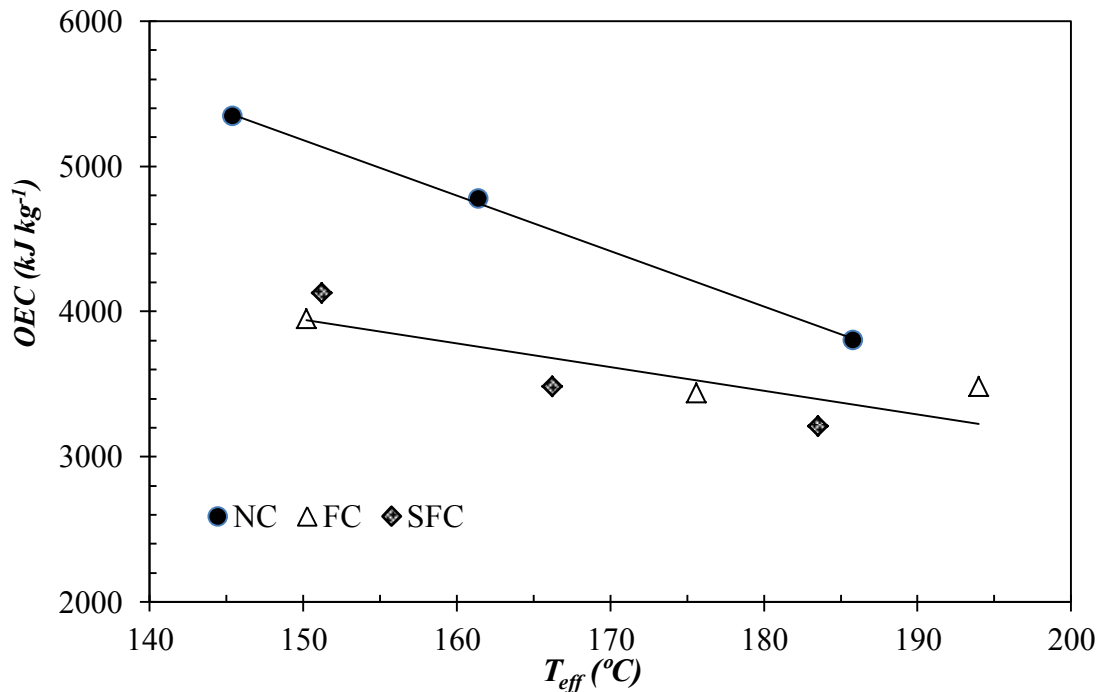
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Table 2. Experimental variables calculated from Eqs. (1), (3), (4) and (5).

	NC1	NC2	NC3	FC1	FC2	FC3	SFC1	SFC2	SFC3
<i>OEC</i> (kJ kg ⁻¹)	5340.4	4772.2	3801.2	3947.1	3439.7	3481.5	4123.4	3481.0	3209.3
<i>SEC</i> (\$ kg ⁻¹)	0.250	0.242	0.228	0.230	0.222	0.223	0.232	0.223	0.219
<i>WL</i> (%)	5.7 ±0.3	5.2 ±1.0	4.9 ±0.5	6.9 ±1.0	7.2 ±1.0	7.4 ±1.0	6.6 ±0.9	6.5 ±0.6	6.4 ±0.1
<i>PED</i> (kJ kg ⁻¹)	347.0 ±1.7	364.2 ±3.0	331.0 ±9.4	399.0 ±4.1	428.8 ±4.0	453.9 ±0.6	362.2 ±0.6	356.8 ±3.5	370.4 ±1.0
<i>η</i> (%)	6.5	7.7	8.7	10.1	12.5	13.0	8.8	10.2	11.5

280

281 To complete the analysis, Figure 3 presents *OEC* vs. T_{eff} for each baking condition. This
 282 confirms the behaviour mentioned above and also shows that FC and SFC modes follow
 283 the same trend with the exception of the lowest oven temperature. In fact, steam
 284 addition is reflected in a decrease of the effective temperature.



285

286 **Figure 3.** Specific oven energy consumption (*OEC*, kJ kg⁻¹) measured at the end of
 287 baking for each baking condition.

288

289 Also the specific energy cost is reported in Table 2. As it was expected, *SEC* presents
290 the same trend that *OEC*, with a difference of 14 % between the maximum and
291 minimum energy consumption conditions (NC1 and SFC3 respectively).

292

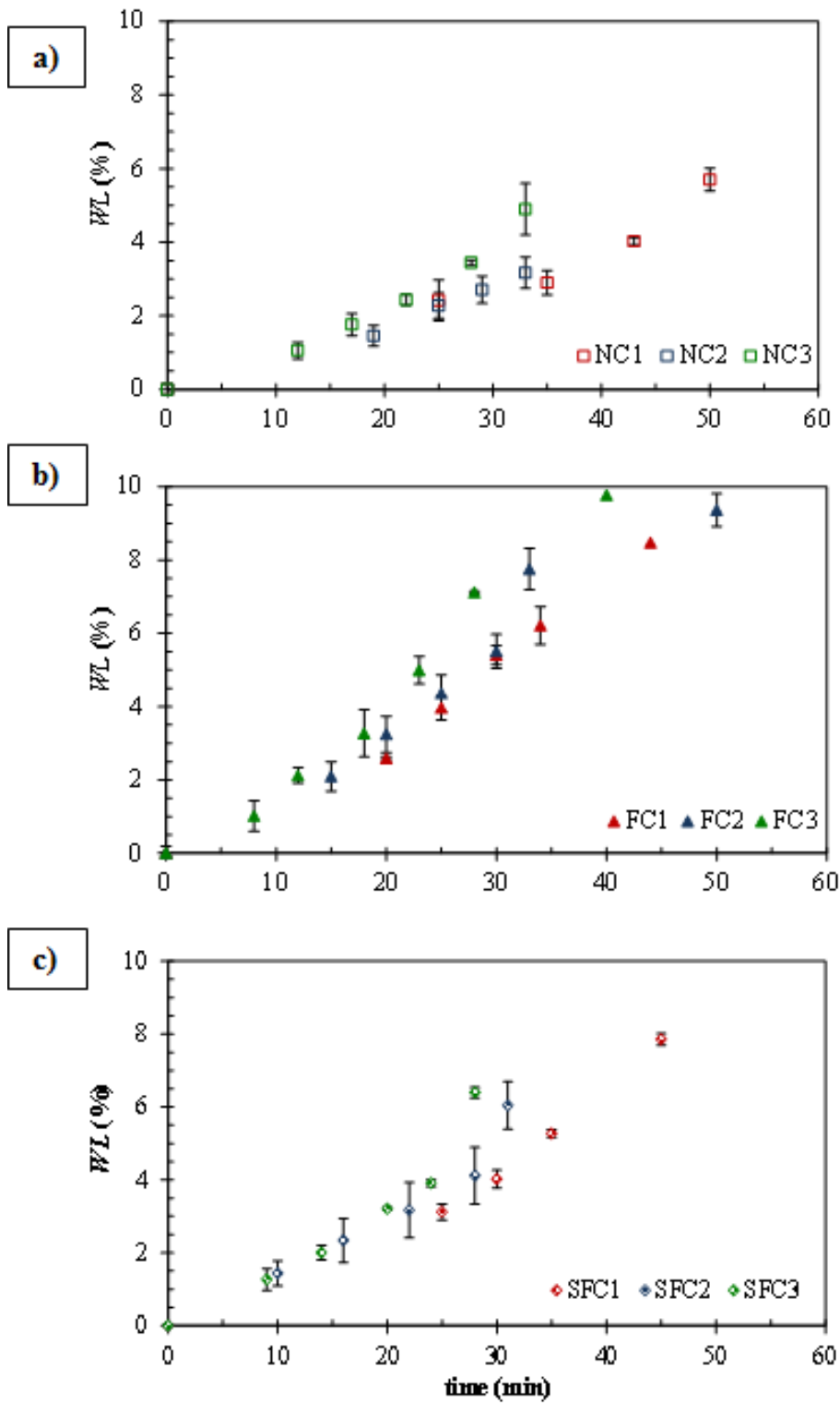
293 **3.2 Product energy demand**

294 As stated before, the amount of water that evaporates during the process strongly affects
295 the energy demand. In this sense, sponge cake weight loss was monitored during the
296 baking tests and the results are shown in Figure 4. First of all, the rate of *WL* evolution
297 significantly increases when baking at the highest oven temperature for the three
298 convection modes. Nevertheless, there were not significant differences between *WL*
299 values at the end of baking in the same convection mode (Table 2), because of the
300 combined effect of the *WL* rate and the baking time. Secondly, when comparing
301 between convection modes it is noticeable that forced convection (Figures 4b and 4c)
302 induces a faster and higher weight loss compared with natural convection mode (Fig.
303 4a) and that steam injection reduces this effect. Moreover, to reinforce this idea, *WL*
304 values at the end of the process were 5.3 ± 0.4 , 7.2 ± 0.3 and 6.5 ± 0.8 , for NC, FC and
305 SFC modes, respectively. This is consistent with the results informed by other authors
306 [8,15].

307 PED_{exp} was calculated at each step time that *WL* was registered during the process. This
308 evolution is presented in Figure 5. There was observed that for all the baking conditions
309 this parameter increased with time and also that as baking evolves, the rate of change
310 slows down. What is more, higher oven temperature induces higher energy demand.

311 Table 2 details the PED_{exp} calculated at the end of the process for each baking
312 condition. There was observed that PED_{exp} is closely related to *WL* behaviour.

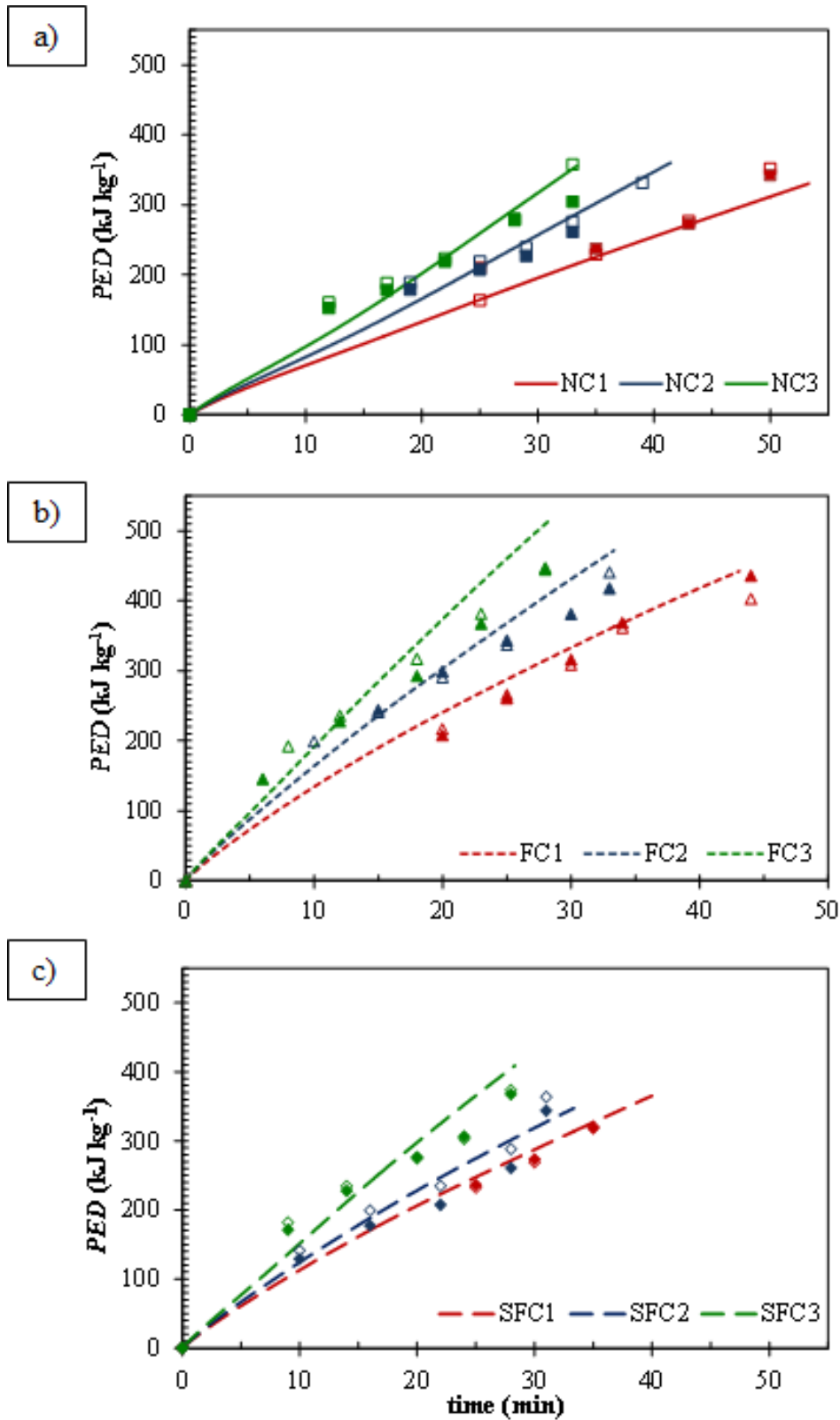
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314

315 **Figure 4.** Weight loss (WL , %) evolution during baking of sponge cake: a) natural
 316 convection, b) forced convection and c) steam assisted forced convection mode.

317



318

319 **Figure 5.** Specific product energy demand (PED , kJ kg^{-1}) during baking: experimental
 320 measured values (empty and full symbols) and simulated values (full lines).

321

322 Other researchers focused in this issue using a similar method to calculate energy
323 demand particularly for bread baking. In this sense, Paton et al. [7] informed similar
324 values considering the energy demand for heating the dough, the energy to evaporate
325 around 10% of the initial moisture content and the energy required for starch
326 gelatinization. Also, Ploteau et al. [8] estimated a similar energy demand taking into
327 account the main transformation that occurs during baking (dough into crumb and crust)
328 and water evaporation. Notice that, as was expected, the energy demand for bread
329 baking is higher than the one required for sponge cake, due to the higher level of
330 dehydration that this product suffers.

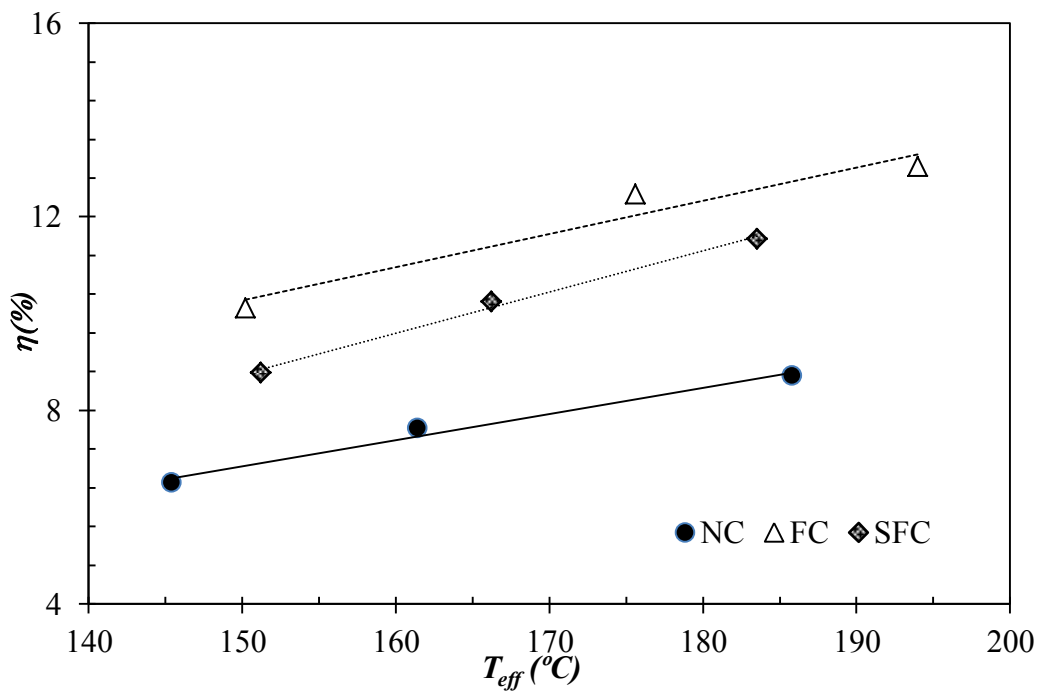
331 Besides, as stated in Section 2.4, PED_{sim} was coupled to the mathematical baking
332 model. In addition to PED_{exp} , Figure 5 shows PED_{sim} values. In fact, the average error
333 (Eq. (13)) was 8.0, 10.1 and 8.0 % for NC, FC and SFC, respectively. The highest
334 relative error values were associated to the baking conditions with the highest effective
335 temperature (NC3, FC2, FC3 and SFC3). From these results it is noticeable that the
336 model successfully reproduces the experimental behaviour discussed above,
337 demonstrating the ability of this mathematical model to incorporate product energy
338 demand.

339

340 **3.3 Efficiency of the process**

341 Once the OEC and PED_{exp} were obtained, the energy efficiency of the process was
342 calculated as the ratio between these two variables (Eq. (4)). The results are presented in
343 Figure 6 as a function of T_{eff} for each baking condition. In all cases η increases linearly
344 with T_{eff} , being more evident the effect of oven temperature in FC and SFC modes, even
345 though this last one presented lower efficiency due to the energy to produce steam
346 inside the oven chamber. Also from the values detailed in Table 2, the greatest

347 efficiency corresponded to FC mode and the lowest to NC mode. This effect is mainly
348 explained by the higher heat and mass transfer rates associated to the forced convection
349 mode which reduces the baking time, in concordance with previous published results
350 [5,6]. In addition, Paton et al. and Khatir et al. [7,21] who studied the optimization of
351 bread baking process, suggested that one way to achieve energy savings is to reduce the
352 baking time by improving the oven design.



353
354 **Figure 6.** Process efficiency (η , %) vs. effective temperature (T_{eff} , °C) for each
355 convection mode.

356 4. Conclusions

357 In this work energy requirements during sponge cake baking were studied. The analysis
358 of the oven energy consumption indicated that higher oven temperatures and forced
359 convection favours energy savings, due to the decrease of the baking times. On the
360 contrary, high oven temperature induces an increase of the product energy demand. This

361 parameter is closely related to the weight loss, in consequence both present similar
362 trends. Additionally, the baking model successfully represented the product energy
363 demand evolution; in fact, the average error calculated between experimental and
364 simulated values was less than 10 %.

365 To take into account the economic aspects, the specific energy cost was estimated,
366 founding a difference of 14 % between the minimal and maximum values.

367 Finally, a measure of the process efficiency was obtained, it increased linearly with the
368 effective temperature, and the greatest values corresponded to FC mode and the lowest
369 to NC mode, indicating again the influence of the reduction of the baking time.

370 In conclusion, on the basis of the results presented in this work, the better baking
371 condition was the fast one, FC3. Notwithstanding, complementary studies of the quality
372 characteristics of the baked sponge cakes (results not shown in this work), shown that
373 forced convection baking with high oven temperature was the condition with the lowest
374 appreciation by the potential consumers, indicating that the selection of an optimal
375 baking condition implies the joint analysis of diverse aspects.

376

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382 **References**

383 [1] Z. Khatir, J. Paton, H. Thompson, N. Kapur, V. Toropov, Optimisation of the

- 384 energy efficiency of bread-baking ovens using a combined experimental and
385 computational approach, *Applied Energy* 112 (2013) 918–927.
- 386 [2] P. Therkelsen, E. Masanet, E. Worrell, Energy efficiency opportunities in the
387 U.S. commercial baking industry, *Journal of Food Engineering* 130 (2014) 14–
388 22.
- 389 [3] A. Mondal, A.K. Datta, Bread baking - A review, *Journal of Food Engineering*
390 86 (2008) 465–474.
- 391 [4] S.M. Goñi, V.O. Salvadori, Energy consumption estimation during oven cooking
392 of food., in: S. Reiter (Ed.), *Energy Consumption* (2014) pp. 99–116.
- 393 [5] A. Le-bail, T. Dessev, V. Jury, R. Zuniga, T. Park, M. Pitroff, Energy demand for
394 selected bread making processes: Conventional versus part baked frozen
395 technologies, *Journal of Food Engineering* 96 (2010) 510–519.
- 396 [6] M. Alamir, E. Witrant, G. Della Valle, O. Rouaud, C. Josset, L. Boillereaux,
397 Estimation of energy saving thanks to a reduced-model-based approach: Example
398 of bread baking by jet impingement, *Energy* 53 (2013) 74–82.
- 399 [7] J. Paton, Z. Khatir, H. Thompson, N. Kapur, V. Toropov, Thermal energy
400 management in the bread baking industry using a system modelling approach,
401 *Applied Thermal Engineering* 53 (2013) 340–347.
- 402 [8] J.P. Ploteau, P. Glouannec, V. Nicolas, A. Magueresse, Experimental
403 investigation of French bread baking under conventional conditions or short
404 infrared emitters, *Applied Thermal Engineering* 75 (2015) 461–467.
- 405 [9] M.M. Ureta, D.F. Olivera, V.O. Salvadori, Baking of Sponge Cake: Experimental
406 characterization and mathematical modelling, *Food and Bioprocess Technology* 9
407 (2015) 664–674.
- 408 [10] M.M. Ureta, D.F. Olivera, V.O. Salvadori, Influence of baking conditions on the

409 quality attributes of sponge cake, *Food Science and Technology International*
410 Online version (2016). doi:10.1177/1082013216666618.

411 [11] S.M. Goñi, V.O. Salvadori, Model-based multi-objective optimization of beef
412 roasting, *Journal of Food Engineering* 111 (2012) 92–101.

413 [12] M.A. Townsend, S. Gupta, The roast: Nonlinear modeling and simulation,
414 *Journal of Food Process Engineering* 11 (1988) 17–42.

415 [13] Edelap, Cuadros Tarifarios, (2016).
416 https://oficinavirtual.edelap.com.ar/reports/Cuadro_Tarifario_de_Publicacion_02
417 .16.pdf. Last accessed September 15, 2016.

418 [14] Y. Choi, M.R. Okos, Effects of temperature and composition on the thermal,
419 properties of foods, *Food Engineering and Process Applications*. Elsevier
420 Applied Science Publishers (1986) pp: 93–101.

421 [15] M. Sakin, F. Kaymak-ertekin, C. Ilicali, Modeling the moisture transfer during
422 baking of white cake, *Journal of Food Engineering* 80 (2007) 822–831.

423 [16] M.S. Andresen, Experimentally supported mathematical modeling of continuous
424 baking processes, (2013) PhD Thesis, Division of Industrial Food Research,
425 National Food Institute, Technical University of Denmark, Lyngby, Denmark.

426 [17] O.D. Baik, S.S. Sablani, M. Marcotte, F. Castaigne, Modeling the thermal
427 properties of a cup cake during baking, *Journal of Food Science* 64 (1999) 295–
428 299.

429 [18] C. Bonacina, G. Comini, A. Fasano, M. Primicerio, Numerical solution of phase-
430 change problems, *International Journal of Heat and Mass Transfer* 16 (1973)
431 1825–1832.

432 [19] C. Rask, Thermal properties of dough and bakery products: A review of
433 published data, *Journal of Food Engineering* 9 (1989) 167–193.

- 434 [20] R. Kannan, W. Boie, Energy management practices in SME - case study of a
435 bakery in Germany, *Energy Conversion and Management* 44 (2003) 945–959.
- 436 [21] Z. Khatir, A.R. Taherkhani, J. Paton, H. Thompson, N. Kapur, V. Toropov,
437 Energy thermal management in commercial bread-baking using a multi-objective
438 optimisation framework, *Applied Thermal Engineering* 80 (2015) 141–149.
- 439
- 440