σ meson exchange effect on non-mesonic hypernuclear weak decay observables

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We analyze the influence of σ meson exchange on the main non-mesonic hypernuclear weak decay observables: Total rate Γ_{NM} , neutron-to-proton branching ratio $\Gamma_{n/p}$, and proton asymmetry parameter a_{Λ} . The σ meson exchange is added to the standard strangeness-changing weak $\Lambda N \rightarrow NN$ transition potential, which includes the exchange of the complete pseudoscalar and vector mesons octet ($\pi, \eta, K, \rho, \omega, K^*$). Using a shell model formalism, the σ meson weak coupling constants are adjusted to reproduce the recent Γ_{NM} and $\Gamma_{n/p}$ experimental data for ${}^5_{\Lambda}\text{He}$. Numerical results for the remaining observables of ${}^5_{\Lambda}\text{He}$ and all the observables of ${}^{12}_{\Lambda}\text{C}$ decays are presented. They clearly show that the addition of the σ meson improves the agreement with the data. However, its effect is not enough to reproduce well the a_{Λ} values, which means that other improvements of the model must be explored to explain the puzzle posed by the experiments.

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The free decay of a Λ hyperon occurs almost exclusively through the mesonic mode, $\Lambda \rightarrow \pi N$, emerging the nucleon with a momentum of about 100 MeV/c. Inside the nuclear medium ($p_F \sim 270$ MeV/c), this mode is Pauli blocked; and for all but the lightest Λ hypernuclei ($A \geq 5$), the weak decay is dominated by the non-mesonic channel, $\Lambda N \rightarrow NN$, with enough kinetic energy to put the two emitted nucleons above the Fermi surface. The non-mesonic hypernuclear weak decay (NMHWD) offers us a very unique opportunity to investigate the strangeness-changing weak interaction between hadrons. Assuming that the NMHWD is saturated by the $\Lambda N \rightarrow NN$ mode, the transitions receive contributions either from neutrons ($\Lambda n \rightarrow nn$) and protons ($\Lambda p \rightarrow np$), with rates Γ_n and Γ_p , respectively ($\Gamma_{\text{NM}} = \Gamma_n + \Gamma_p$, $\Gamma_{n/p} = \Gamma_n/\Gamma_p$). Over the last three decades, a huge amount of theoretical and experimental effort has been invested in solving an interesting puzzle: The theoretical models cannot reproduce simultaneously the experimental values of $\Gamma_{n/p}$ and a_{Λ} .

From the experimental side, there is actually an intense activity, as can be seen in the light of the experiments under way and/or planned at (KEK) [1], (FINUDA) [2], and Brookhaven National Laboratory (BNL) [3]. The preliminary results give a $\Gamma_{n/p}$ ratio value very close to 0.5 [4–6], and the measurements of a_{Λ} favor a negative value for ${}^{12}_{\Lambda}\text{C}$ and a positive value for ${}^5_{\Lambda}\text{He}$ [5–9]. On the other hand, from the pioneering work of Block and Dalitz [10] there have been many theoretical attempts dedicated to solving the puzzle. The earliest studies were based on the simplest model of the virtual pion exchange [11]. This model naturally explains the long-range part of the two-body interaction, and it reproduces reasonably well the total decay rate but fails badly in reproducing the other observables. In order to achieve a better description, some improvements have been introduced: (i) models that include the exchange of different combinations of other heavier mesons, such as η, K, ρ, ω - and K^* [12–19] to reproduce the short-range part of the interaction; (ii) analysis of the two-nucleon ($2N$) stimulated process $\Lambda NN \rightarrow NNN$ [20,21]; (iii) inclusion of interaction

terms that violate the isospin $\Delta T = 1/2$ rule [22–24]; (iv) description of the short-range baryon-baryon interaction in terms of quark degrees of freedom [25,26]; and (v) correlated (in the form of σ and ρ mesons) and uncorrelated two-pion exchanges [27–30]. We emphasize that none of these models gives a fully satisfactory description of all the NMHWD observables simultaneously, even though a consistent (though not sufficient) increase of $\Gamma_{n/p}$ has been found. So far, only Jun [24] has been able to reproduce well the Γ_{NM} and $\Gamma_{n/p}$ (but not a_{Λ}) data by employing, in addition to the one-pion exchange, an entirely phenomenological four-baryon point interaction for the short-range part, including the $\Delta T = 3/2$ contribution, and fixing the model coupling constants. Concerning the proton asymmetry parameter a_{Λ} , all existing calculations based on strict one-meson exchange models [14–16,18,19,26,31,32] find values between -0.73 and -0.19 for ${}^5_{\Lambda}\text{He}$ [33,34] and when results are available in the same model, very similar values for ${}^{12}_{\Lambda}\text{C}$. The final state interactions effect, although it attenuates the a_{Λ} value, does not reverse the sign of the parameter [34]. Only two recent theoretical calculations show some agreement with the experimental data: (i) a first application of effective field theory (EFT) to non-mesonic decay [35] and (ii) a very recent extension of the direct-quark interaction model, which strongly violates the $\Delta T = 1/2$ rule, to include σ meson exchange [30]. However, in both cases, a nuclear matter formalism (which does not include the full contribution of transitions coming from nucleon states beyond the s shell) is used and could give, therefore, a limited description for p -shell hypernuclei or, even worse, for heavier ones.

The EFT approach from Ref. [35] suggests that in order to reproduce the NMHWD data, the microscopic models should be supplemented by isospin and spin-independent central interactions. Motivated by this fact and to set a more detailed description than obtained from previous nuclear matter calculations [30], we analyze the influence of the scalar-isoscalar σ meson exchange over the NMHWD. We will work within the shell model (SM) formalism developed in Refs. [17–19], which explicitly includes the contribution of transitions originated from states beyond the s shell. The σ meson will be added to the standard strangeness-changing weak $\Lambda N \rightarrow NN$ transition potential already including the exchange of

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TABLE I. PC and PV constants for neutron and proton NMHWD rates of ${}^5\text{He}$ obtained with $\Lambda_\sigma = 1.2$ GeV [30]. Parenthetically we give the results with $\Lambda_\sigma = 1.5$ GeV.

μ_σ (MeV)	550	750
a_n^{PC}	0.0096 (0.0126)	0.0010 (0.0018)
b_n^{PC}	1.0806 (0.9459)	3.4141 (2.4946)
c_n^{PC}	0.0000 (0.0000)	0.0000 (0.0000)
a_n^{PV}	0.0022 (0.0031)	0.0003 (0.0005)
b_n^{PV}	7.3380 (6.1721)	21.0396 (14.6053)
c_n^{PV}	0.0508 (0.0510)	0.0509 (0.0509)
a_p^{PC}	0.0192 (0.0251)	0.0019 (0.0036)
b_p^{PC}	1.3623 (1.1915)	4.2979 (3.1322)
c_p^{PC}	0.1422 (0.1421)	0.1421 (0.1422)
a_p^{PV}	0.0014 (0.0020)	0.0002 (0.0004)
b_p^{PV}	12.4826 (10.5148)	35.8000 (24.8719)
c_p^{PV}	0.1398 (0.1398)	0.1399 (0.1397)

the complete pseudoscalar and vector mesons octet (π , η , K , ρ , ω , K^*). This model will be referenced as OCT+S, to differentiate it from our previous $\pi + \eta + K + \rho + \omega + K^*$ model, designated as OCT.

For the pseudoscalar and vector mesons octet, the weak (W) and a strong (S) vertices in the $\Lambda N \rightarrow NN$ decay will be described by means of the same interaction Hamiltonians given in Ref. [15] and adopted in Refs. [17–19]. This leads to the OCT exchange potential

$$V^{\text{OCT}}(\mathbf{r}) = \sum_{i=\pi, \eta, K, \rho, \omega, K^*} \bar{V}_i^{(0)}(\mathbf{r}), \quad (1)$$

with $\bar{V}_i^{(0)}(\mathbf{r})$ defined in Ref. [18]. In this equation, we neglected all kinematic and first-order nonlocality corrections because, as extensively discussed in Ref. [18], although their effects can be very important for particular transitions, they do not affect the main decay observables very much. For the σ meson, we assume weak and strong coupling Hamiltonians of the form [Ref. [30], Eq. (17)]

$$\begin{aligned} \mathcal{H}_{\Lambda N \sigma}^W &= G_F \mu_\pi^2 \bar{\psi}_N (A_\sigma + B_\sigma \gamma_5) \phi_\sigma \begin{pmatrix} 0 \\ 1 \end{pmatrix} \psi_\Lambda, \\ \mathcal{H}_{\Lambda N \sigma}^S &= g_{NN\sigma} \bar{\psi}_N \phi_\sigma \psi_N, \end{aligned} \quad (2)$$

where ψ_N and ψ_Λ are the baryon fields, ϕ_σ is the meson field, and A_σ and B_σ are the weak parity-conserving (PC) and parity-violating (PV) coupling constants, respectively, which will be considered as adjustable parameters of the model. For the strong coupling constant, we will assume the value $g_{NN\sigma} \simeq g_{NN\pi} = 13.3$. The resulting nonrelativistic one σ exchange potential is

$$\bar{V}_\sigma^{(0)}(\mathbf{r}) = G_F \mu_\pi^2 g_{NN\sigma} \left[A_\sigma f_C(r, \mu_\sigma) - i \frac{B_\sigma}{2\bar{M}} f_V(r, \mu_\sigma) \cdot \boldsymbol{\sigma}_1 \cdot \hat{\mathbf{r}} \right],$$

where μ_σ is the σ meson mass, $\bar{M} = (M_\Lambda + M)/2$ with M and M_Λ being the nucleon and Λ masses, respectively, and all the remaining notation has the same meaning as in Ref. [18]. Thus, we have

$$V^{\text{OCT}+S}(\mathbf{r}) = V^{\text{OCT}}(\mathbf{r}) + \bar{V}_\sigma^{(0)}(\mathbf{r}). \quad (3)$$

Using the SM formalism developed in Refs. [17,18], we evaluate the transition rates by means of Fermi's golden rule: $\Gamma_i = 4\pi \sum_{M_I} \sigma(J_I M_I; -1/2, m_{t_i})$ ($i = n, p, m_{t_n} = -1/2, m_{t_p} = 1/2$), where

$$\begin{aligned} \sigma(J_I M_I; m_{t_1}, m_{t_2}) &= \int d\Omega_{p_1} \int dF \sum_{s_1 s_2 J_F M_F} |\langle \mathbf{p}_1 s_1 t_1 \mathbf{p}_2 \\ &\quad \times s_2 t_2 J_F M_F | V | J_I M_I \rangle|^2, \end{aligned} \quad (4)$$

with $\int dF \dots = 2\pi \int \frac{p_1^2 dp_1}{(2\pi)^3} \frac{p_2^2 dp_2}{(2\pi)^3} \delta(E.C.) \dots$. The initial and final nuclear states are described in the extreme p - h model as excitations over the core, i.e. $|J_I\rangle \rightarrow |j_\Lambda\rangle$ and $|J_F\rangle \rightarrow |j_b^{-1}\rangle$ for ${}^5\text{He}$ and $|J_I\rangle \rightarrow |j_\Lambda j_a^{-1}; J_I\rangle$ and $|J_F\rangle \rightarrow |j_a^{-1} j_b^{-1}; J_F\rangle$ for ${}^{12}\text{C}$. The finite nucleon size (FNS) effects are phenomenologically implemented by a monopole form factor $(\Lambda_M^2 - \mu_M^2)/(\Lambda_M^2 + q^2)$, with Λ_M the cutoff for the meson M [17]. The initial and final short-range correlations (SRC) are simulated, respectively, by means of the correlation functions [17,18]

$$\begin{aligned} g_{\Lambda N}(r) &= (1 - e^{-r^2/\alpha^2})^2 + \beta r^2 e^{-r^2/\gamma^2}, \\ g_{NN}(r) &= 1 - j_0(q_c r), \end{aligned} \quad (5)$$

with $\alpha = 0.5$ fm, $\beta = 0.25$ fm $^{-2}$, $\gamma = 1.28$ fm, and $q_c = 3.93$ fm $^{-1}$. The partial rates can be parametrized as

$$\Gamma_i = a_i^{\text{PC}} (A_\sigma - b_i^{\text{PC}})^2 + c_i^{\text{PC}} + a_i^{\text{PV}} (B_\sigma - b_i^{\text{PV}})^2 + c_i^{\text{PV}}, \quad (6)$$

TABLE II. Experimental data for the NMHWD of ${}^5\text{He}$ and ${}^{12}\text{C}$ (total width is in units of $\Gamma_0 = 2.50 \times 10^{-6}$ eV).

Observable	${}^5\text{He}$	${}^{12}\text{C}$
Γ_{NM}	0.424 ± 0.024 [6] 0.41 ± 0.14 [36]	0.940 ± 0.035 [6] 1.14 ± 0.2 [36]
$\Gamma_{n/p}$	0.39 ± 0.11 [4] $(0.45-0.51) \pm 0.15$ [5] $0.45 \pm 0.11 \pm 0.03$ [6] 0.93 ± 0.55 [36]	— $0.87 \pm 0.09 \pm 0.21$ [5] $0.56 \pm 0.12 \pm 0.04$ [6] $1.33^{+0.12}_{-0.81}$ [36]
a_Λ	$0.07 \pm 0.08^{+0.08}_{-0.00}$ [5] $0.11 \pm 0.08 \pm 0.04$ [6,7] 0.24 ± 0.22 [9]	$-0.24 \pm 0.26^{+0.08}_{-0.00}$ [5] $-0.20 \pm 0.26 \pm 0.04$ [6,7] —

TABLE III. Adjusted σ meson coupling constants.

μ_σ (MeV)		550	550	750	750
Λ_σ (GeV)		1.2	1.5	1.2	1.5
Sol I	A_σ	0.67	0.57	2.12	1.53
	B_σ	13.39	11.18	38.39	26.64
Sol II	A_σ	2.08	1.83	6.56	4.74
	B_σ	13.08	10.92	37.50	26.57

with coefficients a_i^X , b_i^X , and c_i^X containing the SM information. They are listed in Table I for ${}^5_\Lambda\text{He}$ and for different μ_σ values. We have observed from the numerical evaluation of the coefficients that they are roughly insensible to the particular correlation function used, but dependent on the Λ_σ value. We include in Table I the results for two different values of this cutoff.

Solving the equation system obtained by fixing $\Gamma_n + \Gamma_p$ and Γ_n/Γ_p to the ${}^5_\Lambda\text{He}$ experimental central values from Ref. [6] (shown in Table II), we obtain two sets of solutions for A_σ and B_σ , exhibited in Table III for two different values of μ_σ and Λ_σ .

We have found that if FNS and SRC are eliminated at all, there are no single solutions for A_σ and B_σ that make the theoretical results consistent with the central values of the experiments. This clearly shows the relevance of these two effects over the parameters. It is important to note that the experimental data have large error bars, and as a consequence, the parameters can vary within a finite region, as shown in Fig. 1 for a particular value of μ_σ and Λ_σ .

In the following, we evaluate a_Λ using the SM formalism recently developed in Ref. [19]:

$$a_\Lambda = \frac{12\pi f}{(J_I + 1)\Gamma_p} \sum_{M_I} M_I \sigma(J_I M_I; -1/2, 1/2),$$

($f = 1$ for ${}^5_\Lambda\text{He}$ and $f = -2$ for ${}^{12}_\Lambda\text{C}$), leading to

$$a_\Lambda = (k_1 A_\sigma B_\sigma + k_2 A_\sigma + k_3 B_\sigma + k_4) / \Gamma_p, \quad (7)$$

where the constants k_i (containing the SM information) will be given below for a particular value of μ_σ and Λ_σ . Numerical results obtained for ${}^5_\Lambda\text{He}$ with the central fixed values of the

FIG. 1. Allowed region for the σ meson coupling constants for $\mu_\sigma = 550$ MeV and $\Lambda_\sigma = 1.2$ GeV.

TABLE IV. Predicted hypernuclear weak decay observables for different sets of σ coupling constants, mass, and cutoff (Γ_{NM} is given in units of $\Gamma_0 = 2.50 \times 10^{-6}$ eV).

μ_σ	Λ_σ	A_σ	B_σ	${}^5_\Lambda\text{He}$	${}^{12}_\Lambda\text{C}$		
(MeV)	(GeV)			a_Λ	Γ_{NM}	$\Gamma_{n/p}$	a_Λ
—	—	0	0	−0.507	1.166	0.267	−0.508
550	1.2	0.67	13.39	−0.326	0.776	0.427	−0.322
550	1.2	2.08	13.08	−0.362	0.793	0.435	−0.348
550	1.5	0.57	11.18	−0.328	0.769	0.415	−0.326
750	1.2	2.12	38.39	−0.326	0.767	0.416	−0.324
750	1.2	6.56	37.50	−0.362	0.780	0.423	−0.342
750	1.5	1.53	26.64	−0.325	0.765	0.411	−0.325

weak coupling constants have been collected in Table IV, together with the predicted values of all the observables for the p -shell ${}^{12}_\Lambda\text{C}$ hypernucleus.

They clearly show that our results are not sensible to the particular μ_σ , Λ_σ , A_σ , and B_σ set selected, because in all cases our OCT+S model predicts the values $a_\Lambda({}^5_\Lambda\text{He}) \simeq -0.34$, $\Gamma_{\text{NM}}({}^{12}_\Lambda\text{C}) \simeq 0.78$, $\Gamma_{n/p}({}^{12}_\Lambda\text{C}) \simeq 0.43$ and $a_\Lambda({}^{12}_\Lambda\text{C}) \simeq -0.33$. This gives evidence of the fact that these variables are strongly correlated between them and shows the stability of our results (in spite of the fact that μ_σ and Λ_σ are unknown parameters of the theory) [37]. A straightforward comparison of OCT+S results with the OCT ones shows that the inclusion of the σ meson reduces the results for Γ_{NM} by $\sim 40\%$. In addition, the neutron-to-proton branching ratio $\Gamma_{n/p}$ is increased $\sim 36\%$. These last two effects occur because the σ meson strongly reduces the PV contribution of the proton-induced decay, as shown in Table V and as can be seen from Eq. (6) for $B_\sigma \simeq b_p^{\text{PV}}$. Furthermore, σ meson helps bring to near zero the asymmetry a_Λ , increasing it $\sim 35\%$.

To illustrate the A_σ and B_σ dependence of the NMHWD observables, we show in Fig. 2 our results for ${}^5_\Lambda\text{He}$. We see that within our OCT+S model, a bigger value for A_σ and a smaller for B_σ are necessary for reversing the asymmetry sign. This can be understood by noting that for $\mu_\sigma = 550$ MeV and $\Lambda_\sigma = 1.2$ GeV, we have $k_1 = -0.010$, $k_2 = 0.127$, $k_3 = 0.014$, and $k_4 = -0.275$. These A_σ and B_σ values overestimate the total rate Γ_{NM} and strongly underestimate the ratio $\Gamma_{n/p}$. From Figs. 1 and 2, we observe that the best value that can be reached for $a_\Lambda({}^5_\Lambda\text{He})$ within our model, consistent with the experimental data of partial rates, is obtained with $A_\sigma = 3.1$, $B_\sigma = 10.1$, leading to $a_\Lambda = -0.24$, which is not consistent with the experimental value. For the p -shell ${}^{12}_\Lambda\text{C}$ hypernucleus, we get a better agreement with data, which

TABLE V. Comparison of partial rate contributions within OCT and OCT+S models for $\mu_\sigma = 550$ MeV, $\Lambda_\sigma = 1.2$ GeV, $A_\sigma = 0.67$, and $B_\sigma = 13.39$ (in units of $\Gamma_0 = 2.50 \times 10^{-6}$ eV).

	Model	Γ_n^{PC}	Γ_n^{PV}	Γ_p^{PC}	Γ_p^{PV}
${}^5_\Lambda\text{He}$	OCT	0.011	0.167	0.178	0.364
	OCT+S	0.002	0.130	0.151	0.141
${}^{12}_\Lambda\text{C}$	OCT	0.024	0.222	0.296	0.624
	OCT+S	0.005	0.227	0.251	0.293

FIG. 2. A_σ and B_σ dependence of the ${}^5_\Lambda\text{He}$ decay observables, for $\mu_\sigma = 550$ MeV and $\Lambda_\sigma = 1.2$ GeV. Shaded region stands for experimental values [6] with error bars.

have large error bars. Thus, the OCT+S model implemented with the SM formalism shows that the inclusion of the σ meson is not enough to reproduce simultaneously all the data, especially the positive proton asymmetry value for ${}^5_\Lambda\text{He}$. At this point, it is important to note that we have not included here the contribution of the $2N$ induced decay to Γ_{NM} . We only qualitatively discuss the effect of this

process on our results, since there is not a SM formalism for $2N$ decay in the literature. We will adopt $\Gamma_{2N} \simeq 0.2(\Gamma_n + \Gamma_p)$, as calculated within nuclear matter inspired models [4,6,38]. This means that we must adjust A_σ and B_σ in $\Gamma_n + \Gamma_p$ to reproduce $(\Gamma_{\text{NM}})_{\text{exp}}/1.2 \sim 0.35$. (The data for $\Gamma_{n/p} = 0.45$ is not modified because it has been obtained by a coincidence method independent of the final state interactions and $2N$ mechanism [6].) Therefore, from Fig. 2 it is clear that no single values for parameters A_σ and B_σ could reproduce these values for $\Gamma_n + \Gamma_p$ and $\Gamma_{n/p}$. Nevertheless, as the σ inclusion has reduced the contribution of $\Gamma_n + \Gamma_p$ by $\sim 40\%$ from the old OCT model, and as the relation $\Gamma_{2N} = 0.2(\Gamma_n + \Gamma_p)$ is only valid for a nuclear matter calculation, a consistent evaluation of Γ_{2N} within the SM with the σ inclusion could produce a different $\Gamma_{2N}/(\Gamma_n + \Gamma_p)$ ratio; but our conclusion is not definitive.

Summarizing, we have analyzed the σ meson contribution to the NMHWD observables in the framework of a SM formalism [17–19], which carefully includes the effect of the p -shell state decays, both in the partial decay rates and in the asymmetry parameter evaluation. From our results, we conclude that even though the σ meson contributes to reducing the total decay width Γ_{NM} and increasing the neutron-to-proton branching ratio $\Gamma_{n/p}$, it is not enough to reproduce the more recent experimental data on the asymmetry. Nevertheless, it improves sensibly the values of a_Λ for the s -shell ${}^5_\Lambda\text{He}$; and for the p -shell ${}^{12}_\Lambda\text{C}$ hypernucleus, we have obtained a better agreement. Our results also corroborate the theoretical expectation that a_Λ should have only a moderate dependence on the particular hypernucleus considered, as can be seen from Table IV. We suggest three possible alternatives for future improvements of the model: (i) additional degrees of freedom should be added to our SM formalism to improve the description of the experimental data, for example, $\Delta I = 3/2$ contributions in the same footing of Ref. [30] (but now in a finite nucleus scheme) where a better agreement has been obtained for ${}^5_\Lambda\text{He}$; (ii) a different decay mechanism should be introduced for s - and p -shell hypernuclei, beyond the Born approximation; (iii) the $2N$ weak decay contribution should be included within a SM formalism. Finally, we have clearly shown that the effects of an isoscalar central spin-independent interaction included through the σ meson would not be enough to reproduce simultaneously all the NMHWD observables, without additional changes in the nuclear model and/or the decay mechanism.

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- [1] H. Outa *et al.*, KEK Report No. KEK-PS E462, 2000.
- [2] A. Feliciello, Nucl. Phys. **A691**, 170 (2001); P. Gionatti, *ibid.* **A691**, 483 (2001).
- [3] R. L. Gill, Nucl. Phys. **A691**, 180 (2001).
- [4] G. Garbarino, A. Parreño, and A. Ramos, Phys. Rev. C **69**, 054603 (2004); Nucl. Phys. **A754**, 137 (2005).

- [5] H. Bhang *et al.*, Nucl. Phys. **A754**, 144 (2005).
- [6] H. Outa *et al.*, Nucl. Phys. **A754**, 157 (2005).
- [7] T. Maruta *et al.*, Nucl. Phys. **A754**, 168 (2005).
- [8] S. Ajimura *et al.*, Phys. Lett. **B282**, 293 (1992).
- [9] S. Ajimura *et al.*, Phys. Rev. Lett. **84**, 4052 (2000).
- [10] M. M. Block and Dalitz, Phys. Rev. Lett. **11**, 96 (1963).

- [11] J. B. Adams, Phys. Rev. **156**, 1611 (1967) (Cf. correction pointed out in Ref. [12].)
- [12] B. H. J. McKellar and B. F. Gibson, Phys. Rev. C **30**, 322 (1984).
- [13] K. Takeuchi, H. Takaki, and H. Bandō, Prog. Theor. Phys. **73**, 841 (1985).
- [14] J. F. Dubach, G. B. Feldman, B. R. Holstein, and L. de la Torre, Ann. Phys. (NY) **249**, 146 (1996).
- [15] A. Parreño, A. Ramos, and C. Bennhold, Phys. Rev. C **56**, 339 (1997) and references therein.
- [16] A. Parreño and A. Ramos, Phys. Rev. C **65**, 015204 (2001).
- [17] C. Barbero, D. Horvat, F. Krmpotić, T. T. S. Kuo, Z. Naranić, and D. Tadić, Phys. Rev. C **66**, 055209 (2002).
- [18] C. Barbero, C. de Conti, A. P. Galeao, and F. Krmpotić, Nucl. Phys. **A726**, 267 (2003).
- [19] C. Barbero, A. P. Galeao, and F. Krmpotić, Phys. Rev. C **72**, 035210 (2005).
- [20] A. Ramos, E. Oset, and L. L. Salcedo, Phys. Rev. C **50**, 2314 (1994).
- [21] A. Ramos, M. J. Vicente-Vacas, and E. Oset, Phys. Rev. C **55**, 735 (1997); **66**, 039903(E) (2002).
- [22] A. Parreño, A. Ramos, C. Bennhold, and K. Maltman, Phys. Lett. **B435**, 1 (1998).
- [23] W. M. Alberico and G. Garbarino, Phys. Lett. **B486**, 362 (2000).
- [24] J.-H. Jun, Phys. Rev. C **63**, 044012 (2001).
- [25] T. Inoue, M. Oka, T. Motoba, and K. Itonaga, Nucl. Phys. **A633**, 312 (1998).
- [26] K. Sasaki, T. Inoue, and M. Oka, Nucl. Phys. **A669**, 331 (2000); **A678**, 455(E) (2000).
- [27] M. Shmatikov, Phys. Lett. **B322**, 311 (1994); Nucl. Phys. **A580**, 538 (1994).
- [28] K. Itonaga, T. Ueda, and T. Motoba, Nucl. Phys. **A577**, 301 (1994); **A585**, 331 (1995); **A639**, 329 (1998).
- [29] E. Jido, E. Oset, and J. A. Palomar, Nucl. Phys. **A694**, 525 (2001).
- [30] K. Sasaki, M. Izaki, and M. Oka, Phys. Rev. C **71**, 035502 (2005).
- [31] K. Itonaga, T. Ueda, and T. Motoba, Phys. Rev. C **65**, 034617 (2002); K. Itonaga, T. Motoba, and T. Ueda, in *Electrophoto Production of Strangeness on Nuand Nuclei* (Sendai03), edited by K. Maeda, H. Tamura, S. N. Nakamura, and O. Hashimoto (World Scientific, Singapore, 2004), p. 397.
- [32] K. Sasaki, T. Inoue, and M. Oka, Nucl. Phys. **A702**, 477 (2002).
- [33] W. M. Alberico and G. Garbarino, Phys. Rep. **369**, 1 (2002).
- [34] W. M. Alberico, G. Garbarino, A. Parreño, and A. Ramos, Phys. Rev. Lett. **94**, 082501 (2005).
- [35] A. Parreño, C. Bennhold, and B. R. Holstein, Phys. Rev. C **70**, 051601(R) (2004) .
- [36] J. J. Szymanski *et al.*, Phys. Rev. C **43**, 849 (1991).
- [37] G. López Castro and A. Mariano, Nucl. Phys. **A697**, 440 (2001).
- [38] W. M. Alberico, A. De Pace, G. Garbarino, and A. Ramos, Phys. Rev. C **61**, 044314 (2000).