# Field/isolated lenticular galaxies with high $S_{N}$ values: the case of NGC 4546 and its globular cluster system 

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#### Abstract

We present a photometric study of the field lenticular galaxy NGC 4546 using Gemini/GMOS imaging in $g^{\prime} r^{\prime} i^{\prime} z^{\prime}$. We perform a 2D image decomposition of the surface brightness distribution of the galaxy using GALFIT, finding that four components adequately describe it. The subtraction of this model from our images and the construction of a colour map allow us to examine in great detail the asymmetric dust structures around the galactic centre. In addition, we perform a detailed analysis of the globular cluster (GC) system of NGC 4546. Using a Gaussian Mixture Model algorithm in the colour-colour plane, we detected hints of multiple groups of GC candidates: the classic blue and red subpopulations, a group with intermediate colours that present a concentrated spatial distribution towards the galaxy, and an additional group towards the red end of the colour distribution. We estimate a total GC population for NGC 4546 of $390 \pm 60$ members and specific frequency $S_{N}=3.3 \pm 0.7$, which is relatively high compared to the typical value for galaxies of similar masses and environment. We suggest that the unusual GC population substructures were possibly formed during the interaction that led to the formation of the young ultra-compact dwarf (NGC 4546-UCD1) found in this system. Finally, we estimate the distance modulus of NGC 4546 by analysing its luminosity function, resulting in $(m-M)=30.75 \pm 0.12 \mathrm{mag}(14.1 \mathrm{Mpc})$.


Key words: galaxies: elliptical and lenticular, cD-galaxies: photometry-galaxies: star clusters: general.

## 1 INTRODUCTION

In the last decades, the study of globular cluster (GC) systems has become an important tool to obtain information about the formation history and evolution of early-type galaxies. This is because the origin of GCs seems to be closely linked to periods of intense star formation (e.g. Kissler-Patig, Forbes \& Minniti 1998; Kuntschner et al. 2002; Puzia et al. 2004, 2005; Strader, Beasley \& Brodie 2007; Sesto et al. 2018; Forte et al. 2019).

In general, GC systems associated with early-type galaxies located in different environments show bimodal colour distributions to a greater or lesser extent. These components are associated with two old ( $>9$ Gyr; Strader et al. 2005) GC subpopulations that present different metallicities: the blue (or metal-poor) and the red (or metal-rich) clusters. The different features and properties shown by both groups (see Brodie \& Strader 2006) suggest

[^0]different formation epochs and/or mechanisms (e.g. Bekki et al. 2008; Lee et al. 2010; Kruijssen 2014, 2015; Choksi, Gnedin \& Li 2018). However, a handful of galaxies in the local Universe present complex GC systems showing multiple peaks in their colour distributions, possibly indicating star formation episodes at lower redshifts (Peng et al. 2006; Blom, Spitler \& Forbes 2012; Tonini 2013; Caso et al. 2013; Caso, Bassino \& Gómez 2015; Escudero et al. 2015; Sesto, Faifer \& Forte 2016). Therefore, the study of galaxies that display both classical and old GC subpopulations, alongside subpopulations with different metallicities and/or ages, provides important constraints for galaxy formation models as well as information about the star formation and assembly histories of individual galaxies.

In this context, we focus on the photometric analysis of the GC system associated with the lenticular (S0) galaxy NGC 4546, in order to characterize and inquire about the evolutionary history of the system as a whole. NGC 4546 is a field $(\log (\rho)=-1.14$ $\mathrm{Mpc}^{-3}$; Cappellari et al. 2011) nearly edge-on galaxy, with only a

Table 1. Properties of NGC 4546. Equatorial and galactic coordinates from NED (http://ned.ipac.caltech.edu/); morphological classification (NED); $V$ magnitude from Ho et al. (2011); distance modulus from Tully et al. (2013); distance in Mpc; effective radius and stellar velocity dispersion from Cappellari et al. (2013); heliocentric velocity from Cappellari et al. (2011); stellar mass from Norris \& Kannappan (2011).

| Property | Value | Units |
| :--- | :---: | :---: |
| $\alpha$ | $12: 35: 29.5$ | $\mathrm{~h}: \mathrm{m}: \mathrm{s}(\mathrm{J} 2000)$ |
| $\delta$ | $-03: 47: 35.5$ | $\mathrm{~d}: \mathrm{m}: \mathrm{s}(\mathrm{J} 2000)$ |
| $l$ | $295: 13: 38.5$ | $\mathrm{~d}: \mathrm{m}: \mathrm{s}$ |
| $b$ | $58: 50: 23.3$ | $\mathrm{~d}: \mathrm{m}: \mathrm{s}$ |
| Type | $\mathrm{SB} 0^{-}(\mathrm{s})$ | - |
| $\mathrm{V}_{\mathbf{T}}^{\mathbf{0}}$ | $10.57 \pm 0.01$ | mag |
| $(\mathrm{m}-\mathrm{M})_{0}$ | $30.73 \pm 0.14$ | mag |
| Dist. | $14.0 \pm 0.9$ | Mpc |
| $R_{\text {eff }}$ | 22.23 | arcsec |
| $\sigma_{e}$ | 188 | $\mathrm{~km} \mathrm{~s}^{-1}$ |
| $\mathrm{~V}_{\text {hel }}$ | $1057 \pm 5$ | $\mathrm{~km} \mathrm{~s}^{-1}$ |
| Stellar mass | $2.7 \times 10^{10}$ | $\mathrm{M}_{\odot}$ |

single previous study of its GC system (Zaritsky et al. 2015). These authors, using images from the Spitzer Survey of Stellar Structures in Galaxies ( $\mathrm{S}^{4} \mathrm{G}$; Sheth et al. 2010), estimated the total population of the GC system within 50 kpc as $N_{\text {tot }}=120$ members. On the other hand, photometric and spectroscopic observations of the galaxy (Galletta 1987; Bettoni, Galletta \& Oosterloo 1991; Emsellem et al. 2004; Kuntschner et al. 2010; Ricci, Steiner \& Menezes 2015) revealed irregular dust lanes, pseudo-spiral arms, and the presence of ionized gas rotating in the opposite direction to its stellar disk. In addition, Norris \& Kannappan (2011) and Norris et al. (2015) studied the stellar population of the ultra-compact dwarf (UCD) NGC 4546-UCD1 linked to the NGC 4546 system. These authors found that NGC 4546-UCD1 displays an extended star formation history with a light-weighted age of $\sim 4 \mathrm{Gyr}$, suggesting that it is
the remnant nucleus of a dwarf galaxy that was tidally disrupted by NGC 4546. All these pieces of evidence point out that NGC 4546 has experienced at least one minor merger event in the recent past.

Adopting the distance modulus $(m-M)_{0}=30.73 \pm 0.14$ for NGC 4546 (see Table 1) and the scale $0.067 \mathrm{kpc} \operatorname{arcsec}^{-1}$, the effective radius of the galaxy $\left(R_{\text {eff }}=22.23\right.$ arcsec $)$ is equivalent to $\approx 1.5 \mathrm{kpc}$ projected distance. Aditional relevant parameters of the galaxy are shown in Table 1.

The structure of the paper is as follows. In Section 2, we present our observational data, the reduction process and photometric calibration. In addition, this section gives the completeness tests performed on the data, as well as a description of the comparison field adopted in this work. Section 3 describes the overall properties of the galaxy light, and the identification of the photometric subcomponents of NGC 4546; in Section 4, we focus on the general analysis of the GC system, as well as the possible subpopulations that comprise it. Finally, a summary of the results and the conclusions of this work are presented in Section 5.

## 2 DATA

### 2.1 Observations and data reduction

The photometric study is based on a mosaic consisting of three deep fields (Fig. 1) obtained with the GMOS camera of the GeminiSouth telescope (Hook et al. 2004). The images were taken under excellent seeing conditions ( $0.46-0.71$ arcsec), as part of Gemini programmes GS-2011A-Q-13 (PI: Norris, M.) and GS-2014A-Q30 (PI: Escudero, C.), using $4 \times 100 \mathrm{~s}$ exposures in the $g^{\prime}, r^{\prime}, i^{\prime}$ filters (Fukugita et al. 1996) and $4 \times 290$ s exposures in the $z^{\prime}$ filter. Fig. 1 shows NGC 4546 in the central region of the mosaic, and also the presence of the dS0 edge-on galaxy CGCG 014-074 with similar redshift $\left(\mathrm{V}_{\text {hel }}=998 \pm 54 \mathrm{~km} \mathrm{~s}^{-1}\right.$; Colless et al. 2003) to NGC 4546, located at a projected distance of $\sim 5.5$ arcmin ( $\sim 22 \mathrm{kpc}$ ) towards the northeast.


Figure 1. Mosaic created with the three GMOS fields used in this study. A false colour image of the galaxy was superimposed. In addition, the galaxy companion CGCG014-074 is observed towards the northeast. The black arrow shows the location of the UCD studied by Norris \& Kannappan (2011) and Norris et al. (2015). Considering the distance of $14 \pm 0.9 \mathrm{Mpc}$ (Tully et al. 2013) for NGC 4546, $1 \operatorname{arcsec}=0.067 \mathrm{kpc}$.

The reduction process of our observations was carried out by specific Gemini/GMOS routines within IRAF $^{1}$ (version V2.15), such as GPREPARE, GBIAS, GIFLAT, GIREDUCE, GMOSAIC, GIFRINGE, and GIRMFRINGE. The raw data were corrected using appropriate bias and flat-field frames obtained from the Gemini Observatory Archive (GOA) as part of the standard GMOS baseline calibrations. Within this reduction stage, a feature present in the $i^{\prime}$ and $z^{\prime}$ frames is the night-sky fringing, caused by thin-film interference effects in the CCD detectors. To subtract this effect from our science data, blank sky calibration images were used. These images, with exposure times of 300 s , are obtained by the Gemini Observatory each semester. We downloaded five blank sky images from GOA, which were combined using the GIFRINGE task. Subsequently, this resulting frame was used to remove the fringing pattern in our data using the task Girmfringe.

As the final step, the reduced images for each field and filter were co-added using the IRAF task IMCOADD, obtaining final $g^{\prime}, r^{\prime}, i^{\prime}$, and $z^{\prime}$ images for the three fields.

### 2.2 Photometry

In order to obtain a better detection, classification, and subsequent photometry of GC candidates, it was necessary to model and subtract the sky background as well as the brightness due to the galaxy halo. To do this, we followed the same procedure described in Faifer et al. (2011) and Escudero et al. (2015), Escudero et al. (2018), using a script that combines features of SEXTRACTOR software (Bertin \& Arnouts 1996), along with IRAF filtering tasks. In addition, the script provides a catalogue for each science field containing all the objects detected in the $g^{\prime} r^{\prime} i^{\prime} z^{\prime}$ filters. Since typical GCs have effective radii of several parsecs (Harris 2009; Puzia et al. 2014) and given the adopted distance to NGC 4546 (Table 1), they are expected to be observed as unresolved sources in our GMOS images. Therefore, we used the stellarity index parameter (CLASS STAR) of SEXTRACTOR as a selection criterion to separate between resolved and unresolved objects using the boundary value of 0.5 .

After performing the objects detection, we selected between 20 and 30 isolated, unresolved, and non-saturated sources uniformly distributed over the GMOS field of view (FoV), with the aim to model the point spread function (PSF) on each science field and filter. Using the DAOPHOT package (Stetson 1987) within IRAF, we fit a Moffat 25 model to the light distribution of the objects through the PSF task, since this provides lower errors than those obtained by using another analytical functions included in the task mentioned above (e.g. Gaussian and Moffat 15 models). In addition, as usual for GMOS images, we found that allowing a quadratic spatial variation of the PSF model over the FoV gives the best results. Subsequently, the corresponding PSF empirical models were applied to each unresolved source detected in our images through the ALLSTAR task. In addition, we performed aperture corrections to the PSF magnitudes using the MKAPFILE task.

### 2.3 Photometric Calibration

In order to transform the instrumental PSF magnitudes to the $A B$ standard system, a standard star field (E5-b; $\alpha_{\mathrm{J} 2000}=12: 05: 25$,

[^1]Table 2. Coefficients used in the transformation to the standard system. $m_{\text {zero }}^{*}$ : final values of the photometric zero-points used for the field 2 . CT: values of colour terms obtained from Escudero et al. (2015). $\mathrm{A}_{\lambda}$ : Galactic extinction coefficients for each filter determined by Schlafly \& Finkbeiner (2011).

| Filter | $m_{\text {zero }}^{*}$ | CT | $\left(m_{1}-\mathrm{m}_{2}\right)$ | $A_{\lambda}$ |
| :--- | :---: | :---: | :---: | :---: |
| $g^{\prime}$ | $28.27 \pm 0.01$ | 0.08 | $\left(g^{\prime}-r^{\prime}\right)$ | 0.112 |
| $r^{\prime}$ | $28.36 \pm 0.01$ | 0.03 | $\left(g^{\prime}-r^{\prime}\right)$ | 0.077 |
| $i^{\prime}$ | $27.98 \pm 0.02$ | -0.02 | $\left(r^{\prime}-i^{\prime}\right)$ | 0.057 |
| $z^{\prime}$ | $26.84 \pm 0.01$ | 0.0 | $\left(i^{\prime}-z^{\prime}\right)$ | 0.043 |

$\left.\delta_{\mathrm{J} 2000}=-45: 38: 11\right)$ was observed in the same night as our central science field (field 2 containing the galaxy). The instrumental magnitudes of the photometric standard stars in this field were obtained using the PHOT task within IRAF. Since the standard field is not very crowded, we decided to use a large aperture of 3 arcsec of radius ( $\sim 5 \mathrm{FWHM}$ ), to avoid performing an aperture correction.

The transformation of our instrumental magnitudes to the standard system was carried out using the following expression:
$m_{\text {std }}=m_{\text {zero }}+m_{\text {inst }}-K_{C P}(X-1)+C T\left(m_{1}-m_{2}\right)_{\text {std }}$
where $m_{\text {std }}$ are the standard magnitudes, $m_{\text {zero }}$ are the photometric zero-points, minst are instrumental magnitudes, $K_{\mathrm{CP}}$ is the mean atmospheric extinction at Cerro Pachón, $X$ is the airmass of our observations, CT is the coefficient of the colour term and ( $m_{1}$ $\left.-m_{2}\right)_{\text {std }}$ are the colours listed in the fourth column of Table 2. The mean magnitude zero-point for each filter of the standard field was determined following the procedure of Jørgensen (2009) and Escudero et al. (2015). On the other hand, owing to the low number of standard stars in our standard field, the values of the colour terms used here were those published in this last mentioned work.

Once the magnitudes of the objects belonging to the central field of our mosaic were transformed using the expression 1, the corresponding data to fields 1 and 3 were calibrated using common sources located in the overlapping regions between them and field 2 . Finally, we applied the Galactic extinction coefficient values given by Schlafly \& Finkbeiner (2011, the fifth column in Table 2).

### 2.4 Completeness test

In order to quantify the completeness of our photometric catalogue, we performed a series of completeness experiments on each science field. We added 200 artificial sources at intervals of 0.2 mag on the $g^{\prime}$-band image, covering the range $21<g_{0}^{\prime}<29 \mathrm{mag}$ (a total of 8000 sources). This procedure was carried out using the STARLIST and ADDSTAR tasks of IRAF. The first one was used initially to generate a sample of artificial objects randomly distributed over the fields. In order to simulate the radial distribution of GC candidates over the mosaic, a power-law function was used in the science field that contains the galaxy, and uniform distribution in the remaining fields where the galaxy halo is weak. On the other hand, the second task adds the respective objects in the science images using the PSF model previously obtained (see Section 2.2). Subsequently, we applied the same script mentioned in Section 2.2 to recover the artificial objects added in the images.

The obtained results of our completeness tests are shown in Fig. 2. The upper panel shows the fraction of artificial objects recovered $(f)$, as a function of the input magnitude. The same panel shows with the dotted-dashed line the completeness analysis performed


Figure 2. Upper panel: completeness fraction as a function of $g_{0}^{\prime}$ magnitude. The solid, dashed, and dotted lines correspond to the three studied GMOS fields of NGC 4546. The dot-dashed grey line shows the completeness of the comparison field (WHDF; Section 2.5). Bottom panel: image $g^{\prime}$ of the central region of NGC 4546 after the subtraction of its surface brightness. The black continuous, dashed, and dotted circles indicate the regions from which a completeness level greater than 80 per cent is obtained for $g_{0}^{\prime}=25$, 25.2 , and 25.4 mag, respectively.
over the comparison field used in this work (see Section 2.5). As seen in Fig. 2, at $g_{0}^{\prime}=25.2$ mag our data have a completeness level greater than 80 per cent.

In addition, we perform completeness tests as a function of the galactocentric radius, since lower completeness is expected towards the central region of the galaxy due to its brightness. The experiments were performed considering the magnitude value previously obtained ( $g_{0}^{\prime}=25.2 \mathrm{mag}$ ), and values above and below it $\left(g_{0}^{\prime}=25\right.$ and $\left.g_{0}^{\prime}=25.4 \mathrm{mag}\right)$. The lower panel of Fig. 2 shows the different limits in galactocentric radius ( 16,22 , and $30 \operatorname{arcsec}$ ) where an 80 per cent completeness level is obtained for the magnitudes $g_{0}^{\prime}=25,25.2$, and 25.4 , respectively. These results were considered for the analysis of the azimuthal and radial distribution of the GC system of NGC 4546 (Section 4.5), as well as for its luminosity function (Section 4.6).

### 2.5 Comparison field

Previous studies (e.g. Bridges et al. 2006; Pierce et al. 2006a,b; Faifer et al. 2011) have shown that observations in three or more photometric bands with good seeing conditions (FWHM $<1$ arcsec) allows selection of GC samples with limited contamination by background objects. The main contamination sources in catalogues


Figure 3. Colour-magnitude diagram with the unresolved sources detected in the WHDF field (black dots) and those obtained from trilegal Galaxy model (open circles). Grey dashed line shows the limiting magnitude adopted in Section $2.4\left(g_{0}^{\prime}=25.2 \mathrm{mag}\right)$ corresponding to 80 per cent of completeness.
are associated with background galaxies, unresolved stellar systems, and Milky Way (MW) stars. Most of these objects can present colours within the typical ranges displayed by GCs (Fukugita, Shimasaku \& Ichikawa 1995). For this reason, it is of utmost importance to consider the effect that these objects can have on the integrated colour distributions, as well as on any other analysis performed on extragalactic GC systems.

We were unable to obtain a comparison field as part of our Gemini programme. Furthermore, a GOA search for imaging of similar depth and quality near to NGC 4546 also gave a negative result. For these reasons, we decided to use the William Herschel Deep Field (WHDF; Metcalfe et al. 2001) to estimate the contamination in our photometric catalogue. The reduction process of this field was performed according to the procedures described in Sections 2.12.3. Used as comparison field in other works (Faifer et al. 2011; Caso et al. 2015; Salinas et al. 2015), this data set has the advantage that was observed with the GMOS instrument in the $g^{\prime} r^{\prime} i z^{\prime}$ filters with a photometric depth and FWHM comparable to our data (upper panel of Fig. 2). In addition, according to the Galactic latitude and longitude of this field $\left(b=-61.7^{\circ}, l=107.5^{\circ}\right)$, the largest number of contaminants would be due to unresolved background galaxies (Faifer et al. 2011). Therefore, we complemented this sample with the expected stars in the Galactic region of NGC 4546, using the stellar population synthesis code TRILEGAL (Girardi et al. 2005). Based on this analysis, we estimate a contamination of 11 per cent in our GC sample for $g_{0}^{\prime}<25.2$ mag. Fig. 3 shows the colourmagnitude diagram with the objects detected in the WHDF field identified as unresolved sources according to SEXTRACTOR (CLASS STAR $>0.5$ ), and those obtained by TRILEGAL.

## 3 SURFACE PHOTOMETRY OF NGC 4546

We analysed the light distribution of NGC 4546 in the $g^{\prime}$ and $z^{\prime}$ images in order to obtain the surface brightness profiles of the galaxy and also information about its different photometric
structures. To do this, we ran the IRAF task ELLIPSE commonly used to measure the surface photometry of galaxies (Li et al. 2011; Lane, Salinas \& Richtler 2013; Escudero et al. 2015, 2018), and the GALFIT ${ }^{2}$ 3.0.5 software (Peng et al. 2002, 2010) to perform a 2 D multicomponent decomposition. Furthermore, the results obtained from these analyses were subsequently used to compare with some features exhibited by the GC system of NGC 4546 (see Section 4.5).

Given that the galaxy's light fills the GMOS FoV of the central pointing, in order to estimate a fair value of the sky background level and perform a good modelling of the galaxy's profile at large radii, we build $g^{\prime}$ and $z^{\prime}$ mosaics with our images using the THELI ${ }^{3}$ data reduction pipeline (Erben et al. 2005; Schirmer 2013). This allows us to reach a distance of $7.4 \mathrm{arcmin}(\sim 30 \mathrm{kpc})$ from the galactic centre to the edge of the mosaic.

### 3.1 Ellipse model

Initially, we ran ELLIPSE in the $g^{\prime}$ band to obtain the surface brightness profile of the galaxy, previously masking unresolved and extended bright sources in the mosaic using the IRAF task OBJMASK. In addition, since the galactic centre in our images is saturated ( $r$ $<1.5 \mathrm{arcsec}$ ), we also mask this region. During the fit process, we allow the free variation of the isophotal parameters [centre, ellipticity, and position angle (PA) of the ellipses] in the range of $0.16-2.5 \mathrm{arcmin}(0.64-10.05 \mathrm{kpc})$ of semimajor axis (SMA). From this last value and up to SMA~7 arcmin ( 28.1 kpc ), given the lowsurface brightness of the galaxy in these regions, all the parameters mentioned above were fixed in order to ensure the convergence of the fitting process. The same procedure was subsequently applied to the $z$ mosaic.

Fig. 4 shows the variation of the isophotal parameters (ellipticity, PA, and the Fourier coefficient $B_{4}$ ) and the surface brightness profile ( $g^{\prime}$ filter) as a function of the equivalent radius $\left(r_{\mathrm{eq}}{ }^{4}\right)$. As can be seen, the isophotal fit in the central region of NGC 4546 shows a significant variation in the PA, changing $\sim 15^{\circ}$ within $r_{\text {eq }}<0.2$ $\operatorname{arcmin}(0.8 \mathrm{kpc})$. This variation is also reflected in the ellipticity, ranging from $\sim 0.15$ to 0.5 within the mentioned radius. In addition, the Fourier coefficient $B_{4}$ changes from boxy $\left(B_{4}<0\right)$ to discy $\left(B_{4}\right.$ $>0$ ) isophotes in the same region.

After subtracting our $g^{\prime}$ model, different dust regions around the galaxy's nucleus are revealed. Some of these structures extend up to a distance of $0.86 \operatorname{arcmin}(3.5 \mathrm{kpc})$ from the galactic centre. To highlight these structures and any other peculiarities in the galaxy, we generated a 2D colour map using our $g^{\prime}$ and $z^{\prime}$ images. The colour map (Fig. 5) reveals in great detail the existence of remarkable irregular dust structures along the major axis of NGC 4546, with colours ranging from $\left(g^{\prime}-z^{\prime}\right)_{0} \sim 1.3$ to 1.5 mag , and also a smooth colour gradient of the stellar component of the galaxy, of $\Delta\left(g^{\prime}-\right.$ $\left.z^{\prime}\right)_{0} / \Delta r \sim 0.1 \mathrm{mag}$ within $r_{\mathrm{eq}}<0.8 \operatorname{arcmin}(\sim 3 \mathrm{kpc})$. In addition, the location of the UCD (NGC4546-UCD1; Norris et al. 2015) is shown with a white circle in this figure.

In order to characterize the global surface brightness of the galaxy and obtain their structural parameters, we fit the Sérsic function (Sérsic 1968) to the obtained profiles $g^{\prime}$ and $z^{\prime}$. The analytical

[^2]

Figure 4. Isophotal parameters as a function of the equivalent galactocentric radius. From top to bottom, the different panels show the ellipticity, PA, Fourier coefficient $B_{4}$, surface brightness profile in $g^{\prime}$ filter, and the residual between the data and the fitted Sérsic function.


Figure 5. $\left(g^{\prime}-z^{\prime}\right)_{0}$ colour map of NGC 4546. Irregular dust structures can be observed around the galactic centre. The white cross and circle indicate the location of the galactic centre and the UCD, respectively.
expression of this function has the following form:
$\mu(r)=\mu_{\mathrm{eff}}+\left(\frac{2.5 b_{n}}{\ln 10}\right)\left[\left(\frac{r}{R_{\mathrm{eff}}}\right)^{(1 / n)}-1\right]$,
with $R_{\text {eff }}$ the effective radius of the galaxy, $\mu_{\text {eff }}$ the surface brightness at that radius, $n$ the Sérsic index, and $b_{n}=1.9992 n-0.3271$. The fits were performed in the range of $0.04-4.5$ arcmin, with the aim to avoid the saturated innermost region, and the outer region

Table 3. Best-fitting parameters of the Sérsic profile ( $\mu_{\text {eff }}, R_{\text {eff }}$, and $n$ ) and total magnitudes obtained in filters $g^{\prime}$ and $z^{\prime}$.

| Filter | $\mu_{\text {eff }}$ <br> $\left(\mathrm{mag} \mathrm{arcsec}^{-2}\right)$ | $R_{\text {eff }}$ <br> $(\operatorname{arcsec})$ | $n$ | $m_{0}$ <br> $(\mathrm{mag})$ |
| :--- | :---: | :---: | :---: | :---: |
| $g^{\prime}$ | $20.84 \pm 0.05$ | $22.20 \pm 0.6$ | $4.06 \pm 0.08$ | $10.71 \pm 0.11$ |
| $z^{\prime}$ | $19.26 \pm 0.04$ | $19.93 \pm 0.6$ | $3.87 \pm 0.07$ | $9.40 \pm 0.10$ |

probably influenced by the sky level. The parameters obtained are listed in Table 3. The mean value of the effective radius obtained for NGC 4546 of the fits is $\left\langle R_{\text {eff }}\right\rangle=21.1 \pm 0.8 \operatorname{arcsec}$ $(\sim 1.39 \pm 0.05 \mathrm{kpc})$. This value is in good agreement in comparison with the values obtained by Bettoni et al. (1991) ( $R_{\text {eff }}=21.7$ arcsec $)$ and Cappellari et al. (2013) ( $R_{\text {eff }}=22.23$ arcsec $)$. In addition, we compute the total $g_{0}^{\prime}$ and $z_{0}^{\prime}$ magnitudes of the galaxy by integrating expression 2.

### 3.2 GALFIT model

Although the 1D surface brightness profile of NGC 4546 is modelled relatively well with only one Sérsic function (Section 3.1), this approach is not very effective in identifying the different photometric subcomponents of the galaxy. Therefore, we used the software GALFIT to perform 2D multicomponent decomposition in our images. GALFIT is a 2D data analysis algorithm designed to fit multiple parametric functions simultaneously (Sérsic, Gaussian, Moffat, etc.), and also allow the modelling of non-axisymmetrical structures (bars, spiral arms, tidal features, etc.).

In this work, we ran GALFIT on our $g^{\prime}$ and $z^{\prime}$ mosaics and fit Sérsic and exponential functions, given their flexibility. In addition, since the galaxy presents boxy and discy isophotes (see Section 3.1), in order to quantify the degree of asymmetry in the galaxy and simulate these types of isophotes, we considered the Fourier modes $m=1$ and $m=4$. Initially, we started by fitting a single Sérsic component using as initial parameters those obtained in Section 3.1. Afterwards, we added additional components and carefully inspecting the residuals obtained in each case. In each run, we considered the object mask, and the empirical PSF previously obtained in Section 2.2. Since the galaxy centre in our images is saturated ( $r<1.5 \operatorname{arcsec}$ ), we also mask this region before running GALFIT. Several tests were performed by varying the initial values of the parameters of each component, in order to test the reliability of our results. In all cases, these modifications did not have significant effect on the final models.

The maximum number of fitted components was determined following the procedure of Huang et al. (2013). The 1D surface brightness profile of each obtained model was extracted, and subsequently, the isophotal parameters were compared with that derived from the original data. According to these authors, 'the best model is one that it contains a minimum number of components with reasonable, robust parameters that describe visibly distinct structure'.

In our case, the best model (Fig. 6) in the aforementioned filters was obtained considering four components: three Sérsic functions and one exponential. The innermost Sérsic indicates the presence of the galaxy's bulge, while the remaining two Sérsic components would indicate the presence of lens/disks. The fit of these three components is similar to the analysis obtained by Gao et al. (2018) on NGC 4546. In that work, the authors mention that the galaxy is probably composed of a thin and a thick disc, denoted as a possible lens and a disc. In our analysis, the fit of these three


Figure 6. Upper panel: comparison between the 1D profile of the data and the obtained GALFIT model. From top to bottom, the different panels show the ellipticity, PA, surface brightness profile in $g^{\prime}$ filter, and the residual between the data and the four considered functions. The red, magenta, blue and green dotted lines show the different subcomponents used for the GALFIT model. Bottom panel: residual $g^{\prime}$-image after subtracting the obtained GALFIT model. The ellipses represent $R_{\text {eff/s }}$, ellipticity, and PA of each fitted component (colour figure in the online version).
functions left an excess of light in the residual image. Therefore, we consider a fourth additional model component through an exponential function, which would represent a faint extended halo. Table 4 lists the best-fiting parameters for the final model in the filters $g^{\prime}$ and $z^{\prime}$. Although the bulge+disc decomposition performed by Bettoni et al. (1991) suggested the possible presence of a small bar in NGC 4546 together with two spiral-like structure, we have not detected these features in our analysis. Therefore, our results are in agreement with Gao et al. (2018).

Table 4. Parameters obtained by GALFIT for each fitted function. The different columns indicate the used filters, fitted models, the individual components, surface brightness for Sérsic and exponential functions, effective radius ( $R_{\text {eff }}$ ) for the Sérsic function and scale length $\left(R_{\mathrm{S}}\right)$ for the exponential function, Sérsic index, ellipticity, PA, the apparent magnitude of each component in the respective filter, and the $\chi^{2} / v$ value obtained, respectively.

| Filter | Model | Component | $\mu_{\mathrm{eff} / \mathrm{s}}$ <br> $\left(\mathrm{mag} \mathrm{arcsec}^{-2}\right)$ | $R_{\mathrm{eff} / \mathrm{s}}$ <br> $(\mathrm{arcsec})$ | $n$ | Ellip | PA <br> $(\mathrm{deg})$ | $m_{g^{\prime} / z^{\prime}}$ <br> $(\mathrm{mag})$ | $\chi^{2 / v}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $g^{\prime}$ | Sérsic | Bulge | 18.4 | 4.3 | 1.70 | 0.16 | 65.3 | 12.28 | 0.9 |
|  | Sérsic | Lens/disc | 20.5 | 23.1 | 0.72 | 0.60 | 77.5 | 11.13 |  |
|  | Sérsic | Disk | 22.4 | 49.5 | 0.86 | 0.48 | 79.6 | 11.30 |  |
|  | Exp. | Halo | 23.4 | 83.6 | - | 0.39 | 80.1 | 11.10 |  |
| $z^{\prime}$ | Sérsic | Bulge | 17.0 | 4.0 | 1.75 | 0.14 | 55.3 | 11.42 | 2.0 |
|  | Sérsic | Lens/disc | 18.9 | 22.1 | 0.94 | 0.59 | 76.9 | 9.51 |  |
|  | Sérsic | Disc | 21.3 | 45.9 | 0.84 | 0.46 | 80.4 | 10.38 |  |
|  | Exp. | Halo | 21.9 | 61.0 | - | 0.36 | 76.9 | 10.27 |  |



Figure 7. Photometric errors for different colour indices used in this study (shifted vertically to avoid overlapping). The vertical dashed line indicates the magnitude corresponding to the photometry errors for the colour indices of $\sim 0.1 \mathrm{mag}$.

As observed in Fig. 6 (upper panel), the final model reproduces in great detail the global structure (ellipticity and PA) of the galaxy. The bottom panel in this figure shows the resulting image in filter $g^{\prime}$ after subtracting the GALFIT model, where the different regions of dust can be observed as whiter regions.

## 4 GC SYSTEM OF NGC 4546

### 4.1 GC candidates

The quality of our photometry is reflected in Fig. 7, where the colour errors obtained at $g_{0}^{\prime}=25.2 \mathrm{mag}$ ( 80 per cent completeness) are $\sim 0.12 \mathrm{mag}$. In order to reduce the contamination effect and the photometric errors in our catalogue, we adopted a slightly brighter magnitude limit of $g_{0}^{\prime}=25 \mathrm{mag}$. At this limit, the colour errors are lower than $\sim 0.1 \mathrm{mag}$.

Fig. 8 shows the colour-magnitude (CM; upper panel) diagram and colour-colour (CC; bottom panel) diagram of all unresolved sources detected in our GMOS mosaic. The horizontal dashed line in the CM diagram indicates the limiting magnitude corresponding to $\epsilon_{\left(g^{\prime}-i^{\prime}\right)} \sim 0.1$ mag. As seen in the CC diagram, the GC candidates of NGC 4546 are relatively easy to identify since they are grouped around specific colours $\left[\left(g^{\prime}-r^{\prime}\right)_{0} \sim 0.65 \mathrm{mag},\left(r^{\prime}-z^{\prime}\right)_{0} \sim 0.5\right.$ mag; bottom panel in Fig. 8].


Figure 8. Upper panel: colour-magnitude diagram with all the unresolved sources detected in our GMOS mosaic (grey dots), as well as our final sample of GC candidates (black dots inside the box). The horizontal dashed line indicates the magnitude corresponding to $\epsilon\left(g^{\prime}-i^{\prime}\right) \sim 0.1$ mag. Bottom panel: colour-colour diagram with the unresolved sources brighter than $g_{0}^{\prime}=25 \mathrm{mag}$. The dashed grey lines show the colour ranges considered for the selection of GC candidates.

The selection of GC candidates was performed considering broad colour ranges similar to the values commonly used in this type of study and photometric system (Faifer et al. 2011; Escudero et al. 2018). The complex photometric substructure evidenced by our analysis presented in Section 3.2, added to the irregular dust structures, the ionized gas rotating in the opposite direction to its stellar disc, and the young UCD, point to a merger event in the past of NGC 4546. In that context, and in order to detect not just 'classic' blue and red GCs candidates, we decided to apply slightly wider colour cuts in our GC candidates selection. Therefore, we considered the following ranges $0.32<\left(g^{\prime}-r^{\prime}\right)_{0}<1.0,0<\left(r^{\prime}-\right.$ $\left.i^{\prime}\right)_{0}<0.7,0.5<\left(g^{\prime}-i^{\prime}\right)_{0}<1.5,0.6<\left(g^{\prime}-z^{\prime}\right)_{0}<1.9,0.05<\left(r^{\prime}\right.$ $\left.-z^{\prime}\right)_{0}<1.0,-0.2<\left(i^{\prime}-z^{\prime}\right)_{0}<0.7 \mathrm{mag}$. Regarding the bright end in the CM diagram, we adopt the magnitude limit $g_{0}^{\prime}=20.1 \mathrm{mag}$, equivalent to the value $M_{V} \sim-11 \mathrm{mag}$ suggested by Mieske et al. (2006) to separate GCs from massive clusters, UCDs, and/or MW stars.

As a final step, we conducted a visual inspection of the selected objects to avoid incorrect detections or artefacts in the final sample. A total of 350 GC candidates meet the criteria mentioned above, which are shown with black dots in Fig. 8.

### 4.2 GC colour distribution

Initially, with the aim to identify the possible different GC subpopulations present in NGC 4546, we obtained the background-corrected colour histogram $\left(g^{\prime}-i^{\prime}\right)_{0}$ adopting a bin size of 0.055 mag (the upper panel in Fig. 9). In addition, a Gaussian kernel with $\sigma=0.04$ mag was applied to obtain the smoothed colour distribution. As seen in the figure, the histogram shows hints of different substructures that survive the background correction: at least two peaks at ( $g^{\prime}$ $\left.-i^{\prime}\right)_{0} \sim 0.79$ and $\left(g^{\prime}-i^{\prime}\right)_{0} \sim 1.05 \mathrm{mag}$, and a small group of GC candidates towards redder colours at $\left(g^{\prime}-i^{\prime}\right)_{0} \sim 1.4$ mag. The location of the first two peaks agrees with typical values for the blue and red GC subpopulations, respectively.

Subsequently, we used the more metallicity sensitive colour index $\left(g^{\prime}-z^{\prime}\right)_{0}$ to corroborate the presence of these different groups. In this case, we built up the background-corrected $\left(g^{\prime}-z\right)_{0}$ histogram adopting a slightly larger bin size of 0.06 mag and a Gaussian kernel with $\sigma=0.05 \mathrm{mag}$ (the bottom panel in Fig. 9). As can be seen in the figure, two clear peaks are observed at $\left(g^{\prime}-z^{\prime}\right)_{0} \sim 0.9$ and $\left(g^{\prime}-z^{\prime}\right)_{0} \sim 1.15 \mathrm{mag}$, with an extended count of objects towards redder colours. Using the relationship of Peng et al. (2006) about the behaviour of the blue and red GC subpopulations as a function of galaxy luminosity, we observe that the peak at $\left(g^{\prime}-z^{\prime}\right)_{0} \sim 0.9$ mag in NGC 4546 results in good agreement with the values of blue subpopulations, while the peak at $\left(g^{\prime}-z^{\prime}\right)_{0} \sim 1.15 \mathrm{mag}$ is bluer compared with the typical values for red subpopulations.

In order to corroborate the bimodal or multimodal character of both colour distribution, as usual, we performed fits of different Gaussian components to the $\left(g^{\prime}-i^{\prime}\right)_{0}$ and $\left(g^{\prime}-z^{\prime}\right)_{0}$ backgroundcorrected histograms using the RMIX ${ }^{5}$ software. It is important to mention that although there is no physical reason to use Gaussian function in this type of analysis, they provide an adequate description of the integrated colour distributions and it allow us to compare NGC 4546 with other galaxies studied in the literature.
The solutions obtained considering the fit with two Gaussian components (Fig. 9) were $\mu_{1}=0.77 \pm 0.03\left(\sigma_{1}=0.05 \pm 0.03\right)$
${ }^{5}$ RMIX is publicly available at http://www.math.memaster.ca/peter/mix/mix .html


Figure 9. Upper panel: $\left(g^{\prime}-i^{\prime}\right)_{0}$ background-corrected colour histogram for the GC candidates (grey line). The black line shows the smoothed colour distribution with a Gaussian kernel of 0.04 mag. Bottom panel: $\left(g^{\prime}-z^{\prime}\right)_{0}$ background-corrected colour histogram (grey line). A Gaussian kernel of 0.06 mag was applied (black line). Blue and red dashed lines indicate the Gaussian components fitted by RMIX, where their sum is indicated by a black dashed line (colour figure in the online version).
and $\mu_{2}=1.02 \pm 0.03\left(\sigma_{2}=0.18 \pm 0.02\right)$ for the colour index $\left(g^{\prime}-i^{\prime}\right)_{0}$; and $\mu_{1}=0.93 \pm 0.02\left(\sigma_{1}=0.05 \pm 0.02\right)$ and $\mu_{2}=$ $1.21 \pm 0.03\left(\sigma_{2}=0.24 \pm 0.02\right)$ for the colour index $\left(g^{\prime}-z^{\prime}\right)_{0}$. This analysis indicates that according to statistical indicators such as $\chi^{2}$, the bimodal description is appropriate in both cases. Our attempts of including a greater number of Gaussian components show that, although they provide a better formal description of the substructure of the distributions, they overfit the data and turn out not to be statistically significant. However, a visual inspection of both figures shows that if the $\left(g^{\prime}-i^{\prime}\right)_{0}$ and $\left(g^{\prime}-z^{\prime}\right)_{0}$ distributions are truly bimodal, then the red subpopulation is strangely and strongly dominant in NGC 4546 (see the discussion in Section 5). Similar cases can be seen in Blom et al. (2012) and Escudero et al. (2015), where the presence of more than two subpopulations is proposed.

Therefore, we explore a different approach consisting in evaluate the hypothesis of multimodality of the colour distribution in
the colour plane. If those distributions in a plane that involves two metallicity-sensitive indices are constituted by two dominant subpopulations (the classic blue and red), in addition to other less populated ones, then its projection on one of the axes of the plane can make it more difficult to identify them. Especially, if one considers that NGC 4546 does not have thousands of GCs as more massive galaxies.

In this context, using the joint information of the colour indices $\left(g^{\prime}-z^{\prime}\right)_{0}$ and $\left(g^{\prime}-i^{\prime}\right)_{0}$ via the CC diagram, we made a probabilistic classification of the different GC groups in NGC 4546. To do this, we applied the Gaussian mixture model (GMM) algorithm using the open source machine learning library SCIKIT-LEARN ${ }^{6}$ for PYTHON (de Souza et al. 2017). GMM is a parametric probability density function to describe the data distribution in certain feature space as a weighted sum of Gaussian component densities.

For a total of $K$ components in an $n$-dimensional parameter space, the final probability distribution $p(x)$ is given by the equation,
$p(x)=\sum_{i=1}^{K} w_{i} \phi\left(x ; \vec{\mu}_{i}, \vec{\Sigma}_{i}\right)$,
where $w_{i}$ are the mixture weights, and $\phi\left(x ; \vec{\mu}_{i}, \vec{\Sigma}_{i}\right)$ the distribution of each individual Gaussian cluster, characterized by its mean vector $\vec{\mu}_{i}$ and covariance matrix $\vec{\Sigma}_{i}$ :
$\phi\left(x ; \vec{\mu}_{i}, \vec{\Sigma}_{i}\right)=\frac{1}{\sqrt{(2 \pi)^{d}\left|\vec{\Sigma}_{i}\right|}} e^{-\frac{1}{2}\left(x-\vec{\mu}_{i}\right) \vec{\Sigma}_{i}^{-1}\left(x-\vec{\mu}_{i}\right)}$.
In this work, we fit GMM to our data set using the ExpectationMaximization algorithm. However, since a priori we do not know the number of groups in which the data substructure is separated, in order to determine the best number of Gaussian clusters $K$ in the CC diagram of our GC sample, we adopted the Akaike information criterion (AIC; Akaike 1974). This parameter is a measure of the relative quality of a statistical model (sum of Gaussian components) for a data set. In this case, we obtained different AIC values for a range of $K$ components (from 1 to 9). Subsequently, we use the elbow method (see e.g. Baron 2019) to select the optimal number of groups in our data set. Fig. 10 (upper panel) shows that the AIC solution suggests a minimum number of five groups in our sample. The bottom panel in Fig. 10 shows the five groups obtained by GMM in the CC diagram, where the ellipses represent the 68 percent and 95 percent confidence interval of the fitted Gaussian components. Different tests were performed considering GC samples towards brighter magnitudes ( $g_{0}^{\prime}<23.5,24,24.5 \mathrm{mag}$ ). In most cases, the minimum number of fitted components was five, except for the sample with $g_{0}^{\prime}<23.5 \mathrm{mag}$ (four components) where the 'reddest' colour component is not observed. According to GMM, the membership of the GC candidates to each group was made considering a belonging probability superior to 50 per cent. Table 5 lists the parameters obtained by GMM considering the whole GC sample.

Similar to that observed in both colour histograms (upper and bottom panels in Fig. 9), two well-marked groups are identified, indicating the typical blue and red GC subpopulations (components B and D in Fig. 10). On the other hand, a third group with intermediate colours (component C), and two additional groups towards the end of the colour sample (components A and E) are detected. These last three groups could be associated with GC candidates of different ages and/or metallicities than the classic blue

[^3]

Figure 10. Upper panel: AIC as a function of the number of the fitted Gaussian components $(K)$. Bottom panel: Colour-colour diagram backgroundcorrected with the five-considered Gaussian components. The small and large ellipses represent 68 percent and 95 percent confidence intervals of the different Gaussian components, respectively. The black filled circle indicates the position of the UCD.
and red ones, or even be extensions and combinations of the latter. Fig. 10 includes the UCD analysed by Norris et al., which according to its integrated colours probably belongs to group D. However, it is not possible to interpret the position of this object in the colour planes in a straightforward manner because it is not an SSP and shows an extended star formation history (Norris et al. 2015). On the other hand, although the presence of multiple subpopulations has been studied in GC systems associated with early-type galaxies (Woodley et al. 2010; Blom et al. 2012; Caso et al. 2015; Escudero et al. 2015; Sesto et al. 2016), it should be considered the possibility that the use of Gaussian components for this type of analysis may not be unique. Therefore, the decomposition used in this work should be considered with caution.

As additional tests, we created hundreds of simulated distributions with a number of objects similar to the observed GC sample, in order to reproduce the different groups identified in the colour plane of NGC 4546. Additionally, we add 12 per cent of background contamination in these samples. Initially, we simulate 2 groups of objects with mean colours and dispersions similar to the blue and red GC subpopulation of NGC 4546, and we ran our AIC and GMM analysis to check if they were recovered. We repeat this procedure

Table 5. Parameters obtained by GMM in the fitting of five Gaussian components on the CC diagram $\left[\left(g^{\prime}-i^{\prime}\right)_{0}\right.$ versus $\left.\left(g^{\prime}-z^{\prime}\right)_{0}\right]$. Shown are the number of GC candidates associated with each group $\left(p_{i}\right)$, the mixture weights $\left(w_{i}\right)$, central vectors of the groups $\left(\vec{\mu}_{i}\right)$, and covariance matrices $\left(\vec{\Sigma}_{i}\right)$.

| Parameter | Value |
| :--- | :---: |
| $p_{\mathrm{A}}$ | 39 |
| $p_{\mathrm{B}}$ | 116 |
| $p_{\mathrm{C}}$ | 49 |
| $p_{\mathrm{D}}$ | 106 |
| $p_{\mathrm{E}}$ | 40 |
| $w_{\mathrm{A}}$ | 0.113 |
| $w_{\mathrm{B}}$ | 0.327 |
| $w_{\mathrm{C}}$ | 0.143 |
| $w_{\mathrm{D}}$ | 0.295 |
| $w_{\mathrm{E}}$ | $\left(g^{\prime}-z^{\prime}\right)$ |
|  | $\left(g^{\prime}-i^{\prime}\right)$ |
| $\vec{\mu}_{\mathrm{A}}$ | $(0.783$ |
| $\vec{\mu}_{\mathrm{B}}$ | $(0.963$ |
| $\vec{\mu}_{\mathrm{C}}$ | $(1.153$ |
| $\vec{\mu}_{\mathrm{D}}$ | $(1.316$ |
| $\vec{\mu}_{\mathrm{E}}$ | $(1.545$ |

500 times. Similarly, we conducted experiments considering three and four simulated groups representing the four reddest groups of NGC 4546. Left and central panels in Fig. 11 show the 500 experiments performed for the simulated cases of two and four groups, respectively. In all cases, we obtained that the method used in this work was able to efficiently recover the simulated distributions in more than 90 per cent of the cases. Interestingly, we found that the inclusion of polluting background objects in the experiments makes the number of ideal components go from four to five. An inspection of this fifth component shows that it corresponds in colour to the ' A ' component previously identified in our sample of GC candidates. As the last test, we generated random samples of objects following a homogeneous distribution in the colours
$\left(g^{\prime}-z^{\prime}\right)$ and $\left(g^{\prime}-i^{\prime}\right)$ and we ran AIC again (the right-hand panel in Fig. 11). In the latter case, when quantifying the optimal number of groups obtained in each experiment, AIC estimated four groups in 42 per cent of the cases, five groups in 38 per cent, and six groups in the remaining 20 percent. Although the central panel (simulation with four groups) and right-hand panels (simulation with uniform sample) of Fig. 11 seem to be similar at first glance, according to the values mentioned above, these results indicate that AIC cannot accurately discern the optimal number of groups for the latter case.

### 4.3 Spatial distribution

It is known that 'blue' and 'red' GCs have different 2D spatial distribution in the sense that blue GCs have more extended and less concentrated distribution than the red GCs (e.g. Usher et al. 2013; Harris, Blakeslee \& Harris 2017; Escudero et al. 2018). Analysing the spatial concentration towards the galaxy of the different samples of GCs candidates can help us to evaluate the reliability of our selection criteria. Additionally, merger events and/or interactions between galaxies can originate new clusters, and also affect the spatial distribution of the stellar populations as well as native GC subpopulations (Bonfini et al. 2012; Sesto et al. 2018). In this sense, the spatial anisotropy observed in some GC systems associated with early-type galaxies has been used to investigate the assembly history of the latter (e.g. D'Abrusco et al. 2014).
In Fig. 12, we show the projected spatial distribution of each group of GC candidates assigned by GMM (see Section 4.2). As can be seen, the blue GC candidates (group B; upper panel) show an extended spatial distribution over the whole GMOS mosaic, with a slight concentration towards NGC 4546. In contrast, the red GC subpopulation (group D; bottom panel) shows a high concentration towards the galactic centre, with approximately 72 per cent of its candidates located within $1.5 \operatorname{arcmin}(6 \mathrm{kpc})$ of galactocentric radius. Similar behaviour is shown by the intermediate GC candidates (group C; middle panel). On the other hand, when observing the spatial distribution of GC candidates in the field of our mosaic containing the neighbouring galaxy CGCG 014-074 (see Fig. 12), there is no significant concentration of objects around it.

Finally, GC candidates associated by GMM to groups with bluer and redder colours (groups A and E) seem to share similarities in its spatial distribution regarding the classic blue and red GC subpopulations (groups B and D), respectively. In particular, it can be seen that the objects belonging to group A do not show a significant spatial concentration on the GMOS mosaic (the upper panel in Fig. 12). In addition, they seem to show a wide brightness range ( $20.5<g_{0}^{\prime}<24.5 \mathrm{mag}$ ) when observing their location in the


Figure 11. AIC as a function of the number of the fitted Gaussian components ( $K$ ) obtained for the 500 experiments performed considering the simulated case of two groups of objects (left-hand panel), four groups (central panel), and considering a sample of objects following a uniform distribution in colours ( $g^{\prime}-$ $z^{\prime}$ ) and $\left(g^{\prime}-i^{\prime}\right)$ (right-hand panel).


Figure 12. Projected spatial distribution of the different GC groups in NGC 4546 assigned by GMM. Upper panel: light green triangles and blue circles represent groups A and B, respectively. Middle panel: green filled circles indicate group C . Bottom panel: magenta circles and orange triangles represent groups $D$ and $E$, respectively. In all panels, the black pentagon and cross indicate the galactic centre of NGC 4546 and the companion galaxy CGCG014-074, respectively. Grey dots represent the entire GC sample associated with NGC 4546. As a comparison, the black ellipse represents the orientation and elongation of the galaxy at $5 R_{\text {eff }}$ (colour figure in the online version).

CM diagram $\left(\left(g^{\prime}-i^{\prime}\right)_{0} \sim 0.6 \mathrm{mag} ;\right.$ Fig. 8). In this context, since the galaxy does not show regions of recent star formation on its colour map (see Fig. 5), the presence of very blue objects with the aforementioned features would suggest that group A is probably composed of MW stars and some bona fide GCs.

In the opposite case, the spatial distribution of the reddest objects (group E) shows a detectable concentration around the galactic centre. A very simple exercise shows that around 60 per cent of this subsample is located inside $R_{\text {gal }} \sim 1.5$ arcmin. However, Fig. 8 shows that in this case, the use of a simple selection criterion such as cuts in different colours leaves GC candidates that are located on the stellar sequence of the MW. In this point, we could adopt a more restrictive cut in colours, but doing it we could reject some non-classic but genuine GCs. Therefore, in an alternative way, we analyse the spatial distribution of these candidates by splitting group E into two samples considering objects located at $R_{\text {gal }}<1.5$ and $R_{\text {gal }}>1.5 \operatorname{arcmin}(6 \mathrm{kpc})$. Fig. 13 shows with orange filled triangles and open squares the location of these two subsamples in the CC diagram, respectively. As seen in the figure, objects with $R_{\text {gal }}>$ 1.5 arcmin (open squares) are mostly located over the region of the stellar sequence, possibly associated with stars of the MW,


Figure 13. Colour-colour diagram with the final sample of GC candidates of NGC 4546 (black dots), the unresolved sources detected in our GMOS mosaic (grey dots), and the GC candidates belonging to the group E according to GMM (orange symbols). Orange filled triangles and open squares indicate those objects located at $R_{\text {gal }}<1.5$ and $R_{\text {gal }}>1.5 \mathrm{arcmin}$, respectively. Cyan circle indicates the UCD. The dashed grey lines show the colour ranges considered for the selection of GC candidates (colour figure in the online version).
while objects closer to the galaxy ( $R_{\text {gal }}<1.5$ arcmin; orange filled triangles) have a different behaviour, showing wide ranges in ( $r$ $\left.-z^{\prime}\right)$ colour. Therefore, the possibility that these objects are an extension of the classic red clusters and not a different subpopulation cannot be ruled out.

The previous qualitative analysis can be also seen in the smoothed colour index $\left(g^{\prime}-z^{\prime}\right)_{0}$ diagram as a function of the projected galactocentric radius ( $R_{\text {gal }}$ ). As seen in Fig. 14, the blue GC subpopulation (group B) is extended over the GMOS mosaic ( $R_{\text {gal }}$ $\gtrsim 0.25 \mathrm{arcmin} ; \gtrsim 1 \mathrm{kpc}$ ), while the groups associated with the intermediate, red, and reddest GC candidates (groups C, D, and E) show a concentrated spatial distribution mainly between $0.25<R_{\text {gal }}$ $<2.4 \operatorname{arcmin}(1-9.6 \mathrm{kpc})$. On the other hand, the objects belonging to the bluest group (A) show marginal clumps between $\sim 0.7$ and 6 $\operatorname{arcmin}(2.8-24 \mathrm{kpc})$. In order to assess whether this last group is still detected towards smaller galactocentric radii, we performed a test considering those objects located at $R_{\text {gal }}<1.5$ arcmin. In this case, Akaike's solution suggests that at least four groups represent this sample, where groups B, C, D, and E are identified again. Therefore, this reinforces the idea that group ' A ' could be a mixture of objects between some bona fide GCs of NGC 4546 and MW stars.

### 4.4 Integrated colours and their comparison with SSP models

Due to the well-known 'age-metallicity degeneracy' effect in optical colours, it is not possible to obtain unique ages and metallicities estimations from them. However, we can use them to check if some SSP models can reproduce the observed mean values for the different GC subpopulations identified in Section 4.2, and thus obtain any useful indication regarding the composition of these subsamples.


Figure 14. Smoothed colour index $\left(g^{\prime}-z^{\prime}\right)_{0}$ versus galactocentric radius considering the whole sample of GC candidates (black dots). The orange solid line shows the colour profile $\left(g^{\prime}-z^{\prime}\right)_{0}$ of the galaxy. The black horizontal dashed lines indicate the mean colour $\left(g^{\prime}-z^{\prime}\right)_{0}$ assigned by GMM to the five groups.


Figure 15. Mean colours $\left(g^{\prime}-z^{\prime}\right)_{0}$ (horizontal dashed lines) obtained by GMM for each group compared with single stellar population models of Bressan et al. (2012). The black and grey lines indicate the different metallicities used $([\mathrm{Z} / \mathrm{H}]=-1.8,-1.4,-1.2,-1.0,-0.6,-0.4,-0.2,0.0$, +0.2 dex from bottom to top). Black filled circle shows the location of the UCD.

In order to do that, we compared the mean colour $\left(g^{\prime}-z^{\prime}\right)_{0}$ obtained by GMM for each group with the SSP models of Bressan et al. (2012, Fig. 15). As can be seen in Sesto et al. (2016), the photometric predictions of these models are in good agreement with observed integrated GC colours in the Sloan photometric system. We consider different metallicity values between $[\mathrm{Z} / \mathrm{H}]=$ -1.8 and +0.2 dex to cover the typical values for blue and red GC subpopulations (e.g. Usher et al. 2012). Assuming old ages between 8 and 12 Gyr for these two groups, the mean metallicity values obtained for them result in $[\mathrm{Z} / \mathrm{H}] \sim-1.2$ and $\sim-0.3$ dex, respectively. In the case of the intermediate group in our sample (group C), we see that similar metallicities to the red GC candidates (i.e. group $D$, with $[Z / H] \sim-0.4$ to -0.2 dex) in the age range of $\sim 3-7$ Gyr, or metallicity values around $\sim-0.6$ dex for an age of $\sim 10 \mathrm{Gyr}$ could reproduce the observed colours. Although values of $[\mathrm{Z} / \mathrm{H}]<-0.4 \mathrm{dex}$, and therefore ages $<3 \mathrm{Gyr}$, could be fitted to the intermediate candidates, these clusters are not significantly bright objects in our sample as seen in other galaxies with recent
star formation, such as NGC 1316 (Sesto et al. 2018). Therefore, this last option does not seem to be the case in NGC 4546. On the other hand, the bluer and redder groups defined by GMM (groups A and E) would be associated with objects with metallicities $[\mathrm{Z} / \mathrm{H}] \lesssim$ -1.0 dex $(>2 \mathrm{Gyr})$ and $[\mathrm{Z} / \mathrm{H}]>+0.0$ dex $(\geq 7 \mathrm{Gyr})$, respectively. Fig. 15 also includes the position of the UCD analysed by Norris et al. (2015) showing that its light is well represented by an SSP of around 4 Gyr old and a supra solar metallicity. This is consistent with the values obtained by these authors through the analysis of Lick indices.

### 4.5 Radial and Azimuthal distribution

With the aim of quantifying the radial and azimuthal distributions of the GC candidates in NGC 4546, we consider the following guidelines. Initially, we obtained the projected surface density profiles for the whole sample of clusters, as well as for the different subpopulations identified in Section 4.2. For this, we constructed 1D radial distributions counting objects in concentric circular rings with steps between $\Delta \log r=0.08$ and 0.12 , according to the sample analysed. Each ring was corrected for contamination and effective area. This last correction was applied in those cases where the ring exceeded the physical limit of the GMOS mosaic. The uncertainties in the surface density profiles are given by the Poisson statistic.

In order to describe the radial distribution of the different GC groups, we fit several functions to our profiles. A power law $\left(\log \sigma_{\mathrm{GC}}=a+b \log (r)\right)$, de Vaucouleurs $\left(\log \sigma_{\mathrm{GC}}=a+b r^{1 / 4}\right)$, and Sérsic profiles (i.e. $r^{1 / n}$ ) were used, with the aim to assess which of these scaling laws best represent each profile, and also to obtain some relevant parameters.

However, as seen in Fig. 12, some GC subpopulations show a significant elongation in their spatial distribution, mainly the intermediate and red subpopulations (groups C and D). Therefore, in order to obtain appropriate density profiles for each GC sample according to its orientation and spatial elongation, and subsequently, to achieve better fits of the aforementioned functions, we decided to study the azimuthal distribution of the different GC groups. For this, we constructed histograms of the azimuthal distribution for the whole GC sample, as well as for each GC group defined by GMM (Section 4.2). We count objects in different wedges within a circular ring of $0.36<R_{\text {gal }}<2.4 \operatorname{arcmin}\left(1.5<R_{\text {gal }}<9.8 \mathrm{kpc}\right)$ centred on the galaxy. The inner radius was chosen to avoid the incompleteness effect in the region near the galactic centre. On the other hand, the outer radius was chosen to cover the largest area within our GMOS mosaic, and thus avoid the correction by areal incompleteness in the counts. Fig. 16 shows the different histograms of this analysis.

Subsequently, we determined the ellipticity ( $\epsilon$ ) and PA of each sample using the expression of McLaughlin, Harris \& Hanes (1994) given by
$\sigma(R, \theta)=k R^{-\alpha}\left[\cos ^{2}(\theta-\mathrm{PA})+(1-\epsilon)^{-2} \sin ^{2}(\theta-\mathrm{PA})\right]^{-\alpha / 2}$,
where $\sigma(R, \theta)$ is the number of GC candidates, $k$ is the normalization constant, $\theta$ is the PA measured counterclockwise from the north, and $\alpha$ the value of the power-law exponent in the surface density fit. During the fit process, the free variation of the different parameters was allowed. Table 6 lists the shape parameters obtained from the azimuthal analysis and those of the stellar light distribution of the galaxy (see Section 3).

We find for the whole GC system an ellipticity of $\epsilon=0.30 \pm 0.04$, while the galaxy light has a higher value of $0.50 \pm 0.01$. This difference probably results from a combination between the azimuthal values obtained for the blue candidates (group B), which


Figure 16. Azimuthal distribution for the whole sample of GC candidates (upper panel), and for the different GC groups assigned by GMM (bottom panel) within the circular ring $0.36<R_{\text {gal }}<2.4 \operatorname{arcmin}\left(1.5<R_{\text {gal }}<\right.$ $9.8 \mathrm{kpc})$. The different colours used in the histograms are the same as those assigned for each GC subpopulation as Fig. 12. In order to avoid overlapping, the histograms corresponding to blue, intermediate, red, and reddest GC candidates were vertically shifted adding $3,13,18$, and 35 to the counts, respectively. Dotted lines in both panels show the fits obtained using expression (5). The vertical dashed line indicates the PA of the galaxy.

Table 6. Ellipticity ( $\epsilon$ ) and PA values for the GC system and for each subpopulation in NGC 4546. In addition, the mean values of these parameters obtained for the galaxy light in the range $0.2<r_{\text {eq }}<2 \operatorname{arcmin}$ (see Section 3.1) are listed.

| Population | $\epsilon$ | PA (degrees) |
| :--- | :---: | :---: |
| All | $0.30 \pm 0.04$ | $83 \pm 4$ |
| Blue (B) | $0.23 \pm 0.18$ | $99 \pm 25$ |
| Interm. (C) | $0.50 \pm 0.06$ | $92 \pm 3$ |
| Red (D) | $0.41 \pm 0.05$ | $61 \pm 6$ |
| +Red (E) | $0.46 \pm 0.20$ | $109 \pm 15$ |
| Gal. light | $0.50 \pm 0.01$ | $79 \pm 2$ |

do not show a significant ellipticity and orientation and that is reflected in their high uncertainties values, and in the relatively high values of the intermediate $(\epsilon=0.50 \pm 0.06$; group $C)$ and red GC subpopulations $(\epsilon=0.41 \pm 0.05$; group $D)$. However, the PA between the GC system and the light of NGC 4546 are in agreement within the errors $\left(\mathrm{PA}=83^{\circ} \pm 4^{\circ}\right.$ and $79^{\circ} \pm 2^{\circ}$, respectively). On the other hand, as listed in Table 6, intermediate and red GC subpopulations (group C and D) show similar values in their ellipticity as compared to the starlight of NGC 4546, but with slightly different orientations between them. In the case of
the reddest GC candidates (group E), even with a low number of objects in the considered region, it was possible to determine PA and an ellipticity, the latter being similar to those of C and D subpopulations.

With the information obtained from this analysis, we reconstructed the density profiles for the whole sample as well as for each group of GCs. The case of the intermediate, red, and reddest GC subpopulations (groups C, D and E), we considered concentric elliptical rings for their density profiles according to its PA and ellipticity values. This was also considered for the whole GC sample. On the other hand, we kept circular rings for the blue GC subpopulation (group B). Fig. 17 shows the different background corrected density profiles along with the galaxy starlight profile (see Section 3) as a function of the galactocentric radius. As seen in this figure, the density profiles of groups $\mathrm{B}, \mathrm{C}, \mathrm{D}$ and E show a decreasing behaviour as we move away from the galactic centre. In contrast, the objects belonging to group A do not show such behaviour, therefore their density profile was not included in the figure.

Afterwards, we fit the power-law, de Vaucouleurs, and Sérsic functions excluding those points centrally located ( $r<0.3$ arcmin) in order to avoid incompleteness effects. Tables 7 and 8 list the parameters and reduced chi-squared values obtained in the fits. The Sérsic profile for the reddest objects (group E) showed a high uncertainty in its parameters, probably due to the low counts in its density profile. Therefore, the values obtained by keeping free all the parameters during the fit for this group were not included in Table 8. However, we found that an exponential profile (i.e. $n=1$ ) gives a reasonable fit this group. Therefore, we include the obtained $R_{\text {eff }}$ and reduced chi-squared values for this fit in Table 8.

This analysis indicates that blue GC subpopulation (group B) has a larger effective radius than the intermediate and red GC subpopulations (groups C and D), while $R_{\text {eff }}$ values of the latter pair are similar. In this sense, the Sérsic function provides a better fit for the blue candidates, while for the intermediate and red GC candidates, the respective power-law and de Vaucouleurs functions achieve a better fit. As seen in Fig. 17 and listed in Tables 7 and 8 , red GC candidates present a higher density and concentration towards NGC 4546, showing a low value of the Sérsic index ( $n<$ 1) that gives its truncated shape.

In addition, Table 8 indicates that the Sérsic profile for the whole sample gives a fit worst than in the case of power-law and de Vaucouleurs functions. This it seems to be related to a slight overdensity of objects around $r_{\text {eq }} \sim 0.66 \operatorname{arcmin}(2.7 \mathrm{kpc})$ that make a single Sérsic law not suitable for describing that profile. Interesting, this position coincides with the galactocentric radius where the highest concentration of red and intermediate GC candidates is found (see Fig. 14).

### 4.6 Luminosity function and total number of GCs

In order to determine the total GC population in NGC 4546 and also to estimate a new value of the distance to the galaxy, we obtained the luminosity function of the globular clusters (GCLF). To do this, we select the unresolved objects in our initial photometric catalogue by performing the same colour cuts mentioned in Section 4.1, but without restricting the magnitudes in the $g^{\prime}$ band. We counted objects in bins of 0.35 mag in the range $17<g_{0}^{\prime}<27 \mathrm{mag}$, correcting by completeness and contamination using the analysis carried out in Sections 2.4 and 2.5, respectively.

Fig. 18 (upper panel) shows the raw luminosity distribution (grey line and scratched histogram), and the completeness and


Figure 17. Density profiles corrected by contamination and areal completeness for the total GC sample (black filled circles in left-hand panel) and for each GC subpopulations in NGC 4546 (right-hand panel). Blue circles, green squares, magenta triangles, and orange crosses in right-hand panel indicate the blue, intermediate, red, and reddest GC subpopulations (groups B, C, D, and E), respectively. These profiles were shifted along the $y$-axis to avoid overlapping. The dashed black line indicates the fit obtained using the Sérsic function. The solid orange line indicates the galaxy starlight profile (colour figure in the online version).

Table 7. Slope (b) and zero-point (a) values obtained in the fit of the density profiles considering a power law and de Vaucouleurs functions. The last column indicates the values of reduced chi-square.

| Population | Scal. law | Slope $(b)$ | Zero point $(a)$ | $\chi_{v}^{2}$ |
| :--- | :---: | :---: | ---: | :---: |
| All | Power | $-2.48 \pm 0.13$ | $2.11 \pm 0.25$ | 1.3 |
|  | de Vauc. | $-1.41 \pm 0.08$ | $1.65 \pm 0.25$ | 1.5 |
| Blue (B) | Power | $-1.76 \pm 0.21$ | $0.27 \pm 0.41$ | 1.6 |
|  | de Vauc. | $-0.94 \pm 0.12$ | $-0.21 \pm 0.39$ | 1.9 |
| Interm. (C) | Power | $-2.18 \pm 0.21$ | $0.79 \pm 0.41$ | 1.2 |
|  | de Vauc. | $-1.58 \pm 0.14$ | $1.32 \pm 0.42$ | 0.7 |
| Red (D) | Power | $-2.94 \pm 0.39$ | $2.45 \pm 0.66$ | 1.2 |
|  | de Vauc. | $-1.89 \pm 0.22$ | $2.52 \pm 0.59$ | 0.9 |
| $+\operatorname{Red}(E)$ | Power | $-1.87 \pm 0.26$ | $0.04 \pm 0.49$ | 0.6 |
|  | de Vauc. | $-1.09 \pm 0.14$ | $-0.21 \pm 0.42$ | 0.5 |

Table 8. Sérsic parameters obtained in the fit of the density profile for the whole GC sample, as well as for blue, intermediate, red and reddest GC subpopulations (groups B, C, D and E, respectively). The last column indicates the values of reduced chi-square.

| Population | $n$ | $R_{\text {eff }}(\operatorname{arcsec})$ | $\chi_{v}^{2}$ |
| :--- | :---: | :--- | :---: |
| All | $2.5 \pm 1.3$ | $46.7 \pm 9.5$ | 1.8 |
| Blue (B) | $1.2 \pm 0.7$ | $53.4 \pm 9.5$ | 0.8 |
| Interm. (C) | $1.6 \pm 0.8$ | $41.5 \pm 8.4$ | 0.5 |
| Red (D) | $0.6 \pm 0.2$ | $38.3 \pm 2.9$ | 0.6 |
| +Red (E) | 1.0 | $52.4 \pm 13.1$ | 0.6 |

background corrected histogram (black line and white histogram) for the GC candidates of NGC 4546. In order to model the GCLF and obtain the position of the turnover (TO), we fit the Gaussian and t 5 functions down to the 80 per cent completeness limit ( $g_{0}^{\prime}=25.2$ mag ). As seen in the figure, from this value an increase in the count of objects is observed, possibly as a consequence of an imperfect correction of the completeness and/or contamination of the sample. The values obtained were $\mathrm{TO}_{G}=23.70 \pm 0.08, \sigma_{G}=0.92 \pm 0.07$ mag and $\mathrm{TO}_{t 5}=23.72 \pm 0.07, \sigma_{t 5}=0.88 \pm 0.07 \mathrm{mag}$ for the Gaussian and t5 function, respectively. These values are reasonably robust thanks to the depth of our photometric sample.


Figure 18. Upper panel: raw histogram (shaded histogram), and background and completeness corrected histogram (black solid line) for the brightness distribution of the GC system of NGC 4546 . Vertical dotted lines indicate the magnitude region used for the fit of the Gaussian (black dashed line) and t5 (black solid line) functions. Bottom panel: corrected GCLFs for the blue, intermediate, and red GC subpopulations (groups B, C, and D). Vertical dotted and solid lines indicate the magnitude limit used for the fits, and the TO positions, respectively.

In this work, we adopted the average values of TO and $\sigma$ of those values mentioned above, obtaining $\langle\mathrm{TO}\rangle=23.71 \pm 0.1$ and $\langle\sigma\rangle=$ $0.9 \pm 0.09 \mathrm{mag}$ for the GCLF of NGC 4546. Assuming a universal value of TO of $M_{V}=-7.4 \mathrm{mag}$ (Jordán et al. 2007) and using the equation 2 of Faifer et al. (2011) to transform $M_{V}$ to $M_{g}$, we obtained the distance modulus of $(m-M)=30.75 \pm 0.12 \mathrm{mag}$ $(d=14.1 \pm 1.0 \mathrm{Mpc})$. This value is in excellent agreement with that previously obtained by Tully et al. (2013) $((m-M)=30.73 \pm 0.14$ mag) using surface brightness fluctuation method.

Based on the information obtained from the surface density profile of the whole GC sample and from the GCLF analysis, we estimate the total GC population and the specific frequency $\left(S_{N}\right)$ of NGC 4546. For this, we follow the same procedure as in Escudero et al. (2015) and Escudero et al. (2018). We integrated the density profile from 0.26 arcmin up to the galactocentric radius of 12.3 arcmin, equivalent to 50 kpc . The inner radius was chosen due to incompleteness in our data towards the galactic centre. On the other hand, the value adopted for the outermost radius is appropriate to include most of the GCs associated with an intermediate-mass galaxy (Faifer et al. 2011; Norris \& Kannappan 2011). For the region $R_{\text {gal }}<0.26$ arcmin, we considered the constant value of 93 GC arcmin ${ }^{-2}$ for the density, which is associated with the second bin in the density profile. This gives us 370 GCs. According to the GCLF parameters used in this work, this value represents 95 per cent of the whole GC sample (GCs brighter than $g_{0}^{\prime}=25.2 \mathrm{mag}$ ). Then, the total population of NGC 4546 is $N_{\text {tot }}=390 \pm 60$ GCs. The error associated with the total number of clusters is mainly due to the uncertainty in the parameters obtained in the analysis of the radial distribution and the luminosity function.

Using $N_{\mathrm{tot}}$, we obtained the $S_{N}$ of the system defined as the total number of GCs per unit host galaxy luminosity. This parameter allows comparisons between GC systems with different star formation histories and, therefore, different mass-luminosity ratios in their stellar populations. The expression initially introduced by Harris \& van den Bergh (1981) is defined as
$S_{N}=N_{\mathrm{tot}} 10^{0.4\left(M_{V}+15\right)}$,
where $M_{V}$ is the absolute magnitude of the galaxy in the $V$ band. Using the previously obtained distance modulus and the total $V$ magnitude $V=10.57 \pm 0.01$ of the Carnegie-Irvine Galaxy Survey (Ho et al. 2011), the absolute magnitude of NGC4546 is $M_{V}=$ $-20.18 \pm 0.12$. Then, we obtained a specific frequency of $S_{N}=$ $3.3 \pm 0.7$. This is a high value when compared to the mean value $S_{N}=1.6 \pm 1.4$ obtained for GC systems associated with S0 galaxies from the Harris, Harris \& Alessi (2013) catalogue.

In order to investigate if the intermediate GC candidates have any influence in the $S_{N}$ value, we obtained the GCLF of the blue, intermediate, and red GC subpopulations (groups B, C, and D; see Section 4.2). Due to the low number of candidates in each of these groups, we considered bins of 0.5 mag to construct the GCLFs. Fig. 18 (bottom panel) and Table 9 show the corrected GCLFs and the parameter values obtained from the fitted functions, respectively.

From this analysis, we estimate the total number of GCs in these three GC subpopulations, obtaining $146 \pm 25$ clusters for the blue (group B), $64 \pm 10$ members for the intermediate (group C), and $115 \pm 20$ for the red ones (group D). Considering only the values corresponding to the blue and red GC subpopulations, we calculate again the $S_{N}$ for NGC 4546, obtaining in this case, $S_{N}=2.2 \pm 0.5$. This value is more consistent with the mean value obtained for this type of galaxies. However, even if we consider these three subsamples, the red fraction of GC candidates in NGC 4546 results

Table 9. TO and $\sigma$ values obtained from the fits of the Gaussian and t 5 functions for the GCLFs of blue, intermediate, and red GC subpopulations (groups B, C, and D).

| Subpopulation | Function | TO | $\sigma$ |
| :--- | :---: | :---: | :---: |
| Blue | Gauss. | $23.70 \pm 0.15$ | $0.91 \pm 0.17$ |
|  | t5 | $23.71 \pm 0.16$ | $0.93 \pm 0.19$ |
| Intermediate | Gauss. | $23.50 \pm 0.11$ | $0.99 \pm 0.12$ |
|  | t5 | $23.50 \pm 0.12$ | $1.00 \pm 0.15$ |
| Red | Gauss. | $23.63 \pm 0.18$ | $0.99 \pm 0.19$ |
|  | t5 | $23.62 \pm 0.18$ | $1.00 \pm 0.20$ |

to be $f_{r}=0.35 \pm 0.10$. This value is similar to those presented for galaxies with similar total stellar masses by Salinas et al. (2015).

It is worth to mention that as the $S_{N}$ parameter depends on $M_{V}$, which in turn depends strongly on age, their values can be affected by age differences among stellar populations in galaxies. Therefore, we consider two quantities that are not affected by such differences, the $T_{N}$ parameter (Zepf \& Ashman 1993), and the specific mass $S_{M}$ (Georgiev et al. 2010). $T_{N}$ is the number of GCs normalized to the stellar mass in units of $1 \times 10^{9} \mathrm{M}_{\odot}$, while $S_{M}$ is the total mass of the GC system relative to the total baryon mass of the host galaxy defined as the sum of the stellar mass and the H I gas mass. For the latter, we follow the guidelines of Harris et al. (2017) to estimate the total mass of the GC system. Then, considering the value of stellar mass of NGC 4546 from Table 1 and the H I gas mass of Bettoni et al. (1991), high values were obtained for both quantities, $T_{N}=14.4$ and $S_{M}=0.28$ (see e.g. fig. 6 of Georgiev et al. 2010). In the same way, in order to compare some of these results with values in the literature, we obtain $T_{N}$ for blue and red GC subpopulations: $T_{\text {blue }}=5.4$ and $T_{\text {red }}=4.3$, respectively. These values compared with those obtained for the sample of galaxies belonging to low-density environments presented by Salinas et al. (2015) show that NGC 4546 has a relatively rich GC system for its mass, comparable to those of early-type galaxies in clusters.

## 5 SUMMARY AND CONCLUSIONS

In this work, we present the analysis of the global properties of the GC system associated with the S0 galaxy NGC 4546, using Gemini/GMOS data of three fields in the $g^{\prime} r^{\prime} i^{\prime} z^{\prime}$ filters. A summary of the main photometric results is presented below.

The analysis of the surface brightness distribution of the galaxy reveals considerable variations in its isophotal parameters towards the inner region ( $r_{\mathrm{eq}}<0.2 \mathrm{arcmin} ; 0.8 \mathrm{kpc}$ ), mainly in its PA and ellipticity. A 2D image decomposition using GALFIT software indicates that the galaxy is well fit with four components (bulge+lenses/discs+halo). The residual image obtained from subtracting this model in our GMOS images does not reveal the presence of a possible bar structure or spiral pattern as mentioned by Bettoni et al. (1991). In addition, extensive irregular regions of dust extending about 6 kpc along the semimajor axis of the galaxy are observed. These structures, together with the presence of a disc of gas rotating in the opposite direction to the stellar component of the galaxy, provide evidence of a merger/interaction event in the recent past with an object of lower mass than NGC 4546 (Eliche-Moral et al. 2018). In this context, the presence of the young NGC 4546UCD1 with an age of $\sim 4$ Gyr and with a rotation direction similar to the gas distribution would be related to the aforementioned interaction event. However, a possible previous interaction with the
small companion S0 galaxy (CGCG 014-074) located at a projected distance of $\sim 22 \mathrm{kpc}$ cannot be ruled out either.

Regarding the study of the GC system of NGC 4546, we measured the photometry of 350 GC candidates obtaining the integrated colour distributions $\left(g^{\prime}-i^{\prime}\right)_{0}$ and $\left(g^{\prime}-z^{\prime}\right)_{0}$, their density profiles, and azimuthal distributions. We estimated the distance modulus of the galaxy through its GCLF, resulting in $(m-M)=30.75 \pm 0.12$ mag. In addition, assuming a maximum length of 50 kpc for the GC system of NGC 4546, we obtained a total population of $N_{\text {tot }}=$ $390 \pm 60$ GCs. This total number of GC candidates is significantly higher than the previously estimated value of Zaritsky et al. (2015), and it corresponds to a relatively high specific frequency for this type of galaxies of $S_{N}=3.3 \pm 0.7$. While this is not as extreme as the value of $S_{N}=10$ obtained for NGC 6861 (Escudero et al. 2015), another low-density environment lenticular galaxy, a comparison with the sample compiled in Salinas et al. (2015) shows that NGC 4546 and NGC 6861 support the view that galaxies in such environment can have $S_{N}$ values in a similar range to that of cluster early-type galaxies.
We studied the $\left(g^{\prime}-i^{\prime}\right)_{0}$ and $\left(g^{\prime}-z^{\prime}\right)_{0}$ GCs colour distribution throughout the fit of Gaussian functions to the histograms. Our analysis shows that the bimodal case results in a GC system strongly dominated by the red subpopulation. An interpretation of this observation could be that NGC 4546 has a relatively quiescent merger history. This is because it is thought that many, if not most, metal-poor GCs are gained from satellite accretion (see e.g. Forbes \& Bridges 2010; Choksi et al. 2018). This scenario is supported by the case of NGC 1277, a galaxy that is strongly suspected of having undergone very few mergers because it completely lacks blue GCs (a so-called red nugget galaxy; Beasley et al. 2018). However, NGC 4546 is an intermediate luminosity galaxy displaying a relatively high $S_{N}$ (and $T_{\text {blue }}$ ) in a low-density environment. In this context, that interpretation may not be suitable as it would mean that with a normal history of mergers, NGC 4546 would have had an even higher $S_{N}$.
Therefore, we carried out a statistical analysis of our GCs sample in the colour-colour plane that showed different components, indicating at least three or more distinct GC groups. The classic blue and red subpopulations are observed, a group with intermediate colours to those mentioned above, and two groups located towards the blue and red ends of the colour distributions. However, a follow-up spectroscopic study will be necessary to confirm whether these groups are distinct in their stellar populations or dynamics. In this work, as seen in other early-type galaxies, the blue GC subpopulation presents a flatter spatial distribution than the red one, which has a high-concentration degree towards the galaxy centre. Noticeably about 72 per cent of the red candidates in our sample are located within 6 kpc of galactocentric radius and a fit of a Sérsic law gave an index $n<1$. This is clearly reflected in the density profile obtained for the whole sample where a slight overdensity is seen at $R_{\text {gal }} \sim 1$ arcmin. In the case of the intermediate GC subpopulation, its density profile presents a slope value between those obtained for the blue and red group, which indicates features shared with them. In this context, the analysis of the azimuthal distribution shows that intermediate and red GC candidates have similar values in their ellipticities with respect to the stellar light distribution of NGC 4546, while blue candidates do not show a significative ellipticity. These results would indicate a possible common origin between the red GCs and the stellar component of the galaxy (Forte et al. 2014), and possibly also that of the intermediate GCs if they were a different group. However, the value of the PA obtained for the red subpopulation differs significantly from the values obtained for
the other group of candidates and for the stellar light of the galaxy. This misalignment could be another indication of the violent past of this galaxy.

On the other hand, the different features shown by the blue GC subpopulation would indicate that this group would be a mixture between clusters originating in situ as well as accreted clusters from low-mass dwarf galaxies during the mass assembly phase of the galaxy. As NGC 4546 is a low-mass object in a very low-density environment, it might be expected that it shows evidence of a deficit of blue GCs due to a low accretion efficiency. However, this is not the case and therefore it would seem to indicate that the blue part of this GC system was assembled in a similar way to other galaxies.

Regarding the bluest GC objects, they do not show a particular characteristic or concentration around the galaxy. The presence of these objects with very blue colours distributed over our GMOS mosaic, possibly indicates that this group is composed of some bona fide GCs but mainly by MW stars. Only spectroscopic follow-up can confirm this.
On the other hand, the group of GC candidates with redder colours show a detectable spatial concentration towards NGC 4546. In this sense, it cannot be ruled out that these objects are an extension of the classic red GCs, but follow-up spectroscopy is required to definitely prove whether this is the case. However, it is noteworthy that most of these redder objects have similar behaviour in colour planes involving $g^{\prime}, r^{\prime}, i^{\prime}$, and $z^{\prime}$ bands as some GC candidates studied by Powalka et al. (2016). These authors, using different colour-colour diagrams in the $u g r i z K_{s}$ filters, found a few tens of GCs in the Virgo cluster core region (some confirmed with radial velocity), which show different behaviour to the bulk of their GC sample when $g^{\prime}, r^{\prime}, i^{\prime}$, and $z^{\prime}$ bands are used. Some of these objects are clearly located on the MW stellar sequence in the $\left(r^{\prime}-z^{\prime}\right)$ versus $\left(g^{\prime}-r^{\prime}\right)$ colour-colour diagram. Interesting, the authors also found that the MW GCs share the same locus in this kind of colour plane. While these objects are uniformly spread over the cluster region, it is important to note that some of them are grouped primarily around the lenticular galaxy M86 and the peculiar spiral galaxy NGC 4438. As mentioned by Powalka et al. (2016), it is then plausible that these GCs are born in an environment less dense than the Virgo core, which could be what we observed in NGC 4546. However, it is still necessary to consider different options that could explain the very red colours of these objects in NGC 4546. Some options that would explain this could be due to a reddening effect by dust in the galaxy, or objects belonging to an old GC subpopulation with higher metallicity, and/or objects associated with star clusters called faint fuzzies (FF; Larsen \& Brodie 2000; Forbes et al. 2014). When comparing the location of these objects around NGC 4546 (see bottom panel in Fig. 12) and the dust substructures (see Section 3.1), it can be seen that only a few of them are found near these regions. Therefore, this effect would not be the main cause of the presence of group E. Regarding the FF, these objects are generally associated with the disks of S 0 galaxies located in low-density environments (Liu et al. 2016), showing large sizes (effective radii of $7-15 \mathrm{pc}$ ), low luminosity $\left(M_{V}>-7\right)$, usually with red colours, and also with high metallicities and old ages. Some of the features shown by the objects belonging to group E in NGC 4546 (detectable spatial concentration; low brightness $g_{0}^{\prime}>23 \mathrm{mag}$ or $M_{V}>-7.5$; very red colours) seem to agree with those of the FF. Unfortunately, due to the lack of spectroscopic data of these objects and the impossibility of measuring their radii with our ground-based imaging due to the distance to NGC4546, it is not possible to determine their metallicities and/or their sizes in our GMOS images to confirm its nature.

Returning to intermediate GC candidates, the analysis of their GCLF showed that the TO value obtained for this subpopulation is marginally brighter than the values corresponding to blue and red GC subpopulations. This feature could indicate younger objects and/or with different metallicities in comparison to the aforementioned subpopulations. However, since these GC candidates do not constitute a dominant and significantly bright population in the colour-magnitude diagram, as seen in other recent galaxy mergers (e.g. GCs of $\sim 2$ Gyr in NGC 1316; Sesto et al. 2016), they would not be objects very young nor massive. In contrast, it is necessary to mention that the galaxy does not seem to show evidence of a recent star formation. Kuntschner et al. (2010) conducted a spectroscopic study of the stellar component of NGC 4546 using the integral-field spectrograph SAURON. These authors found an age of $11.7_{-1.0}^{+1.1} \mathrm{Gyr}$ for the galaxy, using the information obtained by the Lick indices up to $R_{\text {eff. }}$. Also, McDermid et al. (2015) used the same data as these authors but with the full spectral fitting technique, obtaining a mass-weighted age of $13.61 \pm 0.68 \mathrm{Gyr}$. In this sense, the presence of these intermediate GC candidates would suggest that they would not have been formed in a recent star formation event ( $<3 \mathrm{Gyr}$ ), given a contribution of young field stars would be expected during that process (Forte et al. 2014).

If this intermediate colour GC group is really different from the classic subpopulations, a possible scenario about its origin could involve the young NGC 4546-UCD1 mentioned above. Norris et al. (2015) assume that this object is the final result of tidal interaction between NGC 4546 and a dwarf galaxy of mass $\sim 3 \times 10^{9} \mathrm{M}_{\odot}$. NGC 4546-UCD1, with a metallicity $[\mathrm{Z} / \mathrm{H}]=0.18$ dex and an extended star formation history from early epochs has previously interacted with the galaxy in the last Gyrs, beginning its current state between 1-3 Gyr ago. These previous encounters ( $>3 \mathrm{Gyr}$ ) may have formed new GCs with a different metallicity compared with the typical blue and red ones, which we observed in our analysis. In this context, if we assume that the intermediate GC subpopulation could have originated as a result of this interaction, using single stellar population photometric models, their colour peak at ( $g^{\prime}-$ $\left.z^{\prime}\right)_{0} \sim 1.15 \mathrm{mag}$ would indicate a mean age and metallicity of $\sim 5 \mathrm{Gyr}$ and $[\mathrm{Z} / \mathrm{H}] \sim-0.3$ dex, respectively.

Regarding the origin of lenticular galaxies in low-density environments, Bekki \& Couch (2011) have shown that encounters, interactions, and unequal mergers of gas-rich discs in group environments could transform late-type galaxies in lenticulars. According to their simulation, it is expected that new stars form during the process of transformation. Therefore, the possible detection of intermediate colour GCs in this galaxy could be the most obvious indication of a strong transformation process that happened some Gyr ago, and highlight the potentiality of GC studies to trace the violent past of their host galaxies. In order to confirm it a spectroscopic study of the GCs subpopulation and a more detailed analysis of the stellar population of field stars looking for younger stellar components in NGC 4546 is necessary.

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