Revision of Plausibility Relations in Dynamic Systems

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Abstract

An agent receives information from the environment which usually includes other agents. Some of those agents could be providers of data. It is natural for the agent to maintain a certain order among the informants based on the reliability or plausibility they show. In a dynamic environment that order might change.

In this work we present a model for representing changes on plausibility relations. The central idea is that the beliefs of an agent are provided by a set of informants, for which there is a plausibility relation. This relation establishes if some informants are more reliable than others. We propose change operators for the plausibility relation. We give postulates for these operators and define their construction.

Keywords: Plausibility relations, Belief change, Revision, Contraction.

1 Introduction

Current reasoning systems attempt to model an agent’s knowledge and interaction with its environment in a symbolic manner. This environment, its world is generally dynamic and changing due to natural evolution or the actions of other agents that are a part of it. In consequence, an agent that is a part of a reasoning system must have the following components: a knowledge base where its knowledge of the world is stored, a communication mechanism with the environment and other agents in it, and a means of modifying its knowledge of the environment.

Knowledge may be represented by a logic language which is propositional, first order, modal or extensions of these. Each one of these alternatives has advantages as well as disadvantages. The higher the expressive power of a given language, the more computational problems there are regarding complexity and decidability.

Communication mechanisms can be varied, depending on the environment being modeled. They can be multimedia mechanisms such as microphones, speakers, video cameras, infrared sensors, motion detectors and even wired or wireless systems where information is transmitted without any kind of preprocessing. They are irrelevant, however, for the purpose of this work.
Mechanisms for modifying knowledge may be modeled by what is known as Belief Change Theory. Belief Change Theory assumes that the underlying language is at least propositional. An agent's knowledge is represented as a set of sentences and new information as a single sentence. In turn, every change operator takes a set of sentences and a single sentence and produces a new set of sentences as a result.

This paper is organized as follows. Section 2 introduces the main concepts related to belief revision. Section 3 presents the concept of plausibility and its application in belief revision systems. Section 4 defines revision of plausibility based relations, the operations involved, their characteristic postulates and their construction. Finally, section 5 includes this paper's conclusions as well future work.

We will adopt a propositional language $\mathcal{L}$ with a complete set of boolean connectives: $\land$, $\lor$, $\neg$, $\rightarrow$, $\leftrightarrow$. Formulas in $\mathcal{L}$ will be denoted by lowercase Greek characters: $\alpha, \beta, \delta, \ldots, \omega$. Sets of sentences in $\mathcal{L}$ will be denoted by uppercase Latin characters: $A, B, C, \ldots, Z$. The symbol $\top$ represents a tautology or truth. The symbol $\bot$ represents a contradiction or falsum. We also use a consequence operator $\text{Cn}$. $\text{Cn}$ takes sets of sentences in $\mathcal{L}$ and produces new sets of sentences. The operator $\text{Cn}$ satisfies inclusion ($A \subseteq \text{Cn}(A)$), iteration ($\text{Cn}(A) = \text{Cn}(\text{Cn}(A))$), and monotonicity (if $A \subseteq B$ then $\text{Cn}(A) \subseteq \text{Cn}(B)$). To simplify notation, we write $\text{Cn}(\alpha)$ for $\text{Cn}\{\alpha\}$ where $\alpha$ is any sentence in $\mathcal{L}$. We also write $\alpha \in \text{Cn}(A)$ as $A \vdash \alpha$. Moreover, belief bases will be finite set of sentences.

2 Belief Change

Belief revision is the process by which an agent changes its set of beliefs, making a transition from one epistemic state to another. When such an agent learns new information it may realize that this information clashes with its old beliefs. In this case the agent has to revise its belief set and decide which of the old beliefs need to be eliminated in favor of the new information.

One of the most fundamental approaches to the formalization of the dynamics of beliefs is the AGM model [AGMS85], proposed by Carlos Alchourrón, Peter Gärdenfors and David Makinson. In the AGM approach the epistemic states are represented by belief sets, that is, sets of sentences closed under logical consequence.

Let $\mathbf{K} = \text{Cn}(\mathbf{K})$ be a belief set and $\alpha$ a sentence in a propositional language $\mathcal{L}$. The three main types of changes are the following [GR92]:

**Expansion:** A new sentence is added to an epistemic state regardless of the consequences of the so formed larger set. If $\ast^+$ is an expansion operator, then $\mathbf{K}^{+\alpha}$ denotes the belief set $\mathbf{K}$ expanded by $\alpha$.

**Contraction:** Some sentence in the epistemic state is retracted without adding any new belief. If $\ast^-$ is a contraction operator, then $\mathbf{K}^{-\alpha}$ denotes the belief set $\mathbf{K}$ contracted by $\alpha$.

**Revision:** A new sentence is consistently added to an epistemic state. In order to make this operation possible, some sentences may be retracted from the original epistemic state. If $\ast^*$ is a revision operator, then $\mathbf{K}^{*\alpha}$ denotes the belief set $\mathbf{K}$ revised by $\alpha$.

Expansions can be defined as the logical closure of $\mathbf{K}$ and $\alpha$:

$$\mathbf{K}^{+\alpha} = \text{Cn}(\mathbf{K} \cup \{\alpha\})$$
It is not possible to give a similarly explicit definition of contractions and revisions using logical and set-theoretical notions only. These operations can be defined using logical notions and some selection mechanism. Contractions and Revisions are interdefinable by the following identities:

Levi Identity: \( K*\alpha = (K - \neg\alpha) + \alpha \).

Harper Identity: \( K - \alpha = K \cap K*\neg\alpha \).

Thus, given a definition for one of these operators we can obtain the other by using the above identities. Gärdenfors [Gär88] proposed the following basic rationality postulates for contraction operators:

(K1) Closure: \( K - \alpha = Cl(K - \alpha) \).

(K2) Inclusion: \( K - \alpha \subseteq K \).

(K3) Vacuity: If \( \alpha \not\in K \) then \( K - \alpha = K \).

(K4) Success: If \( K \not\vdash \alpha \) then \( \alpha \not\in K - \alpha \).

(K5) Recovery: \( K \subseteq (K - \alpha) + \alpha \).

(K6) Extensionality: If \( \vdash \alpha \leftrightarrow \beta \) then \( K - \alpha = K - \beta \).

and the following basic rationality postulates for revision operators:

(K*1) Closure: \( K*\alpha = Cl(K*\alpha) \).

(K*2) Success: \( \alpha \in K*\alpha \).

(K*3) Inclusion: \( K*\alpha \subseteq K + \alpha \).

(K*4) Vacuity: If \( K \not\vdash \neg\alpha \) then \( K*\alpha = K + \alpha \).

(K*5) Consistency: If \( \not\vdash \neg\alpha \) then \( K*\alpha \not\vdash \bot \).

(K*6) Extensionality: If \( \vdash \alpha \leftrightarrow \beta \) then \( K*\alpha = K*\beta \).

All of these operations have some controversial postulates. A thorough presentation of the different belief change models can be found in [Fal99].

3 Plausibility in the context of Belief Change

Among the operations for belief change, we have two that warrant special attention: contractions and revisions. Both of these operations require the elimination of sentences from a knowledge base. Therefore, in addition to a set of sentences which represent an agent’s knowledge state, we need a selection mechanism to determine which beliefs are eliminated in the change process and which are not. In order to make this possible, we use some method that assigns an informational value to sentences. In a process of pure contraction the sentences with the least informational value will be selected among the candidates for elimination. Models that use this technique are known as information-theoretic approaches.

Usually, theories that assign informational value to beliefs are based on the Bayesian Model. In this type of model, an agent’s epistemic state requires that each sentence be assigned a
measure of probability reflecting the belief’s degree of certainty. Then, if a belief must be eliminated from an epistemic state, the one with the lowest value can be selected.

However, this kind of modification cannot be modeled within classic models for belief change. This is because those beliefs which are accepted in an epistemic state (whether they are belief bases or belief sets) are completely true. This is to say, they have a maximum degree of certainty (a probability of 1). If this certainty value were changed, a new value as close to 1 as possible should be assigned. It is not possible to represent this epistemic attitude in the classic models of theory change.

The other possibility consists of assigning a different value to beliefs, one that represents their epistemic importance to the agent (epistemic entrenchment). [GM88, GR92]. This measure is completely external to the belief, not referring to the confidence to be had in the belief. What it represents is the importance (or weight) that this belief can have on an agent’s decision processes.

Let us contrast this to the case of probability. When we assign a probability \( x \) to a belief \( \alpha \), within a probabilistic model it is assumed that the probability of \( \neg\alpha \) is \( 1 - x \). This does not apply to epistemic entrenchment because if an agent believes \( \alpha \) it assumes maximum certainty for this belief, even though its weight can be low for a given decision process.

We propose a model of plausibility in which, instead of assigning a degree of importance to each sentence, we assume that there is an informant which provides it. This is to say, each sentence in the knowledge base is provided by an informant.

Associated with each knowledge base \( K \), there is an informant set \( J_K \). For each informant set \( J_K \) there is a plausibility relation \( G_{JK} \). In order to simplify the notation we will eliminate the subindex \( K \) for the informant set and the subindex \( J_K \) for the plausibility relation \( (J \) and \( G \) respectively). When we must carry out a change operation in which belief elimination is necessary, we eliminate those beliefs provided by the less reliable informants. This translates to informants which are lesser under the plausibility relation \( G \).

This paper’s central idea is not the definition of change operators based on plausibility. What we present are change operators that allow the modification of each informant’s degree of credibility relative to the other informants in \( J \). For example, if an informant provides information that proves to be wrong, the agent may decide to decrement its relative degree of credibility. If, on the other hand, an informant provides information that often turns out to be true its credibility should be raised. Some interesting related work can be found in [Par98, Res76].

4 Representation and revision of partial order relations

4.1 Representation of the informant relation

4.1.1 The concept of generator set

Let us assume that we have a universal set of informants, \( J \), and that, of these informants, some are to be considered more reliable than others. This is to say, in any case in which two distinct informants provide an agent with contradictory information the more trustworthy one is to be believed over the other. The agent must, therefore, have a mechanism by means of which the set \( J \) is ordered. To this end we present the following concept.

**Definition 4.1.1:** Given a set of informants \( J \) we will call any binary relation \( G \subseteq J^2 \) a generator set over \( J \). An informant \( i \) is less trustworthy than an informant \( j \) according to \( G \) if
\((i, j) \in G^*\).

\(G^*\) represents the reflexive transitive closure of \(G\). It is desirable for \(G^*\) to be a partial order over \(J\), although according to the preceding definition this is not always the case. We address this matter in the following definition.

**Definition 4.1.2:** A generator set \(G \subseteq J^2\) is said to be sound if \(G^*\) is a partial order over \(J\).

**Example 4.1.1:** For example the generator set \(G_1 = \{(i, j), (j, k), (i, l)\}\) is sound. However \(G_2 = G_1 \cup \{(k, i)\}\) is not sound because \((i, k) \in G_2^*\) and \((k, i) \in G_2^*\). This violates the antisymmetry condition for partial orders.

Why is it desirable for a generator set to be sound? For a relation to be a partial order it must obey reflexivity, antisymmetry and transitivity. Given a generator set \(G\) it is obvious that its reflexive transitive closure, \(G^*\), will obey reflexivity and transitivity. However if antisymmetry is not respected then there is at least one pair of distinct informants, \(i\) and \(j\) such that both \((i, j) \in G^*\) and \((j, i) \in G^*\). This would mean that both \(i\) is less trustworthy than \(j\) and that \(j\) is less trustworthy than \(i\). Given that these beliefs are contradictory, believing them simultaneously would lead the believing agent to inconsistencies.

### 4.1.2 Some interesting properties of Generator Sets

The following are interesting properties associated with generator sets.

\(\text{(G1)}\) : A generator set \(G\) is sound iff \(G\) can be represented by a directed acyclic graph.

The fact that \(G\) may be represented by a directed graph is trivial. The fact that it must be acyclic arises from the following argument. Let us assume that \(G\) contains a cycle of length longer than one. Cycles of length one are ignored because arcs of the form \((i, i)\) are to be expected due to reflexivity. Since one such arc must be present in \(G\) for all \(i \in J\) these may be ignored. Now let \(i, j \in J, i \neq j\) be two vertices of said cycle. Then there exists a path from \(i\) to \(j\) and from \(j\) to \(i\). This would imply that both \((i, j) \in G^*\) and \((j, i) \in G^*\). Since this violates antisymmetry \(G^*\) cannot be a partial order and therefore \(G\) cannot be sound. By a similar argument the reverse implication may also be proven.

\(\text{(G2)}\) : If \(G\) is a sound generator set and \((j, i) \notin G^*\) then \(G \cup \{(i, j)\}\) is a sound generator set.

Let us assume that \(G\) is a sound generator set, \((j, i) \notin G^*\) and that \(G \cup \{(i, j)\}\) is not sound. If \(G\) is sound then it has no cycle. And if \(G \cup \{(i, j)\}\) is not sound then it has a cycle and it follows that \((i, j)\) completed it. Therefore, there was a path from \(j\) to \(i\) in \(G\) and hence \((j, i) \in G^*\). This contradicts our earlier assumption.

### 4.2 The expansion operator

Let us assume that an agent learns that, of a pair of informants, one is more reliable than the other. This would warrant the modification of its knowledge accordingly. For this purpose, we define the operator \(\oplus : \mathcal{P}(\mathcal{I}^2) \times \mathcal{I}^2 \rightarrow \mathcal{P}(\mathcal{I}^2)\). This operator adds new tuples to a generator set
in order to establish relations between informants. Given a pair of informants and a generator set, this function returns a new generator set in which said agents are now related. According to this new generator set we may say that the first informant is “less reliable” than the second.

4.2.1 Postulates for the expansion operator

(E1) Success: \((i, j) \in (G \cup (i, j))^\ast\)

Establishing new relations among informants is most likely a costly process for the agent. Consequently a desirable property of expansions is that the new relation given will indeed be added to the agents beliefs, and not lost somehow.

(E2) Inclusion: \(G^\ast \subseteq (G \cup (i, j))^\ast\)

Here the case of equality between the previous set and the new one occurs in the event of an expansion by a relation which was already entailed by the generator set. This leads us to the following postulate for expansions.

(E3) Vacuity: if \((i, j) \in G^\ast\) then \((G \cup (i, j))^\ast = G^\ast\).

What this postulate states is that there is no information to be lost or gained by the addition of redundant data to the generator set.

(E4) Commutativity: \(((G \cup (k, l)) \cup (i, j))^\ast = ((G \cup (i, j)) \cup (k, l))^\ast\)

The order in which tuples are added to the generator set does not affect the final, closed relation. This is important because sometimes we will use \(G \cup A\) as a shorthand for the expansion of \(G\) by every tuple in \(A\). Such is the case of the following postulate.

(E5) Extensionality: if \(A^\ast = B^\ast\) then \((G \cup A)^\ast = (G \cup B)^\ast\)

The expansion of a generator set by two sets whose reflexive transitive closure is equal yields generator sets whose closure is also equal.

(E6) Conditional Soundness Preservation: if \(G\) is a sound generator set and \((j, i) \notin G^\ast\) then \(G \oplus (i, j)\) is a sound generator set.

4.2.2 Construction

In this subsection, we will introduce a construction of expansions on plausibility relations.

Definition 4.2.1: Given a pair of informants \(i, j \in J\) and generator set \(G \subseteq J^2\), we define the expansion of \(G\) by \((i, j)\) as \(G \oplus (i, j) = G \cup \{(i, j)\}\). \(\square\)

The following lemma summarizes some interesting properties of the operator.

Lemma 4.2.1: Let \(\oplus\) be an expansion operator as defined in Definition 4.2.1. Then \(\oplus\) satisfies success, inclusion, vacuity, commutation, and extensionality. \(\square\)
Expansion does not preserve soundness 
perse, but is conditioned as stated in the postulate. This property is a consequence of the properties of sound generator sets and the definition of expansion that we have provided.

4.3 The contraction operator

At the beginning of the previous subsection, we said that an agent may need to assert the fact that one informant is less reliable than another. In a similar fashion the opposite may also become true. This is to say, we may wish to reflect the fact that an informant is no longer more reliable than another. For this purpose we define a contraction operator \( \ominus : \mathcal{P}(J^2) \times J^2 \rightarrow \mathcal{P}(J^2) \).

Assume we have a pair of informants \( i \) and \( j \) and a generator set \( G \). The basic task of the \( \ominus \) function is to construct a new generator set in which this is no longer the case while losing as little information as possible. However we cannot simply remove the pair \((i, j)\) from \( G \). Care must be taken to also remove pairs that, through transitivity, would imply the pair \((i, j)\) in \( G^* \). As long as there is a path in the generator set from \( i \) to \( j \), \((i, j)\) will be found in its transitive closure. It is therefore necessary to eliminate a set of pairs so that no path is left from \( i \) to \( j \) in \( G \). This set is desirably minimal.

4.3.1 Postulates for the contraction operator

(C1) Inclusion: \((G \ominus (i, j))^* \subseteq G^*\)

If a tuple is entailed by a generator set, then its contraction by said tuple removes at least one element from the set: the tuple itself. The sets are equal in the case in which \((i, j) \notin G^*\). This is expressed in the following postulate.

(C2) Vacuity: if \((i, j) \notin G^*\) then \(G \ominus (i, j) = G\)

That is, if a tuple is not a consequence of a given generator set then its contraction by said tuple provokes no change.

(C3) Success: if \(i \neq j\) then \((i, j) \notin (G \ominus (i, j))^*\)

A tuple cannot be entailed by the generator set resulting from its contraction. In the case of \(i = j\), the tuple will trivially be in the reflexive transitive closure of any generator set due to reflexivity.

(C4) Path Disruption: for all \( k \in J \), if \((i, k) \in G^* \) and \((k, j) \in G^*\) then either \((i, k) \notin (G \ominus (i, j))^* \) or \((k, j) \notin (G \ominus (i, j))^* \)

Let \( k \in J \) be such that both \((i, k)\) and \((k, j)\) are in \( G^* \), and assume that we contract \( G \) by \((i, j)\). If both \((i, k)\) and \((k, j)\) are still entailed then by transitivity \((i, j)\) would also be entailed. This would go against the success postulate.

(C5) Recovery: if \((i, j) \notin G^*\) then \(G^* \subseteq ((G \ominus (i, j)) \circ (i, j))^*\)
This postulate is a direct consequence of the vacuity postulate for contraction and the inclusion postulate for expansion.

**(C6) Reverse Recovery:** if \((i, j) \in G^*\) then \(((G \uplus (i, j)) \ominus (i, j))^* \subseteq G^*\)

Here the case of equality between the sets arises when the contraction of \(G\) by \((i, j)\) only causes the deletion of this tuple and no other implying pairs must also be removed. If other pairs were removed to avoid the appearance of \((i, j)\) in the closure then they would not reappear with the expansion of \(G \ominus (i, j)\) by \((i, j)\).

**(C7) Soundness Preservation:** if \(G\) is a sound generator set then \(G \ominus (i, j)\) is a sound generator set.

### 4.3.2 Construction

In this subsection we will introduce a construction for contractions on plausibility relations. However, before we do so, we will need to present a few concepts.

First let us briefly review the concept of path. We say that a set of tuples \(P\) is a *path* from \(i\) to \(j\) if \((i, j) \in P\), or \((i, k) \in P\) and there is a path from \(k\) to \(j\) in \(P\). We say that \(P\) is a *nonredundant path* from \(i\) to \(j\) if it is a path from \(i\) to \(j\) and there is no path from \(i\) to \(j\) in every \(P' \subset P\).

**Definition 4.3.1:** Given a pair of informants \(i, j \in I\) and generator set \(G \subseteq I^2\), we define the *path set* from \(i\) to \(j\) in \(G\), and we will note it \(G_{ij}\), as

\[
G_{ij} = \{ C \subseteq G : C \text{ is a nonredundant path from } i \text{ to } j \text{ in } G \}
\]

Notice that according to this definition the path set from \(i\) to \(j\) in a generator set \(G\) is a set of sets. Each set represents a path from \(i\) to \(j\). In the contraction of \(G\) by \((i, j)\), in order to avoid the appearance of this tuple, none of these paths may remain complete. Therefore, we need a selection function to decide which tuples will be erased from each path in \(G_{ij}\).

**Definition 4.3.2:** Given a minimum clipping of \(G_{ij}\), we say that \(\gamma\) is a *cut function* for \(G_{ij}\) if and only if:

1. \(\gamma(G_{ij}) \subseteq G\).
2. For each \(C \in G_{ij}, \gamma(G_{ij}) \cap C \neq \emptyset\).

Now we may present our definition of contraction.

**Definition 4.3.3:** Given a pair of informants \(i, j \in I\) and generator set \(G \subseteq I^2\), we define the contraction of \(G\) by \((i, j)\) as \(G \ominus (i, j) = G \setminus \gamma(G_{ij})\)

The following result gives a summary of the properties of the contraction operator.
Lemma 4.3.1: Let $\otimes$ be a contraction operator as defined as in Definition 4.3.3. Then $\otimes$ satisfies inclusion, vacuity, success, path disruption, recovery, reverse recovery and soundness preservation.

Notice that here, in contrast to the case of expansion, the soundness preservation property of contraction is not conditioned. This is due to the way we define contraction. Since contraction is basically a process of elimination, it is impossible for this operation to introduce cycles if there were none to begin with.

4.4 Revision operator

Suppose that an agent learns that an informant is less reliable than another. The agent’s current generator set should be modified to reflect this new information. However, it would be convenient if the generator set were also modified, when necessary, so that the opposite can no longer hold. That is to say, if up to now the agent believed that the second informant was less reliable then this should be retracted.

For this purpose we define the revision operator $\otimes: \mathcal{P}(I^2) \times I^2 \rightarrow \mathcal{P}(I^2)$. Assume we have a pair of informants $i$ and $j$ and a generator set $G$, and the agent now has reason to believe that $i$ is less reliable than $j$. The basic task of the $\otimes$ operator is to construct a new generator set in which $(i, j)$ is entailed but $(j, i)$ is not.

4.4.1 Postulates for the revision operator

(R1) Success: $(i, j) \in (G \otimes (i, j))^*$

This is basically a consequence of the definition given for revision and the success postulate for expansion.

(R2) Inclusion: $(G \otimes (i, j))^* \subseteq (G \oplus (i, j))^*$

This is due to the fact that expansion simply inserts the new tuple into the generator set while revision may need to remove tuples before adding the new one. The border case of equality presents itself when $(j, i) \notin G^*$, which leads us to our next postulate.

(R3) Vacuity: if $(j, i) \notin G^*$ then $G \otimes (i, j) = G \oplus (i, j)$

This is a consequence of our definition of revision and the vacuity postulate for contraction. In this case, there is nothing to be contracted before expanding.

(R4) Path Disruption: for all $k \in I$, if $(j, k) \in G^*$ and $(k, i) \in G^*$ then either $(j, k) \notin (G \otimes (i, j))^*$ or $(k, i) \notin (G \otimes (i, j))^*$

This postulate is analogous to the one presented for contraction. Let $k \in I$ be such that both $(j, k)$ and $(k, i)$ are in $G^*$, and assume that we revise $G$ by $(i, j)$. If both $(j, k)$ and $(k, i)$ are still entailed then, by transitivity, $(j, i)$ would also be entailed. This would go against the success postulate for the contraction performed previous to expansion according to our definition of revision.
(R5) **Soundness Preservation:** if \( G \) is a sound generator set then \( G \otimes (i, j) \) is a sound generator set.

### 4.4.2 Construction

In this subsection, we will introduce a construction of revisions on plausibility relations.

**Definition 4.4.1:** Given a pair of informants \( i, j \in J \) and generator set \( G \subseteq J^2 \), we define the revision of \( G \) by \( (i, j) \) as \( G \otimes (i, j) = (G \circ (j, i)) \circ (i, j). \)

The following lemma enunciates some interesting properties of the operator.

**Lemma 4.4.1:** Let \( \otimes \) be a revision operator as defined in Definition 4.4.1. Then \( \otimes \) satisfies **success**, **inclusion**, **vacuity**, **path disruption**, and **soundness preservation**.

Again here, as in the case of contraction, soundness preservation is not conditioned. In the case that the new tuple to be inserted, \( (i, j) \) were to complete a cycle, the previous contraction of \( (j, i) \) would insure that there is no link between \( j \) and \( i \). Hence, it is impossible for revision to introduce cycles.

## 5 Conclusions and Future Work

We have introduced a model for representing changes in plausibility relations. We presented different change operators on the plausibility relation, giving postulates for said operators as well as defining their construction. If we view every belief in the epistemic state of an agent as provided by an informant, we can dynamically modify the order among beliefs throughout the agent’s span of existence.

Clearly, what follows is to devise ways of handling the perception of changing plausibilities in real sources of information. Such is the case of weather forecasting systems, predictors of stock market behavior, *et cetera*. From these examples we will seek to understand the complexities of dynamic updating in decision making and advising systems.

### References


