Implementing a Typed Assembly Language and its Machine Model

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Abstract

We describe the implementation of a first-order linearly typed assembly language, HBAL, that allows the safe reuse of heap space for elements of different types. Linear typing ensures the single pointer property, disallowing aliasing, but allowing safe in-place-update compilation of a functional programming language. HBAL was designed as a target low-level language for Hofmann’s LFPL programs [5] that run in a bounded amount of heap space.

Keywords: Programming Languages, Type Systems, Compilers, Typed Assembly Languages, Resource Awareness.

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1 Introduction

When computing resources are limited, such as in embedded and real-time systems or for applications to be run across the Internet, resource awareness is crucial. The particular resource we are concerned with in this paper is heap space. We describe the implementation of HBAL, a first-order heap-bounded assembly language, whose type system allows for safe reuse of heap space for elements of different types. HBAL is suitable for resource-aware computing using proof-carrying code.

In C even a malloc-free program can use more memory than what was assigned to the program initially. For example, a pointer can access an arbitrary memory location beyond the intended scope of the program. Since type systems are a convenient and elegant way of expressing a semantic constraint such as resource boundedness, in order to provide end-to-end static guarantees of resource-boundedness, we use type-systems for both high-level and low-level languages. In this context, the compiler translates typed high-level code into typed low-level code, where the typing derivation of the low-level code is the proof in proof-carrying code.

In our implementation the HBAL language is used to capture in-place update compilation of a functional programming language with similar type systems, providing a static guarantee of bounded heap-space usage. We implemented a compiling function from Hofmann’s LFPL [3] into HBAL.

Typed assembly languages have been an active subject of study for several years. Contributions include TAL [7, 8], STAL [9], DTAL [12], and Alias Types [10, 11].

TAL began with higher-order functions and polymorphism, considering System F as a high-level language. But TAL assumed a particular compilation technique, continuation-passing style, which is not used by every compiler. STAL addressed this by modeling stacks with stack polymorphism. DTAL introduced the possibility for making some array bounds-checking optimizations, using dependent types. Alias Types allowed for areas of store to be reused in ways that TAL prohibited, tracking aliasing of locations to allow for safe memory management.

HBAL uses a deliberately restricted type system which reflects in the low-level the state-of-the-art of a type-system approach to dealing with resource bounds in a high-level language, following Hofmann’s work ([3, 4, 2, 5]).

HBAL uses linear typing to prevent aliasing, and includes pseudoinstructions for safely altering the types of heap locations. This means that we do not need to assume an external garbage collector, and we can provide a static guarantee that every program runs in a fixed amount of heap space. However, HBAL is not incompatible with garbage collection, and it can be extended to include malloc and free operations if desired. This could be done so that the memory-allocation initialization part of an application could be typed within the system.

This section and Section 2, where HBAL’s syntax and semantics are described, are extracted from [1]. The new contribution, i.e. the implementation of the compiler LFPL-to-HBAL and the machine model for HBAL, is
described in Section 3. In Section 4 we provide some examples of HBAL programs. Conclusions and some future work are depicted in Section 5.

2 The HBAL language

HBAL is a first-order linearly typed assembly language. In the HBAL type system a word type \((\sigma)\) is either an integer or a pointer to a structured type \(A\) (denoted as \([A]\)), where \(A\) can be code, the type of instructions, a flagged word type \((\sigma^z)\), a Cartesian product \((A \times A)\), a list \((L(A))\), a tree \((T(A))\), or a diamond \((\diamond)\). The flag \((z)\) can be 0 (uninitialized) or 1 (initialized).

The machine registers are called \(r_0 \ldots r_n\) and there are two dedicated registers for the program counter \(pc\) and stack pointer \(sp\). A context \(\Gamma\) is a finite mapping of registers \(r_i\) to word types \(\sigma\), treated as a set of type assignments \(r_i : \sigma\).

The initial context is denoted \(\{\}\), but it contains the type assignment \(r_0 : \text{int}\). This register is used to always store the constant number 0, making it unusable by the programmer.

When we write the extended context \(\Gamma, r_i : \sigma\), it is understood that \(r_i\) does not already appear in \(\Gamma\). We assume that the program counter, register \(pc\), never appears in any context. The context \(\Gamma \upharpoonright r_i\) is defined to be the same as \(\Gamma\) except undefined on \(r_i\).

\(\text{size}(A)\) is the size of the type \(A\) as it is laid out in memory and \(A[c]\) denotes the type of the \(c\)th word in the layout of \(A\) in memory.

When a pointer is read form memory into a register, the memory is made inaccessible by uninitializing the pointer type. This prevents aliases, preserving the single pointer property. So, \(A^{c=1}\) denotes \(A\) with the initialization flag set on the \(c\)th word, and \(A^{c=0}\) denotes \(A\) with the \(c\)th initialization flag cleared. \(A^{c=0}\) denotes the uninitialized of \(A\).

There exists a subtyping relation on types, given by the contextual, reflexive, and transitive closure of the uninitialization operation, so \(B(A) \leq B(A^{c=0})\).

A program \(P\) consists of a sequence of instructions \(p\) and labels \(l\).

\[
\begin{align*}
P & ::= \langle \rangle ~ | ~ p ~ ; ~ P ~ | ~ l ~ ; ~ P \\ p & ::= \text{load} ~ r \leftarrow r[c] ~ | ~ \text{store} ~ r[c] \leftarrow r \\
& | ~ \text{arithmetic} ~ r \leftarrow r \odot c ~ | ~ \text{arith} ~ r \leftarrow r \odot r \\
& | ~ \text{bnz} ~ r ~ l ~ | ~ \text{bez} ~ r ~ l ~ | ~ \text{jmp} ~ l \\
& | ~ \text{call} ~ l ~ | ~ \text{ret} ~ l \\
& | ~ \text{malloc} ~ A ~ | ~ \text{sfree} ~ c \\
& | ~ \text{use} ~ r ~ A ~ | ~ \text{discard} ~ c \\
& | ~ \text{fold-nil}_A ~ r[c] ~ | ~ \text{fold-cons}_A ~ r[c] \\
& | ~ \text{fold-leaf}_A ~ r[c] ~ | ~ \text{fold-node}_A ~ r[c] \\
& | ~ \text{case-lst}_A ~ r[c] ~ l ~ | ~ \text{case-tree}_A ~ r[c] ~ l \\
\od & ::= + ~ | ~ - ~ | ~ * ~ | ~ / 
\end{align*}
\]
HBAL has a small set of standard assembly instructions, together with
several pseudo-instructions. There are three kinds of pseudo-instructions;
they are either typechecking directives (use and discard) that will be erased
by the assembler, datatype constructors and destructors (fold-nil, fold-cons,
and caselist for lists, and fold-leaf, fold-node, and casetree for binary
trees), or hiding pointer arithmetic operations (malloc and free), because
it is not allowed to overwrite the stack pointer directly.

A program is a sequence of instructions and labels which defines a number
of mutually recursive first-order functions. The typing rules define a judgment:

$$\Gamma \vdash P$$

which means that $P$ is a well-typed assembly program in context $\Gamma$.

A program must be given together with a signature, $\Sigma$. The signature
assigns procedure types of the form $A_1, \ldots, A_n \rightarrow A$ for $n \geq 0$ to subroutine
labels and contexts to branch target labels.

**Typing rules**

The typing rules ensure the single pointer property that says that every loca-
tion can be reached from at most one live pointer in a register or on the heap.
As an example, we give the typing rules for load and store instructions.

\[
A[c] = \text{int}^1 \quad \Gamma, r_j : [A], r_i : \text{int} \vdash P \\
\Gamma, r_j : [A] \vdash \text{load} \quad r_i \leftarrow r_j[c] \quad P
\]

\[
A[c] = [B]^1 \quad r_i \neq sp \quad \Gamma, r_j : [A^{c=0}], r_i : [B] \vdash P \\
\Gamma, r_j : [A] \vdash \text{load} \quad r_i \leftarrow r_j[c] \quad P
\]

\[
A[c] = \text{int}^z \quad \Gamma, r_i : \text{int}, r_j : [A^{c=1}] \vdash P \\
\Gamma, r_i : \text{int}, r_j : [A] \vdash \text{store} \quad r_j[c] \leftarrow r_i \quad P
\]

\[
A[c] = [B]^z \quad r_i \neq sp \quad B \neq \text{code} \quad \Gamma, r_j : [A^{c=1}] \vdash P \\
\Gamma, r_i : [B], r_j : [A] \vdash \text{store} \quad r_j[c] \leftarrow r_i \quad P
\]

There are two rules for load and store because loading or copying a
pointer may violate the single pointer property, while loading or copying an
integer does not.

**2.1 Semantics**

Given an interpretation for HBAL types, which captures the way datatypes
are implemented in memory, and an operational semantics for the untyped
assembly instructions it was possible to prove a type soundness property.
The safety preservation theorem establishes that the execution of a typeable
HBAL program modifies structures on the heap safely.
First, it is necessary to define the function $\text{Asm}(p)$ that translate pseudo-instructions to sequences of untyped instructions which results from assembling $p$. We assume that the assembler has resolved each label $l$ to a memory location $LAdr(l)$. Below we show its definition by giving a pseudo-instruction on the left and its untyped expansion on the right.

<table>
<thead>
<tr>
<th>Pseudo-Instruction</th>
<th>Untyped Expansion</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>salloc A</code></td>
<td><code>arithi sp ← sp - (size(A))</code></td>
</tr>
<tr>
<td><code>sfree A</code></td>
<td><code>arithi sp ← sp + (size(A))</code></td>
</tr>
</tbody>
</table>
| `call l`           | `arithi $r_1 ← pc + 6$`  
                      | `store $sp[m] ← r_1$`  
                      | `arith pc ← r_0 + LAdr(l)` |
| `ret l`            | `load pc ← sp[0]`  |
| `fold-nil_A r_i[c]` | `store r_i[c] ← 0` |
| `fold-cons_A r_i[c]` | `store r_i[c] ← 1` |
| `caselist_A r_i[c] l_{cons}` | `load r_1 ← r_i[c]`  
                      | `bnz r_1 l_{cons}` |
| `fold-leaf_A r_i[c]` | `store r_i[c] ← 0` |
| `fold-node_A r_i[c]` | `store r_i[c] ← 1` |
| `casetree_A r_i[c] l_{node}` | `load r_1 ← r_i[c]`  
                      | `bnz r_1 l_{node}` |

Let $\text{Loc} \subseteq \mathbb{Z}$ stand for the set of memory locations on the machine, $\text{Reg} = \{0, 1, \ldots, R_{\text{max}}\}$ be the register indices, $\text{Wrd}$ be the set of machine words that can stand for integers or locations, and $\text{Code}$ be the set of machine words which can stand for machine instructions, and $\text{Wrd}$ is disjoint from $\text{Code}$.

A machine configuration $M$ is a pair $(R, H)$ where $H : \text{Loc} \rightarrow \text{Wrd} \uplus \text{Code}$ is a heap configuration and $R : \text{Reg} \rightarrow \text{Wrd}$ is a register configuration, such that $R(0) = 0$.

The unbounded stack assumption, that is, that every machine has the space to grow its stack downwards indefinitely, is formalized by saying that $H$ is defined to be data for all values below $R(sp)$, i.e., $\forall m \leq R(sp), H(m) \in \text{Wrd}$. To ensure that the stack does not clash with the heap data or program code, it is established that $R(sp) \leq 0$ while locations used for program and heap data are positive.

The effect of each machine instruction (i.e., an untyped assembly language instruction) on a machine configuration is defined as:

**Definition 1 (Machine transitions)** Given a machine $M = (R, H)$ we define $M \leadsto M' = (R', H')$, using the table below, by case analysis on the
instruction at $H(R(pc)) \in \text{Code}$:

\[
\begin{align*}
\text{load} & \quad r_i \leftarrow r_j[c] & R' = R[i \mapsto H(R(j) + c)] \\
\text{store} & \quad r_j[c] \leftarrow r_i & H' = H[R(j) + c \mapsto R(i)] \\
\text{arithi} & \quad r_i \leftarrow r_j \odot c & R' = R[i \mapsto R(j) \odot c] \\
\text{arith} & \quad r_i \leftarrow r_j \odot r_k & R' = R[i \mapsto R(j) \odot R(k)] \\
\text{jmp} & \quad x & R' = R[pc \mapsto x] \\
\text{bnz} & \quad r_i \quad x & R' = \begin{cases} R & \text{if } R(i) = 0 \\
R[pc \mapsto x] & \text{otherwise} \end{cases} \\
\text{bez} & \quad r_i \quad x & \text{similarly to bnz}
\end{align*}
\]

First, $M'$ differs from $M$ by incrementing $R(pc)$ according to the length of the instruction. Then the transformation given in the table above is applied, to give the new value $H'$ or $R'$ for an instruction that affects the register or heap configuration respectively.

In the definition above, the value of $i$ for the load and arithmetic instructions is greater than 0. As we said, the operations on $r_0$ have no effect.

Given a machine configuration $M = (R, H)$, the satisfaction relation $H \models_k m : A$ can be defined in such way that captures when the location $m$ represents a valid element of type $A$ in heap $H$. This relation is defined in [1].

Memory $M$ is type safe (for $P$) at $u$ if and only if:

- the typed program $P = (p_1, \ldots, p_u, \ldots, p_n)$ has been assembled in $M$ by applying the $\text{Asm}(p_k)$ function to each instruction $p_k \in p_1, \ldots, p_u$,

- $M$ satisfies the typing constraints necessary to execute the next instruction $p_u$.

The next theorem establishes that a type safe machine can always progress to a new machine by executing the next typed instruction.

**Theorem 1 (Progress)** Suppose $M$ is type safe at $u$. Then there exists a machine $M'$ such that $M \sim^{\text{Asm}(p_u)} M'$.

The second theorem establishes that whenever a type safe machine progresses to a new machine, the new machine is also type safe, provided we followed a typed path within the program $P$.

**Theorem 2 (Safety preservation)** Suppose $M$ is type safe at $u$ and $M \sim^{\text{Asm}(p_u)} M'$. Then either

- $\exists p_v$ such that $p_v \sim p_u$ and $M'$ is type safe at $v$, or

- $R'(pc) \notin \text{dom}(PAdr)$ (the machine has left $P$).

This theorem ends our presentation about the assembly language HBAL. The following sections are about the implementation of a compiler LFPL-to-HBAL and an interpreter for HBAL programs.
3 Implementation

As theorems 1 and 2 show, to guarantee safe execution of a HBAL program \( P \) we must:

- Typecheck \( P \) once \( (\Gamma_{init} \vdash P) \),
- Check that the memory satisfy the typing assumptions in the initial context before each execution \( (\Gamma_{init} \models M) \).

We implemented a compiler LFPL-to-HBAL and an HBAL machine model that executes HBAL programs provided by the compiler. In the following subsections we depict each module of our implementation, as shown in Figure 1. This system was implemented using Ocaml [6].

Compiler LFPL to HBAL

As shown in Figure 1, the compiler takes an LFPL program \( P \) as input and outputs an equivalent HBAL program \( P_H \), an initial context \( \Gamma_{init} \), and an environment \( \Sigma \).

The first-order functional language LFPL (Linear Functional Programming Language) has the following grammar of types and terms:

\[
A ::= \mathbf{N} \mid \diamond \mid L(A) \mid T(A) \mid A_1 \otimes A_2 \mid A_1 + A_2
\]

\[
e ::= x \quad \text{(variable)}
\mid f(e_1, \ldots, e_n) \quad \text{function application}
\mid c \quad \text{integer constant}
\mid e_1 * e_2 \quad \text{infix op., } \ast \in \{+,-,\times,=,\leq \ldots\}
\mid \text{if } e \text{ then } e' \text{ else } e'' \quad \text{conditional}
\mid \text{ln}(e) \quad \text{left injection}
\mid \text{lnr}(e) \quad \text{right injection}
\mid e_1 \odot e_2 \quad \text{pairing}
\mid \text{nil} \quad \text{empty list}
\mid \text{cons}(e_1, e_2, e_3) \quad \text{cons with res. arg.}
\mid \text{leaf}(e) \quad \text{leaf constructor}
\mid \text{node}(e_1, e_2, e_3, e_4, e_5) \quad \text{node constr. w. two res. args.}
\mid \text{match } e_1 \text{ with } \text{nil} \Rightarrow e_2 \mid \text{cons}(d, h, t) \Rightarrow e_3 \quad \text{list elimination}
\mid \text{match } e_1 \text{ with } \text{leaf}(a) \Rightarrow e_2
\mid \text{node}(d_1, d_2, a, l, r) \Rightarrow e_3 \quad \text{tree elim.}
\mid \text{match } e_1 \text{ with } x \odot y \Rightarrow e_2 \quad \text{pair elim.}
\mid \text{match } e_1 \text{ with } \text{ln}(x) \Rightarrow e_2 \mid \text{lnr}(x) \Rightarrow e_3 \quad \text{sum elim.}
\]

Heap space in LFPL is explicitly manipulated through high-level constructs; to construct a value of a recursive datatype, the programmer must supply an argument of type \( \diamond \) for every sub-instance of the recursive type. More about the LFPL language can be found in [3].
The compiler translates a LFPL program $P$ into a HBAL program $P_H$ and constructs the initial context $\Gamma_{init}$ and environment $\Sigma$. All of these are sent to the typechecker as input.

This part of our implementation could be consider as the code producer, the untrusted part of the generation of mobile code.

**Typechecker**

The compiler’s output is given to a typechecker that decides if the HBAL program $P_H$ is type safe in the environment $\Sigma$ with an initial context $\Gamma_{init}$. If it is safe, the program and the context are given to an assembler.

**Assembler**

This module applies the function $\text{Asm}(p)$ to each pseudoinstruction in the program $P_H$, obtaining an expanded untyped assembly program. After that, each instruction of the expanded program is assembled, i.e. stored in a cell of an array, and each label is replaced by its address.

The initial context $\Gamma_{init}$ and the assembled program $\text{Asm}(P_H)$, are provided to the machine model.

**Machine Model**

The first task of the Machine Model is to check if the heap configuration of the machine where the program will be executed verifies the restrictions imposed by the initial context $(H \models \Gamma_{init})$. If the initial machine $M = (R, H)$
is *memory safe*, then the evaluation module is called to execute the program \( \text{Asm}(P) \) on \( M \).

The execution of \( \text{Asm}(P) \) on the machine \( M = (R, H) \) is *safe*, because since \( H \models \Gamma_{\text{init}} \), by definition, \( M \) is safe for \( P \) at the first instruction, and by theorems 1 and 2, each step in the execution of \( \text{Asm}(P) \) progresses to a new *safe* machine.

The typechecker, assembler, and machine model modules are considered as the *code consumer*, and they are part of the TCB (*Trusted Computing Base*). The code provided by the compiler is safe, if it passes the analyses for *safe code* and *safe memory*.

It is worthy of mention that once the program \( P_H \) is determined as *code safe* and assembled, each new execution in the same TCB only requires the *memory safe* verification, which only involves checking the types of live registers against the current memory.

## 4 Examples

In this section we give some examples of HBAL programs that show the kind of errors that can be avoided by applying our typechecker.

Note that in this implementation the flagged word type notation was changed from \( \sigma^1 \) to \( \sigma^+ \) (initialized) and from \( \sigma^0 \) to \( \sigma^- \) (uninitialized).

### Preventing reading of uninitialized locations

The following HBAL program stores an integer (1) in the heap address pointed by \( r_5 \) and the next address, and the same integer in the register \( r_3 \). But an attempt to copy in the register \( r_3 \) the value stored in the \( r_5[2] \) is detected by the typechecker as a violation of the first load typing rule.

The notation \( r_5[c] \) is used to denote the value stored in the heap at the address pointed by the register \( r_5 \) with offset \( c \). A graphical explanation of this program intended execution is given in Figure 2.

```plaintext
sign
main:{sp: [[code]+, r5: [int+ * int+]]+}
<>"
main:
arithi r4 <- r0 + 1;
store r5[0] <- r4;
store r5[1] <- r4;
load r3 <- r5[1];
load r3 <- r5[2];
ret main;
<>

The value stored in \(r5[2]\) can be confidential information, then the problem can be considered as a \textit{privacy} violation, or junk, in such case the problem can be seen as a \textit{safety} concern.

\textbf{Preventing malicious diversion of control}

In procedure calls the calling convention gives this type to the stack pointer:

\[ sp : [A_1 \times \cdots \times A_n \times \text{[code]}^1 \times A^{i=0}] \]

The stack frame contains space for the return value of type \(A\), followed by the return pointer, and then the subroutine arguments at the top. Figure 3 shows graphically the stack after a procedure call with three arguments.

The next program illustrates an attack attempting to divert control to a different return address.

\begin{verbatim}
main:{sp:[int**int**int**[code]**int-]+}
<>
main:
load r2 <- sp[0];
arithi r3 <- r2 + 1;
store r2[3] <- r3;
ret main;
<>
\end{verbatim}

This program is rejected by the typechecker because the store operation attempts to alter a code address.
5 Conclusions

In this work we describe the implementation of a first-order linearly typed assembly language, HBAL. The HBAL language allows safe reuse of heap space for elements of different types. Linear typing ensures the single pointer property, disallowing aliasing, but allowing safe in-place-update compilation of programming language. HBAL was designed as a target low-level language for Hofmann’s LFPL programs that run in a bounded amount of heap space.

The described implementation includes a LFPL-to-HBAL compiler, the typechecker, and a machine model that execute HBAL programs. The system was implemented using the Ocaml language. The typechecker and machine model can be used as a Trusted Computing Base by a code consumer in an environment that uses mobile code.

The implementation is simplified by the fact that HBAL has a clear distinction between its syntax and its operational semantics: the store is not mentioned in its syntax or static semantics and the well typedness of a HBAL program is independent of the memory contents. Since it is unrealistic to expect to know the content of the memory where mobile code will be run to be able to establish its safety, this approach splits the concerns as one might expect. The typechecker can build a safety proof for execution on any safe memory, and the machine model only needs to check that the initial memory is safe for each run.

The compiler and typechecker can be used on-line, with examples of well behaved programs and programs with errors, at the web page:

http://www.cs.stevens-tech.edu/~abc/hbal/

Further research could integrate into HBAL a general scheme for defining high-level types apart from just lists and trees. Besides, some constructors could be added to allow a more flexible layout in memory, such as null pointers and a caseptr discriminator.

The implementation presented in this paper could be extended to compile different languages to HBAL. This extension may include languages without resource awareness that produce programs that are not memory safe. In such case the typechecker will work as a filter accepting only safe programs from the high-level language.

6 Acknowledgments

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References


