The Ant Colony Metaphor for Multiple Knapsack Problem

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Abstract
This paper presents an Ant Colony (AC) model for the Multiple Knapsack Problem (MKP). The ant colony metaphor, as well as other evolutionary metaphors, was applied successfully to diverse heavily constrained problems. An AC system is also considered a class of multiagent distributed algorithm for combinatorial optimisation. The principle of an AC system is adapted to the MKP. We present some results regarding its performance against known optimum for different instances of MKP. The obtained results show the potential power of this particular evolutionary approach for optimisation problems.

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1. Introduction

The Zero/One Multiple Knapsack Problem and Zero/One Knapsack Problem have been intensively studied using different traditional methods, such as Branch-and-Bound and Dynamic Programming [11,12]. Also, modern heuristic techniques [9,10,13] like Genetic Algorithms (GA) and Simulated Annealing (SA) have shown to be able to produce high-quality solutions for these types of highly constrained NP-complete problems.

In this paper we propose to solve MKP by using the Ant Colony Metaphor [4,5], an approach based on the result of low-level interaction among many co-operating simple agents that are not aware of their co-operative behaviour. Each simple agent is called 'ant' and the AC system (a distributed algorithm) is a set of ants co-operating in a common problem solving activity.

Our work has been inspired by previous works in this area [2,3,5,6] in which different versions of AC are used in order to solve Travelling Salesman Problem (TSP), Bin Packing and continuous space optimisation problems. Problems like TSP and Bin Packing can be represented as a sequence on \( n \) items (\( n \) cities to be visited or \( n \) objects to be packed), where the actual order of the sequence determines a particular solution to the problem. Thus in general, the search space consists of all \( n! \) permutations.

Bin Packing and TSP are properly suitable to be solved by using an AC system [2]. In this paper, we adapt the original AC system [4] so it can be used to solve non-ordering problems like the MKP. We also present experimental results that show that the adapted AC system can solve MKP in an efficient way. In this adapted AC system, the ants (agents) are not concerned with discovering the best ordering (or tours), they just look for a subset of \( n \) items, such that the total profit is maximised and all constraints are satisfied.

The adapted AC system uses Ant-cycle [5], a particular instance of the algorithms belonging to Ant system class (other instances proposed in [5] are Ant-density and Ant-quantity). In Ant-cycle every ant changes the system shared memory using a quantity (called trail) that is proportional to its global behaviour. On the other hand, Ant-density and Ant-quantity algorithms use strictly local information.

The primary purpose of our study is to evaluate the AC system performance in relation with the known results for different instances of MKP. The MKP instances considered are taken from [1].

We also present some results regarding its performance when varying the values of the parameters that control the probabilities for item selection.

The remainder of the paper is organised in the following way. In the next sections the MKP formulation and the classical and adapted model of an Ant Colony System are given. Next, the experiments performed, the results obtained and the statistical analysis are shown. Finally, the conclusions are exposed.

2. MKP formulation

MKP can be formulated \([1,9,11]\) as:

\[
\text{maximise} \quad \sum_{j=1}^{n} p_j x_j \quad (2.1)
\]

\[
\text{subject to} \quad \sum_{j=1}^{n} r_{ij} x_j \leq c_i \quad i = 1, \ldots, m \quad (2.2)
\]

\[
x_j \in \{0,1\} \quad \quad j = 1, \ldots, n \quad (2.3)
\]
Each of the $m$ constrains described in equation (2.2) is called a knapsack constrain, so the MKP is also called the $m$-dimensional Knapsack Problem.

Let $I=\{1,...,m\}$ and $J=\{1,...,n\}$, with $c_i \geq 0$ for all $i \in I$, $j \in J$. A well-stated MKP assumes that $p_j > 0$ and $r_{ij} \leq c_i < \sum_{j \in J} r_{ij}$ for all $i \in I$, $j \in J$, since any violation of these conditions will result in some $x_i$’s being fixed to zero and/or some constrains being eliminated. Note that the $(r_{ij})_{m \times n}$ matrix and $(c_i)_{m}$ vector are both non-negative which distinguishes this problem from general 0-1 linear integer programming problem.

Many practical problems can be formulated as a MKP, for example, the capital budgeting problem where project $j$ has profit $p_j$ and consumes $r_{ij}$ units of resource $i$. The goal is to find a subset of the $n$ projects such that the total profit is maximised and all resource constrains are satisfied.

3. The Ant Colony System for a Order Based Problem

In this section, we describe our AC system applied to the Travelling Salesman Problem.

Given a set of $n$ cities, the Travelling Salesman Problem [11,12] is to find a closed path that visits every city exactly once (tour) with minimal total length. i.e.

\[
\text{minimize } \text{COST}(i_1,...,i_n) = \sum_{j=1}^{n-1} d(C_{i_j}, C_{i_{j+1}}) + d(C_{i_n}, C_{i_1})
\]

where $d(C_k, C_l)$ is the distance between city $k$ and city $l$.

Let $b_i(t) (i=1,...,n)$ be the number of ants in city $i$ at time $t$ and let $N_a = \sum_{i=1}^{n} b_i(t)$, the total number of ants.

Let $\tau_{ij}(t+n)$ be the intensity of trial on path $ij$ at time $t+n$, given by

\[
\tau_{ij}(t+n) = \rho \tau_{ij}(t) + \Delta \tau_{ij}(t, t+n)
\] (3.1)

where $\rho$ is such $(1-\rho)$ is the coefficient of evaporation ($0<\rho<1$).

\[
\Delta \tau_{ij}(t, t+n) = \sum_{k=1}^{N_a} \Delta \tau_{ij}^k(t, t+n), \text{ where } \Delta \tau_{ij}^k(t, t+n) \text{ is the quantity per unit of length of trial substance (pheromone in real ants) laid on path } ij \text{ by the } k\text{-th ant between time } t \text{ and } t+n \text{ and is given by the following formula:}
\]

\[
\Delta \tau_{ij}^k(t, t+n) = \begin{cases} 
Q & \text{if } k \text{-th ant uses edge } (i, j) \text{ in its tour} \\
L^k & \\
0 & \text{otherwise}
\end{cases}
\] (3.2)

where $Q$ is a constant and $L^k$ is the tour length of the $k$-th ant.

The intensity of trial at time 0, $\tau_{ij}(0)$, is set to a randomly chosen value.

During the next $(t+n)$ tour the probability to visit city $j$ when being at city $i$ is
where \( \text{allowed}_k \) is a set of cities not visited for that particular tour and \( \eta_{ij} \) is a local heuristic. For the TSP, the parameter \( \eta_{ij} \), called visibility, is \( 1/d(C_i, C_j) \) [5]. The parameters \( \alpha \) and \( \beta \) allow a user control on the relative importance of trail versus visibility. Hence, the transition probability is a trade-off between visibility, which says that close cities should be chosen with high probability, and trail intensity, that says that if on path \( ij \) there is a lot of traffic then is it highly profitable.

A data structure, called tabu list, is associated to each ant in order to avoid that ants visit a city more than once, i.e. the tabu \(_k\) list maintain a set of visited cities up to time \( t \) by the \( k \)-th ant. Therefore the \( \text{allowed}_k \) set can be defined as follow: \( \text{allowed}_k = \{ j \mid j \not\in \text{tabu}_k \} \). When a tour is completed the tabu list is emptied and every ant is free again to choose an alternative way.

By using the above definitions, we describe the Ant-cycle algorithm:

---

**The Ant-cycle algorithm**

1. **Initialise:**
   - Set \( t := 0 \) \( \{ t \) is the time counter\}.
   - For every edge \((i,j)\) set an initial value \( \tau_{ij}(t) \).
   - For every edge \((i,j)\) set \( \Delta \tau_{ij}(t, t+n) := 0 \).
   - Place \( b_i(t) \) ants on every node \( i \) \( \{ b_i(t) \) is the number of ants on node \( i \) at time \( t \} \).
   - Set \( s := 1 \) \( \{ s \) is the tabu list index\}.
   - For \( i := 1 \) to \( n \) do
     - For \( k := 1 \) to \( b_i(t) \) do
       - tabu\(_k\)(s):=i \( \{ \) starting town is the first element of the tabu list of the \( k \)-th ant\}.

2. **Repeat until tabu list is full** \( \{ \) this step will be repeated \((n-1)\) times\}.
   - Set \( s := s + 1 \) \( \{ \) for every town\}.
   - For \( k := 1 \) to \( b_i(t) \) do
     - Choose the town \( j \) to moved to, with probability \( P_{ij}(t,k) \) given by equation (3.3).
     - Move the \( k \)-th ant to \( j \) \( \{ \) this instruction creates the new values \( b_j(t+1) \} \).
     - Insert node \( j \) in tabu\(_k\)(s) \( \{ \) it results from the tabu list\}.

3. **For \( k := 1 \) to \( n \) do**
   - Compute \( L^k \) \( \{ \) scan the tabu list of the \( k \)-th ant\}.
   - For \( s := 1 \) to \( n-1 \) do
     - Set \((h,l) := (\text{tabu}_k(s), \text{tabu}_k(s+1)) \) \( \{ (h,l) \) is the edge connecting town \( s \) y \( s+1 \) in the tabu list of ant \( k \} \).
     - \( \Delta \tau_{hl}(t, t+n) := \Delta \tau_{hl}(t, t+n) + Q/L^k \) \( \{ \) in the tabu list of ant \( k \} \).

4. **For every edge \((i,j)\) compute \( \tau_{ij}(t+n) \) according to equation (3.1)**.
   - Set \( t := t+n \)
For every edge \((i,j)\) set \(\Delta \tau_{ij}(t,t+n)=0\)

\[\text{For every edge } (i,j) \text{ set } \Delta \tau_{ij}(t,t+n)=0.\]

5 Memorise the shortest tour found up to now
   if \((NC < NC_{\text{MAX}})\) or (not all the ants choose the same tour)

   \[\text{if } (NC < NC_{\text{MAX}}) \text{ or (not all the ants choose the same tour)} \]
   \[\text{then}\]
   \[\text{Empty all tabu list}\]
   \[\text{Goto step 1.2}\]
   \[\text{else}\]
   \[\text{Print shortest tour and Stop}\]

4. The Ant Colony System for MKP

In order to solve MKP, it is necessary to adapt the Ant Colony model in some way. The purpose of the ants in MKP is not to get a tour with minimum cost like in TSP; but they look for a subset of \(n\) items or projects (see MKP formulation) such that the total profit is maximised and all resource constrains are satisfied.

Let \(b_i \ (i=1,...,n)\) be the number of ants incorporating in the solution the item \(i\) at time \(t=0\) and let \(N_a = \sum_{i=1}^{n} b_i\); the total number of ants.

Since in MKP there are not paths, the intensity of trial and visibility are computed in a slightly different way.

Let \(\tau_i(t+N_{\text{max}})\) be the intensity of trial on item \(i\) at time \(t+N_{\text{max}}\), given by

\[
\tau_i(t+N_{\text{max}}) = \rho \tau_i(t) + \Delta \tau_i(t, t+N_{\text{max}})
\]

(4.1)

where \(\rho\) is such \((1-\rho)\) is the coefficient of evaporation and \(N_{\text{max}}\) is the maximum number of items qualified to be added to some solution by some ant.

\[
\Delta \tau_i(t, t+N_{\text{max}}) = \sum_{k=1}^{N_a} \Delta \tau_i^k(t, t+N_{\text{max}}), \quad \text{where } \Delta \tau_i^k(t, t+N_{\text{max}}) \text{ is the quantity per unit of length of trial substance (pheromone in real ants) laid on item } i \text{ by the } k\text{-th ant between time } t \text{ and } t+N_{\text{max}} \text{ and is given by the following formula:}
\]

\[
\Delta \tau_i^k(t, t+N_{\text{max}}) = \begin{cases} 
L^k & \text{if } k\text{-th ant incorporates item } i \\
Q & \\
0 & \text{otherwise}
\end{cases}
\]

(4.2)

where \(Q\) is a constant and \(L^k\) is the profit (Eq. 2.1) obtained by the \(k\)-th ant.

The intensity of trial at time 0, \(\tau_i(0)\), is set to a randomly chosen value.

During the next \((t+N_{\text{max}})\) item incorporation the probability to select the item \(i\) by the \(k\)-th ant, in order to complete the solution \(k\) is:
\[
P_i(t,k) = \begin{cases} 
\left( \frac{[\tau(t)]^\alpha [\eta(k,t)]^\beta}{\sum_{j \in allowed_k} [\sigma(t)]^\alpha [\eta(k,t)]^\beta} \right) & i \in allowed_k \\
0 & \text{otherwise} 
\end{cases}
\tag{4.3}
\]

where \( allowed_k \) is a set of items still not considered by the \( k^{th} \) ant and the \( solution_k \) satisfies all constraints if some of them are added. The parameter \( \eta_i \), called pseudo-utility, is a local heuristic. We chose \( \eta_i \) as follow:

\[
\eta_i(k,t) = \frac{p_i}{\bar{\delta}_j(k)} ; \quad \bar{\delta}_j(k) = \frac{\sum_{j=1}^{m} \delta_i(k)}{m} \tag{4.4}
\]

\[
\delta_j(k) = \frac{r_{ji}}{(c_j - u_j(k))} ; \quad u_j(k) = \sum_{l \in solution_k} r_{jl}
\]

Where \((c_j - u_j(k))\) is the remaining amount to reach the boundary of the constraint \( j \), \( r_{ji} \leq (c_j - u_j(k)) \) and \( \delta_j(k) \in (0,1] \), is the tightness of item \( i \) on constraint \( j \) when item \( i \) is added to \( solution_k \). Consequently the pseudo-utility \( \eta_i(t,k) \) turns larger as \( \bar{\delta}_j(k) \) (tightness average) turns smaller.

The parameters \( \alpha \) and \( \beta \), as for TSP, allow a user control on relative importance of trail versus the heuristic (pseudo-utility for MKP). Hence, the transition probability is a trade-off between pseudo-utility, which says that more profitable items that uses less resources should be chosen with high probability, and trail intensity, that says that if item \( i \) is part of a lot of solutions, then is it highly desirable.

A data structure, called tabu list, is also associated to each ant in order to avoid that ants choose a item more than once, i.e. the \( tabu_k \) list maintain the set of added items up to time \( t \) by the \( k^{th} \) ant. This list also maintains \( u_j(k) (j=1..m) \) in order to reduce the required computational time.

The \( allowed_k \) set can be defined as follows: \( allowed_k = \{ j \mid j \notin tabu_k and the solution_k with item j added satisfies all constraints \} \). When all ants add to the solutions as many items as they can, an item \( h_k \) is selected from the \( k^{th} \) tabu list. Then the \( k^{th} \) tabu list is emptied and the \( k^{th} \) ant is free again to choose starting with the item \( h_k \) as its initial solution.

The outline of the adapted Ant-cycle algorithm follows:
The Adapted Ant-cycle algorithm

1. Initialise:
   Set \( t := 0 \) \{t is the time counter\}
   For every item (i) set an initial value \( \tau_i(t) \)
   For every item (i) set \( \Delta \tau_i(t, t+N_{\text{max}}) := 0 \)
   \( b_i \) ants choose the item i \{\( b_i \) is the number of ants choosing item i at time 0\}
   Set \( s := 1 \) \{s is the tabu list index\}
   For \( i := 1 \) to \( n \) do
     For \( k := 1 \) to \( b_i \) do
       \( \text{tabu}_k(s) := i \) \{initial item of the tabu list of the k-th ant\}

2. For \( k := 1 \) to \( N_a \) do
   \( s := 2 \)
   Repeat until some constraint is not satisfied by k-th ant
   Choose the item i, with probability \( P_i(t, k) \) given by equation (4.3)
   \( \text{tabu}_k(s) := i \)
   \( s := s + 1 \)

3. For \( k := 1 \) to \( N_a \) do
   Compute \( L_k \) \{it results from the tabu list\}
   For \( s := 1 \) to Number of items in \( \text{tabu}_k \) do \{scan the tabu list of the k-th ant\}
   \( h = \text{tabu}_k(s) \)
   \( \Delta \tau_h(t, t + N_{\text{max}}) := \Delta \tau_h(t, t + N_{\text{max}}) + L_k/Q \)

4. For every item (i) compute \( \tau_i(t+N_{\text{max}}) \) according to equation (4.1)
   Set \( t := t + N_{\text{max}} \)
   For every item (i) set \( \Delta \tau_i(t, t+N_{\text{max}}) := 0 \)

5. Memorise the best solution found up to now
   if \( NC < N_{\text{Cmax}} \) or (not all the ants find the same solution)
   \{NC is the number of algorithms cycles; in NC cycles are tested NC.Na solutions\}
   then
     \( h_k := \) item randomly select from \( \text{tabu}_k \) \( (k=1..Na) \)
     Empty all tabu list
     \( \text{tabu}_k(1) = h_k \) \( (k=1..Na) \)
   Goto step 2
   else
     Print best solution and Stop

5. Experimental results

Several parameters were considered for the experiments. Next each one and its values for different running are presented below.

- \# cycles: \( 20 \)
- \# items of the instance to be applied: \( \sum_{i=1}^{n} p_i \) \{Eq. 2.1\}
- \( Q \) (used in Eq. 4.2): \( \sum_{i=1}^{n} p_i \)
- Coefficient of evaporation (\( \rho \)): \( 0.3, 0.7 \)
- Trade-off between trail and pseudo-utility (\( \alpha, \beta \)): \( (0,1), (1,0), (1,1), (1,5), (5,1) \)
The above values were selected regarding the results achieved in previous works [2,3,4,5,6]. The five combinations of values corresponding to $\alpha$ and $\beta$ parameters have influence on the probability values $P(t,k)$ as follows:

a) $(\alpha=0, \beta=1)$ - only the heuristic is important (no co-operation between agents)
b) $(\alpha=1, \beta=0)$ - only the trial is important (no problem knowledge tailored)
c) $(\alpha=1, \beta=1)$ - heuristic and trial are equally proportional
d) $(\alpha=1, \beta=5)$ - the heuristic is more important
e) $(\alpha=5, \beta=1)$ - the trial is more important

**Table I** shows for each test case the following data:

- # of instance
- Size of instance $<n,m>$
- Known optimum (from [1])
- The best result obtained out of 5 runs by the AC system using some combination of parameter values

<table>
<thead>
<tr>
<th>#instance</th>
<th>Instance</th>
<th>Known Optimum</th>
<th>Best Value by AC</th>
</tr>
</thead>
<tbody>
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<td>4015</td>
<td>4015</td>
</tr>
<tr>
<td>2</td>
<td>&lt;20,10&gt;</td>
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<td>6120</td>
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<td>3</td>
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<td>12400</td>
</tr>
<tr>
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<td>&lt;39,5&gt;</td>
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<td>10570</td>
</tr>
<tr>
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</tr>
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</table>

*Table I. Best results obtained by the AC system*

The shadow cells in Table I indicate suboptimal results which are just 4 out of 19 instances of the MKP considered. For example, the best value obtained for the instance #8 is the same that was reported by Khuri et al. [9] where a GA was used. A
similar situation takes place for instance #19. In this case, the value corresponding to "known Optimum" column is the best value reported by Paul Chu et al. [13] again, by using a GA.

It is important to remark that for some instances, the AC system was able to find the best solution (or suboptimal) when the first cycle was completed, meaning that the greedy heuristic was sufficient, excluding any co-operation. However, the best results in general were obtained by using \( (\alpha=1, \beta=1) \) or \( (\alpha=1, \beta=5) \) combinations, i.e. the significance of the heuristic influence was at least as important as the trail influence. Table II shows the relative importance of the trail and heuristic effect on the final result, for instances #8, #9, #10 and #15 (from Table I).

<table>
<thead>
<tr>
<th>#instance</th>
<th>Known Optimum</th>
<th>( \alpha=0, \beta=1 )</th>
<th>( \alpha=1, \beta=0 )</th>
<th>( \alpha=1, \beta=1 )</th>
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</table>

Table II. Relative importance of trial versus pseudo-utility

By the \( (\alpha=1, \beta=0) \) combination, the AC system achieved the worst results, because it explores the solution search space by using only co-operation which alone is not a very effective strategy. On the other hand, by \( (\alpha=5, \beta=1) \) combination, the AC system showed for all instances a stable behaviour, however the achieved results were not the best ones. In Figure 1 the best results found in each cycle by using two different seeds for instance #11 are plotted. It can be seen that the AC system stuck prematurely in a local optimum due to the considerable pressure on the trail \( (\alpha=5) \).

Figure 1. The AC system stuck in a local optimum

Figure 2 shows the changes on the amount of trail on each item for instance #9, along the running of the AC system. It can be seen that as the running proceeds, the amount of trail turns larger on those items which are part of the solution. On the other hand, the amount of trail is not necessarily zero or near zero for that items which are not part of the solution. At the bottom of the Figure 2, it is possible to note the correspondence between the best solution in relation to the amount of trial after 20 cycles.
Figure 2. Amount of trail along the AC system running

Figure 3, for the same instance, shows other perspective of the amount of the trial on each item by plotting that amount for the first (randomly chosen) and the last cycle (when the AC system converged to the solution).

Finally, it is worth to note that the variation on the evaporation coefficient ($\rho$ parameter) did not influence strongly the AC system performance.
6. Conclusions

We have shown an alternative approach to solve the Multiple Knapsack Problem. The original conception applied to Travelling Salesman Problem, Bin Packing and continuous space optimisation problems, was adapted to obtain an AC system able to solve effectively MKP.

Although in some cases the greedy heuristic (local search) was enough, the best performance of the AC system was achieved when the trial and heuristic guide the search in conjunction. However, the weight of the heuristic owned a primary role when the probabilities of the item selection were calculated.

Considering the acceptable performance of our AC system, future works include: an extensive study regarding the effect on the performance of the AC system for different values of its main parameters; tuning the parameters in order to test harder instances of MKP; and finally, regarding the importance of the heuristic, to enhance the AC system by using alternative heuristics.

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