Simple dynamical models of the Sagittarius dwarf galaxy

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ABSTRACT

We present two simple dynamical models for Sagittarius based on \(N\)-body simulations of the progressive disruption of a satellite galaxy orbiting for 12.5 Gyr within a realistic Galactic potential. In both models the satellite initially has observable properties similar to those of current outlying dwarfs; in one case it is purely stellar while in the other it is embedded in an extended massive halo. The purely stellar progenitor is a King model with a total velocity dispersion of 18.9 km s\(^{-1}\), a core radius of 0.44 kpc and a tidal radius of 3 kpc. The initial stellar distribution in the other case follows a King profile with the same core radius, a slightly larger total velocity dispersion and similar extent. Both these models are consistent with all published data on the current Sagittarius system, they match not only the observed properties of the main body of Sagittarius, but also those reported for unbound debris at larger distances.

Key words: Galaxy: halo – Galaxy: structure – galaxies: individual: Sagittarius dSph – galaxies: interactions – Local Group.

1 INTRODUCTION

The Sagittarius dwarf galaxy is the closest satellite of the Milky Way (Ibata, Gilmore & Irwin 1994, 1995, hereafter IG95). Soon after its discovery, several groups carried out simulations to see if its properties were consistent with the disruption of an object similar to the other dwarf companions of the Milky Way, but none produced a model in full agreement with both the age and the structure of the observed system (Johnston, Spergel & Hernquist 1995; Velázquez & White 1995; Edelsohn & Elmegreen 1997; Ibata et al. 1997, hereafter I97; Gómez-Flechoso, Fux & Martinet 1999). All groups assumed light to trace mass and an initial system similar to observed dwarf spheroidals. All found the simulated galaxy to disrupt after one or two orbits whereas the observed system has apparently completed ten or more. Most considered this to be a problem (but cf. Velázquez & White 1995). As a result, several unconventional models were proposed to explain the survival and structure of Sagittarius. In an extensive numerical study, Ibata & Lewis (1998) concluded that Sagittarius must have a stiff and extended dark matter halo if it is to survive with 25 per cent of its initial mass still bound today. Since an extended halo cannot remain undistorted in the Galaxy’s tidal field for any conventional form of dark matter, it is unclear how this idea should be interpreted. Furthermore, it produces an uncomfortably large mass-to-light ratio (\(~100\) ), it cannot reproduce the observed elongation and it suggests that little tidal debris will be liberated, in apparent conflict with the observations of Mateo, Olszewski & Morrison (1998) and Majewski et al. (1999) (see also Johnston et al. 1999b). A somewhat less unorthodox model was proposed by Zhao (1998), where Sagittarius was scattered onto its current tightly bound orbit by an encounter with the Magellanic Clouds about 2 Gyr ago. This appears physically possible but requires careful tuning of the orbits of the two systems (see Ibata & Lewis 1998; Jiang & Binney 2000). Another mechanism by which the dwarf could have moved to a short-period orbit is dynamical friction, which can be important only if Sagittarius has lost a lot of mass in the past. Jiang & Binney (2000) found a oneparameter family of initial configurations that evolve into something like the present system over a Hubble time. Their initial systems have masses \(~10^{10-11} \, M_\odot\) and start from a Galactocentric radius \(~200\, kpc\).

Driven by this apparent puzzle, we decided to search more thoroughly for a self-consistent model of the disruption of Sagittarius, which, after a Hubble time, has similar characteristics to those observed. (See Table 1 for a summary of the observed properties of the system.) Below we present two models which meet these requirements.

2 METHOD

In our numerical simulations, we represent the Galaxy by a fixed potential with three components: a dark logarithmic halo

\[
\Phi_{\text{halo}} = -\frac{v_{\text{halo}}^2}{2} \ln(r^2 + d^2),
\]

(*)
Table 1. Properties of Sagittarius (IGI95; I97).

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Orbital properties</td>
<td></td>
</tr>
<tr>
<td>distance from the Sun d</td>
<td>25 ± 2 kpc</td>
</tr>
<tr>
<td>heliocentric radial velocity v^e_{cen}</td>
<td>140 ± 2 km s^{-1}</td>
</tr>
<tr>
<td>proper motion in b \mu_b</td>
<td>250 ± 90 km s^{-1}</td>
</tr>
<tr>
<td>gradient along the orbit d\nu/\partial b</td>
<td>&lt; 3 km s^{-1} , deg^{-1}</td>
</tr>
<tr>
<td>angular position in the sky (l, b)</td>
<td>(5.6°, -14°)</td>
</tr>
<tr>
<td>Internal properties</td>
<td></td>
</tr>
<tr>
<td>luminosity</td>
<td>\geq 10^3 , L_\odot</td>
</tr>
<tr>
<td>velocity dispersion \sigma(r_0)</td>
<td>11.4 ± 1 km s^{-1}</td>
</tr>
<tr>
<td>angular extent in (l, b)</td>
<td>8° × 3°</td>
</tr>
<tr>
<td>half-mass radius</td>
<td>0.55 kpc</td>
</tr>
<tr>
<td>mean metallicity ([Fe/H])</td>
<td>~ -1.0 dex</td>
</tr>
</tbody>
</table>

where a Miyamoto–Nagai disc

\[ \Phi_{\text{disc}} = -\frac{GM_{\text{disc}}}{\sqrt{R^2 + (a + \sqrt{a^2 + b^2})^2}} \]

and a spherical Hernquist bulge

\[ \Phi_{\text{bulge}} = -\frac{GM_{\text{bulge}}}{r + c}, \]

where d = 12 kpc and v_{\text{halo}} = 131.5 km s^{-1}; M_{\text{disc}} = 10^{11} \, M_\odot; a = 6.5 kpc and b = 0.26 kpc; M_{\text{bulge}} = 3.4 \times 10^{10} \, M_\odot and c = 0.7 kpc. This choice of parameters gives a flat rotation curve with an asymptotic circular velocity of 186 km s^{-1}. The mass of the dark-matter halo within 16 kpc is 7.87 \times 10^{10} \, M_\odot in this model.

We represent the satellite galaxy by a collection of 10^7 particles and model their self-gravity by a multipole expansion of the internal potential to fourth order (White 1983; Zaritsky & White 1988). This type of code has the advantage that a large number of particles can be collected in a relatively small amount of computer time. Hence a substantial parameter space can be explored while retaining considerable detail on the structure of the disrupted system. In this quadrupole expansion, higher than monopole terms are softened more strongly. We choose \epsilon_1 \sim 0.2-0.25\sigma_c for the monopole term (\sigma_c is the core radius of the system) and \epsilon_2 = 2\epsilon_1 for dipole and higher terms and for the centre of expansion. The centre of expansion is a particle which, in practice, follows the density maximum of the satellite closely at all times.

For the stellar distribution of the pre-disruption dwarf we choose a King model (King 1966), since this is a good representation of the distant dwarf spheroidals. King models are defined by a combination of three parameters: \psi(r = 0) (depth of the potential well of the system), \sigma^2 (measure of the central velocity dispersion) and \rho_0 (central density) or r_0 (King radius). The ratio \psi(r = 0)/\sigma^2 defines how centrally concentrated the system is, and for any value of this parameter, a set of homologous models with different central densities and core (or King) radii may be found. We assume that the progenitor of Sagittarius obeys the known metallicity–luminosity relation for the Local Group dSph (Mateo 1998). The metallicity determinations for Sagittarius (I97) indicate ([Fe/H]) \sim -1, corresponding to a total luminosity in the range 3.5 \times 10^{-2} - 3.5 \times 10^{0} \, L_\odot. To obtain an initial guess for the mass of the system, we transform this luminosity into a mass assuming a mass-to-light ratio \sim 2. The relevant initial stellar mass interval is then 7 \times 10^2 - 7 \times 10^3 \, M_\odot.

Note that our choice of a fixed potential to represent our Galaxy means that we neglect any exchange of energy between the satellite and the Galactic halo. This is an excellent approximation for the range of orbits and satellite masses that we consider, since these imply dynamical friction decay times substantially in excess of the Hubble time. The orbits are also sufficiently large that impulsive heating during disc passages can be neglected.

The orbit of Sagittarius is relatively well constrained (I97). The heliocentric distance d \sim 25 ± 2 kpc and position (l, b) = (5.6°, -14°) of the galaxy core are well determined; the heliocentric radial velocity v^e_{cen} \sim 140 ± 2 km s^{-1} and its variation across the satellite are also accurately measured. Outside the main body (b < -20°) the radial velocity shows a small gradient dv_r/\partial b \sim 3 \, km s^{-1} deg, but no gradient is detected across the main body itself. The proper motion measurements are not very accurate; \mu_b \sim 2.1 ± 0.7 \, mas yr^{-1}, and no measurement is available in the l-direction. On the other hand the strong north–south elongation of the system suggests that it has little motion in the l-direction, thus implying the orbit should be close to polar. We generate a range of possible orbits satisfying these constraints and concentrate on those with relatively long periods in order to maximize the survival chances of our satellite. We begin all our simulations half a radial period after the Big Bang to allow for the initial expansion. We place the initial satellite at apocentre, then we integrate forward until \sim 13 Gyr. The orbits are chosen so at this time the position and velocity of the satellite core correspond to those observed. We allow ourselves some slight freedom in choosing the final time in order to fit the observed data as well as possible.

3 RESULTS

Fig. 1 gives an example of an orbit which is consistent with all the current data on Sagittarius. It has a pericentre of 16.3 kpc, an apocentre of 68.3 kpc, and a radial period of \sim 0.85 Gyr. We use similar orbits for all the simulations described below. Note that the slow precession about the Galactic rotation axis is in part the result of the quasi-polar nature of the orbit and in part to the fact we have assumed the Milky Way's dark halo to be spherical.

After letting our satellite relax in isolation, we integrate each simulation for \sim 13 Gyr. In practice we needed to run a large number of simulations, and test each to see if it satisfies the observational constraints at the present time. Since it remains uncertain whether dwarf spheroidals have extended dark halos (e.g. Klessen & Kroupa 1998), we have considered both purely stellar models and models in which the initial stellar system is embedded in a more massive and more extended dark halo.
3.1 Constant mass-to-light ratio: a purely stellar model

Our preferred purely stellar model (Model 1) initially has a core radius of \( r_c = 0.44 \text{kpc} \), a total velocity dispersion of \( 18.9 \text{km s}^{-1} \) and a concentration parameter \( c = \log_{10}(r_c/r_e) - 0.83 \). This implies a total mass of \( M = 4.66 \times 10^8 M_{\odot} \). For a satellite to survive for about 10 Gyr on an orbit with pericentre \( \sim 15 \text{kpc} \), apocentre \( \sim 70 \text{kpc} \) and period \( \sim 1 \text{Gyr} \) (for which the observational constraints are satisfied), its initial central density has to be \( \rho_0 \geq 0.36-0.4 M_{\odot} \text{pc}^{-3} \). Satellites with significantly smaller initial densities do not survive long enough.

In Fig. 2 we plot heliocentric distance as a function of galactic latitude for stars projected near the main remnant 12.5 Gyr after infall. Streams of particles are visible at all latitudes over a broad range of distance. Sagittarius has been orbiting long enough for its debris streams to be wrapped several times around the Galaxy. (See also Fig. 8, Section 3.3.1.)

The remnant galaxy, i.e. the central region of the satellite’s debris, is similar to the real system. In Fig. 3 we plot its mass surface density. The transformation from observed surface brightness to mass surface density (which is what the simulations give us) can be done as follows. The observed mass surface density \( \Sigma \) for an assumed mass-to-light ratio \( Y \) is

\[
\Sigma = \frac{N_X L_X}{f_X Y} \quad (M_\odot \text{deg}^{-2}),
\]

where \( N_X \) is the number of observed stars of type X per square degree, \( L_X \) is their luminosity and \( f_X \) is the fraction of the total luminosity in stars of type X. In IGI95 the spatial structure of Sagittarius was determined from the excess of counts at the apparent magnitude of the horizontal branch. Uncertainties in the result are primarily the result of contamination by sources in the Galactic bulge. Their lowest isodensity contour is at \( \Sigma_{\text{min}} \sim 5 \times 10^6 M_\odot \text{deg}^{-2} \), assuming \( Y \sim 2.25 \) and \( [\text{Fe/H}] \sim -1 \) (Bergbusch & VandenBerg 1992), and has an extent of \( 7.5^\circ \times 3^\circ \). This same isodensity contour is shown in Fig. 3 as a thick line. It has an extent of \( -8^\circ \times 4.8^\circ \), in reasonable agreement with the observations given the uncertainties. In I97 isodensity contours were derived from counts of main sequence stars close to the turn-off, roughly one magnitude above the plate limit. The minimum contour in this case corresponds to \( \Sigma_{\text{min}} \sim 10^5 M_\odot \text{deg}^{-2} \), and has an extent of roughly \( 15^\circ \times 7^\circ \). In Fig. 3 this contour is shown as a dashed line, and has an extent of \( 21^\circ \times 6.5^\circ \), also in good agreement with the observations. Note that the isophotes (or isodensity contours) become rounder towards the centre of the satellite. Its angular core radius is \( R_c \sim 1.29^\circ \), which for a distance of 26 kpc (derived from the simulations) corresponds to 0.58 kpc, again in good agreement with the observations.

The kinematic properties of the remnant galaxy are more difficult to compare with observations because a substantial amount of mass from debris streams is projected on top of the main body. Like I97, we measure the radial velocity across the system considering only particles for which \( 100 \text{km s}^{-1} \leq v_{\text{hel}} \leq 180 \text{km s}^{-1} \). In the left panel of Fig. 4 we plot the heliocentric radial velocity, and in the right panel we plot its dispersion as a function of Galactic latitude. For comparison, we analysed the observations of I97 at CTIO (Cerro Tololo Inter-American Observatory) in the same way (their table 2b); these data have a precision of a few km s\(^{-1}\) (triangles in Fig. 4). Our model is consistent with the observed kinematics; we obtain a heliocentric radial velocity of \( 139.5 \text{km s}^{-1} \) and an internal velocity dispersion in the radial direction of \( 11 \text{km s}^{-1} \) for the main body. However, when the radial velocity restrictions for inclusion in this calculation are relaxed, we find much larger velocity dispersions because of the contribution of stars from other streams. It is important to consider this problem when determining which stars should be considered members of Sagittarius.

3.2 Varying mass-to-light ratio: a model with a dark halo

The observational data for Sagittarius mainly refer to the current
remnant system, which corresponds to the innermost regions of the progenitor satellite. As a consequence, models that are initially dark matter dominated in their outskirts are relatively poorly constrained.

As an example we focus on a progenitor with a mass distribution which is similar to that of Model I in its inner regions, but is considerably more extended. We take the mass distribution to be a (heavy) King model with $r_c = 0.54$ kpc and $r_t = 10.4$ kpc, with an initial total velocity dispersion of 25.2 km s$^{-1}$ and total mass of $M = 1.7 \times 10^9 M_\odot$. For an orbit like that of Model I this produces a suitable remnant after 12 Gyr. The mass distribution of this remnant satisfies many of the observational constraints of Table 1. Its core radius is slightly larger $r_c \sim 0.65$ kpc, and the radial velocity dispersion in the main body is 12.1 km s$^{-1}$.

We will construct a two-component satellite with this mass distribution by solving for the dependence of mass-to-light ratio on the initial binding energy which produces the initial light profile of Model I. We choose the mass-to-light ratio of satellite material to be a decreasing function of binding energy, so that the most bound particles have near 'stellar' mass-to-light ratios, whereas weakly bound particles are almost entirely 'dark'. From the energy distribution of the heavy King model, and that of a King model with $r_0 = 0.095$ kpc and $\sigma = 25.6$ km s$^{-1}$, we can derive the mass-to-light ratio as a function of binding energy as

$$Y(\epsilon) = Y_* \frac{dM/d\epsilon}{dM/d\epsilon} = e_\epsilon + e_{\text{max}} - e_{\text{max}},$$

where $Y_*$ is the mass-to-light ratio of a stellar population. The energies $e_\epsilon$ of the lighter King model have been shifted by a fixed amount $e_{\text{max}} - e_{\text{max}}$, to be on the same scale as that of the heavier King model. The resulting mass-to-light ratio is shown in Fig. 5.

In Fig. 6 we show the surface mass densities normalized to their central values for Model I (only stars), for the heavy King model and for the two-component model ('stars' and dark matter). We shall refer to this two-component model as Model II, which is obtained by weighting each simulation particle by $Y(\epsilon)^{-1}$.

If we require that the central stellar mass surface densities of Model I and Model II be the same, we find that the total mass in stars in Model II is $\sim 1.69 \times 10^9 M_\odot$. To match Sagittarius surface brightness, we choose the central stellar mass-to-light ratio $Y_0 = 1.5$. Thus, the total luminosity of Model II is then $1.13 \times 10^8 L_\odot$, implying a mass-to-light ratio of 15.1. Its initial velocity dispersion is 23 km s$^{-1}$. The visible extent of the remnant has properties which are almost identical to those of Model I, and we find its velocity dispersion to be 11.1 km s$^{-1}$. Both results are again in good agreement with the observations.

The two initial satellites (Models I and II) have the same stellar mass distributions in their inner regions, differing only in that one has an extended dark halo. We may thus conclude that the presence of a dark halo does not affect the final structure of the remnant, which is very similar in both models. However there is a significant difference in the properties of their debris streams. In Model I the unbound debris streams are predicted to contain 5.2 times the light in the main body of the remnant ($M_V \sim -14.1$), as defined by the dotted contour in Fig. 3, whereas in Model II ($M_V \sim -13.4$) this ratio is 4.85. If we had chosen Model II to be a constant mass-to-light ratio model, we would have obtained an almost equally good fit to the main body of Sagittarius, but would have predicted the streams to contain 19 times the light in the main body of the remnant. In this last case, Sagittarius would have contributed $4.56 \times 10^8 L_\odot$ to the Galactic stellar halo in the form of debris stars (for $Y = 3.5$). Thus we see that the observed properties of the main remnant do not usefully constrain the number of stars which may be present in the debris streams, but that the different models can be better constrained from the properties of their debris streams, as we exemplify below.

### 3.3 Discussion

#### 3.3.1 Some predictions

In this section we concentrate for simplicity on Model I. We can use it to predict star counts as a function of distance and radial velocity at different points on the sky. We focus on fields along the path defined by the orbit of Sgr, which is where we expect to find debris streams. This is illustrated in Fig. 7, where the number counts are normalized to their values on the main body of our simulated Sagittarius, as shown in the first row. We assume fields which are $1° \times 1°$. For the distance, we use 5-kpc bins, whereas for the radial velocity we take 25 km s$^{-1}$ bins. Note that the contrast of structures in the radial velocity counts are generally larger than
properties of the main body of Sagittarius, it is nevertheless worthwhile to compare our simulations to data sets which have claimed detections of Sagittarius debris.

3.3.2.1 Outer structure of Sagittarius. Mateo et al. (1998) have traced Sagittarius material out to 30° from its nucleus: the globular cluster M54. They obtained deep photometric data along the southeast extension of the major axis of Sagittarius. In Fig. 9 we show the particle counts in our simulation for the strip 3° to 10° in longitude, and spanning about 30° in latitude outside the main remnant body. For comparison we plot the data by Mateo and collaborators, shifted a few degrees in latitude, and arbitrarily offset in number counts. Thus qualitatively we reproduce the break in the number counts profile. This change in slope is indicative of the transition between material which is still bound today and that lost in the last pericentric passage.

3.3.2.2 Star counts at b = −40°. Majewski et al. (1999) have claimed a detection of a possible stream from Sagittarius at b = −40° and l = 11°, at a slightly smaller heliocentric distance of 23 kpc and with a radial velocity of the order of 30 km s⁻¹. As they discuss, this velocity may be strongly affected by contamination from other Galactic components. We note, however, that we would predict a stream of stars (shown in blue) going through this latitude and longitude with roughly the observed distance, and with a radial velocity of 55 km s⁻¹. (See the central and bottom left panels of Fig. 8, −90° ≤ l ≤ 90°.) As mentioned above, this stream is formed mostly by material lost in the previous pericentric passage and not three passages ago, as in the model of Johnston et al. (1999b). This difference reflects the different orbital time-scales in the two models. The surface density of stars may be able to distinguish between them; it is predicted to be higher in our case.

Unfortunately, Majewski and collaborators could not detect the northern stream. They either did not reach the magnitude limit of 19.3 mag expected for the red giant clump, or were offset by a few degrees from its expected location. Thus, for example, Majewski et al. (1999) had a limiting magnitude of ~21 at b = 41° and l = −6°, but V ≲ 19 at b = 41° and l = 6°. The actual stream in our model is predicted to go through l ≈ 1° and to be about 2° wide. Note that the width prediction is more secure than the location since the motion of Sagittarius in the l-direction is poorly constrained at present, although a flattened halo would make the streams wider.

3.3.2.3 RR Lyrae found by the Sloan Digital Sky Survey. The Sloan Digital Sky Survey (SDSS) commissioning data has detected 148 candidate RR Lyrae stars in about 100 deg² of sky, along the celestial equator (−1.27° ≤ δ ≤ 1.27°), and from α = 160.5° to α = 236.5° (Ivezic et al. 2000). Although the faint-magnitude limit of the SDSS would allow them to detect RR Lyrae stars to large Galactocentric distances, they find no candidates fainter than r* ≈ 20, i.e. farther than 65 kpc from the Galactic centre. The distribution of stars in their sample is very inhomogeneous and shows a clump of over 50 stars at about 45 kpc from the Galactic centre, which is also detected in the distribution of non-variable objects with RR Lyrae star colours.

By studying carefully Fig. 8, and from our previous discussions, we are naturally led to believe this substructure could be associated with the northern streams of Sagittarius. In the upper left panel of Fig. 10 we see how, in our simulations of Model I, a stream of material intersects the area observed by SDSS. The
Figure 8. Top panel: distribution in the sky \((l, b)\) of the particles for our constant mass-to-light ratio model of Sagittarius after 12.5 Gyr. Different colours indicate material stripped off in different passages. Central panel: heliocentric distance as a function of Galactic latitude, at the same time as the top panel, and with the same colour coding. Note that ‘streams’ formed early on are wider than the more recent ones. Bottom panel: heliocentric radial velocity as a function of Galactic latitude, at the same time and using the same colour coding as before.
positions of the particles in our simulations are in excellent agreement with those of the RR Lyrae candidates belonging to the reported substructure. The upper right panel shows the visual magnitude of the particles falling in the region of the sky analysed by SDSS. We note here that there are basically two substructures in this region: one at $V \sim 19.5$ mag, and a second one, at a fainter magnitude $V \sim 20.5$ mag (for $M_V = 0.7$ mag characteristic of RR Lyrae stars, e.g. Layden et al. 1996). The first lump clearly could correspond to the substructure observed in the SDSS data. The material in this lump is mostly formed by particles that were lost in recent pericentric passages (i.e. 1–3 Gyr ago) as shown in the bottom left panel of Fig. 10.

As Ivezić et al. (2000) discuss, they do not find any RR Lyrae stars fainter than $V \sim 20$ mag. This would be in apparent contradiction with our results, (e.g. top right panel of Fig. 10). However, we need to estimate how much material we find in each lump, calibrate this number with respect to the number of RR Lyrae in the lump observed by SDSS and thereby determine how many RR Lyrae SDSS could have been missed. In the first lump we find 1264 particles, whereas the second has 362 particles. According to Ivezić et al. (2000) the detection efficiency decreases rapidly between $V \sim 20$ mag, where it is 50 per cent, and $V \sim 21$ mag, where it is zero. We here assume that for stars of $V \sim 20.5$ mag this efficiency is about 15 per cent, which means that only 54 of the 362 particles could, in principle, have been observed. Therefore, we estimate that the ratio of unobserved to that of observed debris material is 0.043 in this region of the sky. Thus if SDSS found $\sim 50$ RR Lyrae belonging to the first substructure, it should have detected $\sim 2.14 \pm 1.46$ RR Lyrae in the fainter magnitude range. This means that the failure to detect

Figure 9. Number counts along the major axis of the remnant system, outside its main body, within a strip of $3^\circ$ to $10^\circ$ in longitude. The error bars indicate Poissonian noise in the number counts. For comparison, we show the data by Mateo et al. (1998) arbitrarily shifted.

Figure 10. The top left panel shows the region of the sky analysed by the SDSS, where an excess of RR Lyrae has been observed. The top right panel shows the distribution of apparent magnitudes (i.e. distances for $M_V = 0.7$ mag) of the particles in our simulations falling in that region of the sky. We have colour coded particles according to the range in distance: thick black dots correspond to $18 \leq V \leq 20$, lighter black dots to $V = 18$ and grey diamonds to $V \geq 20$. Note that the first group is strongly clustered around the magnitude range 19–19.5, as found by the SDSS for their RR Lyrae. The bottom left panel shows the distribution of pericentric passages (i.e. times) when the particles became unbound for each of the subgroups. The dotted histogram corresponds to all the particles present in this field of the sky. We note here that there are about twice as many particles which have been released in the last 3 Gyr than earlier on. Most of the material in the first clump ($V \sim 19–19.5$) became unbound in the twelfth to fourteenth pericentric passages, i.e. 1–3 passages ago. Conversely all particles in the second clump ($V \sim 20.5$) became unbound in the first seven passages. Finally the bottom right panel shows the radial velocity distribution with the same colour coding as before. We note that the stream appears rather diffuse in velocity space and strongly clustered in space because of the ‘bunching up’ of the particles orbits which takes place near their apocentres.

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fainter RR Lyrae in this region of the sky is barely significant in this context. From this perspective we cannot rule out that a second stream of debris material is located at much larger distances (typically between 80 and 100 kpc from the Sun, as shown in Fig. 8).

Nevertheless the absence of a visible stream may be indicating that this material could be dark-matter dominated. This second stream is formed by particles that became unbound more than 7 Gyr ago. It therefore corresponds to particles orbiting the outskirts of the progenitor of Sagittarius. If this region of the system was dark-matter dominated, such streams would remain unobservable. Fainter data (V ∼ 20–21 mag) in this region of the sky could be crucial to constrain the initial properties of the system, e.g. size, total luminosity. This particular region of the sky should thus be explored further!

3.3.2.4 Carbon stars by the APM. The APM survey has detected about 75 high latitude carbon giants presumably belonging to the halo. These stars being of intermediate age, could trace streams that have recently become unbound from Sagittarius or from other Galactic satellites. Ibata et al. (2000) have proposed that a large fraction of the observed halo carbon stars belong to Sagittarius tidal debris, since they preferentially occur near the great circle of its orbit. Even though there are large uncertainties in the determination of distances to these carbon stars, and the survey is not complete, particularly in regions where we expect Sagittarius streams to be present, this proposal clearly fits within the expectations for the models we have developed here.

4 CONCLUSIONS

We have found viable models for the Sagittarius dwarf galaxy with a wide range of total luminosities and masses, and both with and without extended dark halos. A purely stellar progenitor could be a King model with a total velocity dispersion of 18.9 km s⁻¹, a core radius of 0.44 kpc and a tidal radius of 3 kpc. For the case where the progenitor is embedded in an extended massive halo, the initial stellar distribution follows a King profile with the same core radius, a slightly larger total velocity dispersion of 23 km s⁻¹ and similar extent. The dark matter is more extended. The data available at present only weakly constrain the total initial extent either of the light or of the mass. The observed metallicity data, for example, are consistent with an initial galaxy similar to either of our detailed models, both of which would lie within the scatter of the luminosity–size–velocity dispersion–metallicity distribution for more distant dwarf spheroidal galaxies in the Local Group. Thus we see no indication that Sagittarius is in any way anomalous. Further work on the debris streams of Sagittarius is needed to constrain better its initial total luminosity, and to distinguish between purely stellar or dark-matter dominated progenitors.

It is certainly encouraging that our models could reproduce the data available both on the main body and on the debris streams. We wish to stress, however, that this does not mean that we have found the ‘ultimate’ model. Other models with similar characteristics may also exist. Alternatives would include progenitors with smaller stellar masses or larger dark halos; flattened systems or with anisotropic velocity distributions; or systems with a stellar disc and a spherical dark halo (as proposed for the progenitors of dSph by Mayer et al. 2000). Moreover, our assumption of a rigid Galactic potential, which does not vary in time over 12 Gyr, is clearly simplistic in view of current models for the formation of structure in the Universe. Only when we have a better estimate of the total luminosity of Sagittarius, both in its main body, as well as on its streams, we will be able to model it in greater detail. The present interest in the debris streams of Sagittarius will help us understand not only the properties of what has turned out to be just another dwarf spheroidal, but also the formation history of our Galaxy. A complete map of the streams will, for example, allow us to derive the Galactic potential (Johnston et al. 1999a). If these streams are less smooth or broader than expected, this may indicate smaller scale structure present in the halo either now or when this was assembled.

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