AN ATLAS OF BURST OSCILLATIONS AND SPECTRAL PROPERTIES IN 4U 1728−34

STEVE VAN STRAATEN, MICHIEL VAN DER KLIS, ERIK KUULKERS, and MARIANO MÉNDEZ

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ABSTRACT

We study correlations between the burst properties and the position in the color-color diagram of the low mass X-ray binary 4U 1728−34 using 21 bursts found in two data sets obtained with the Rossi X-Ray Timing Explorer. Using spectral fits we analyze the spectral evolution during the bursts and determine the burst peak flux, temperature, rise time, and fluence. Using dynamical power spectra, we study the properties of the ~363 Hz burst oscillations. We find correlations between fluence, peak flux, the occurrence of radius expansion, and the presence of burst oscillations and the position of the source in the color-color diagram. The radius expansion bursts with and without burst oscillations differ both with respect to where they occur in the color-color diagram and in how the radius expansion takes place. We compare our results with those of a similar study by Muno and coworkers for KS 1731−26. Both KS 1731−260 and 4U 1728−34 show more or less the same behavior with respect to the dependence of the presence/absence of the burst oscillations on the position of the source in the color-color diagram, but the dependence of most of the spectral burst parameters on the position in the color-color diagram is clearly different. We find that the systematic absence in 4U 1728−34 of burst oscillations in the "island" state of the color-color diagram is not explained by the bursts involving mixed H-He burning, as Cumming & Bildsten found may be the case in KS 1731−260.

Subject headings: accretion, accretion disks — binaries: close — stars: individual (4U 1728−34) — stars: neutron — X-rays: bursts — X-rays: stars

1. INTRODUCTION

Type I X-ray bursts (for a review see, e.g., Lewin, van Paradijs, & Taam 1993) in the low-mass X-ray binary (LMXB) 4U 1728−34 were discovered with the SAS 3 observatory in 1976 (Lewin 1976; Hoffman et al. 1976). An extensive study of the burst properties of 96 bursts was done by Basinska et al. (1984) with the Y-axis detectors on board SAS 3. Radius expansion bursts were reported by Basinska et al. (1984), Inoue (1988), Foster, Fabian, & Ross (1986), and Day & Tawara (1990). The source has been classified by Hasinger & van der Klis (1989) as an atoll source based on timing and spectral observations with the EXOSAT satellite. The distance to the source is about 4 kpc (van Paradijs 1978; Foster et al. 1986; Di Salvo et al. 2000). No optical counterpart has been identified (Liller 1977).

After the launch of the Rossi X-Ray Timing Explorer (RXTE), burst oscillations on a millisecond timescale (i.e., at 363 Hz) were first discovered in 4U 1728−34 by Strohmayer et al. (1996b). Such oscillations have since been found in several other atoll sources, i.e., 4U 1636−53 (Strohmayer et al. 1998b, 1998c; Strohmayer 1999; Miller 1999, 2000; Zhang et al. 1997), 4U 1702−43 (Strohmayer & Markwardt 1999; Markwardt, Strohmayer, & Swank 1999), KS 1731−260 (Morgan & Smith 1996; Smith, Morgan, & Bradt 1997; Muno et al. 2000), MXB 1743−29 (Strohmayer et al. 1996a; Strohmayer et al. 1997), Aql X-1 (Zhang et al. 1998; Ford 1999; Yu et al. 1999), and marginally in the Rapid Burster (Fox & Lewin 1999). The frequency during the burst usually increases to an asymptotic value that tends to be quite stable (see for an overview Strohmayer, Swank, & Zhang 1998a). This led to a simple model (Strohmayer et al. 1997) in which the oscillations arise due to a hot spot in a layer that due to the burst has expanded in radius (by 10−30 m; this is not related to the expansion by several kilometers during classical radius expansion bursts) and is therefore rotating slightly slower than the neutron star itself. As the layer contract, the frequency increases toward the neutron star spin frequency. However, note that in 4U 1636−53 (Miller 1999; Strohmayer 1999) and in KS 1731−260 (Muno et al. 2000) decreases in frequency have also been seen. For 4U 1728−34, Strohmayer et al. (1998b) found that for three bursts (bursts 4, 5, and 17 in this paper) occurring more than 1.5 yr apart, the observed asymptotic oscillation periods were all close to 2.7476 ms and within 0.2 μs of each other.

For several atoll sources, correlations have been found between timing properties and the position of the source in the X-ray color-color diagram (e.g., Hasinger & van der Klis 1989; Prins & van der Klis 1997; Méndez et al. 1999; van Straaten et al. 2000). A correlation between the position of 4U 1728−34 in the color-color diagram and several power spectral features is shown in Méndez & van der Klis (1999) and Di Salvo et al. (2001). The most obvious explanation for these correlations is that both the timing properties and the position in the color-color diagram track the changing mass accretion rate (Hasinger & van der Klis 1989), from low in the so-called island state and increasing along the banana branch (for definitions see Hasinger & van der Klis 1989). A link between the position in the color-color diagram and burst spectral properties was found for 4U 1636−53 (van der Klis et al. 1990) and 4U 1705−44 (van der Klis 1989).
For KS 1731–260, Muno et al. (2000) connected the position in the color-color diagram with both the X-ray spectral properties during the bursts and the presence of burst oscillations. In the island state, KS 1731–260 showed longer decay timescales, larger fluences, no evidence for radius expansion, and no burst oscillations. On the banana branch, the bursts were shorter, the fluences were smaller, and radius expansion episodes (where the emitting region expands by a factor of 2.5–5.2) and burst oscillations were present.

In this paper we present an overview of the spectral and burst oscillation properties of 21 bursts in 4U 1728–34. We particularly investigate the relation between oscillation characteristics and radius expansion characteristics of the bursts. We also connect our results to the position of the source in the color-color diagram when the bursts took place.

2. OBSERVATIONS AND DATA ANALYSIS

In this analysis we use data obtained with RXTE’s Proportional Counter Array (PCA; for more instrument information, see Zhang et al. 1993). To prevent breakdown events, the voltage of the PCA was lowered on three occasions, leading to four periods of a different voltage called “gain epochs.” We study bursts occurring in two RXTE data sets. One set (observation program 10073) took place during gain epoch 1 (before 1996 March 21) and one (observation program 20083) during gain epoch 3 (between 1996 April 15 and 1999 March 22). We find a total number of 21 bursts. In the data that we analyzed, all five detectors of the PCA were operational. All bursts are listed in Table 1. The start times listed in Table 1 are the times when the rise in count rate, caused by the burst, triggered the Experiment Data System (EDS).

2.1. Spectral Analysis

We use the Standard 2 mode, which has a 16 s time resolution and 129 energy channels, to analyze the spectral properties of 96 s of persistent emission just before each burst. To study the spectral properties during the bursts, we use a burst trigger mode that has 64 energy channels and a time resolution of 8 ms. We determine a spectrum every 0.25 s. We correct each spectrum for background and dead time using the methods supplied by the RXTE team. We fit the spectra between 2.8 and 20 keV. For the fits we implement a systematic error of 1%. We fix the hydrogen column density, \( N_H \), to the value of \( 2.5 \times 10^{22} \) atoms cm\(^{-2}\) (Hoffman et al. 1976; Grindlay & Hertz 1981; Foster et al. 1986; Di Salvo et al. 2000).

The spectra of the persistent emission were fitted with an exponentially cutoff power law defined as \( N_{\lambda} E^{-\Gamma} \exp(-E/kT) \), where \( E \) is the photon energy, \( \Gamma \) is the power-law index, \( N_{\lambda} \) is the cutoff power-law normalization, and \( kT \) is the cutoff energy. To this we add a Gaussian line with a fixed width (\( \sigma = 0.1 \) keV) and energy (6.5 keV) as observed previously (see Di Salvo et al. 2000). This line could be due to iron emission. For the epoch 1 data, eight spectra have a reduced \( \chi^2 \), \( \chi^2/\text{degrees of freedom (dof)} < 1.6 \), and four spectra (the four with the lowest spectral index, all \( \sim 1 \)) have a \( \chi^2/\text{dof} \) around 2.2 with 49 degrees of freedom. The fits are generally better for the data from epoch 3 (\( \chi^2/\text{dof} < 1.2 \) with 42 degrees of freedom), even for spectra as hard or harder than seen in epoch 1, presumably due to better calibration in epoch 3.

When we fit the burst spectra, we model the total burst emission by a component equal to that of the persistent emission (which is fixed during the burst) plus a single blackbody component to describe the net burst emission. The bolometric blackbody flux, blackbody temperature,
blackbody radius at 4.3 kpc (see Foster et al. 1986), and $\chi^2$/dof of four representative bursts are shown in Figure 1. The fits generally have a $\chi^2$/dof below about 2 with 26 (epoch 1) or 23 (epoch 3) degrees of freedom; however, sometimes it goes up to about 3. We note that in some of the bursts that show radius expansion (see below), the $\chi^2$/dof peaks during the increase/decrease phase of the radius (see, e.g., bursts 21 and 9 in Fig. 1; this also occurs in bursts 1, 2, 7–11, and 20). It seems that the spectra deviate from simple Planckian functions when the radius varies rapidly (see also Lewin et al. 1993). We note that there are alternative methods (Sztajno et al. 1986) to handle the spectral analysis during bursts. We picked the commonly used method described above as the aim of our paper is only to provide the homogeneous description of all burst properties for the purpose of correlating with the location in the color–color diagram (see below) and not to do detailed spectral modeling.

When a burst undergoes a radius expansion episode, the luminosity $L$ stays constant and is equal to the Eddington luminosity, $L_{\text{Edd}}$ (modulo gravitational redshift effects with changing radius). Because $L \propto R^2 T_{\text{eff}}^4$, with $R$ the radius of the photosphere and $T_{\text{eff}}$ the effective temperature, when $R$ increases, $T_{\text{eff}}$ must decrease. Bursts 1, 2, 7–12, 20, and 21 clearly show this rise in blackbody radius and simultaneous dip in blackbody temperature. Bursts 4–6 have a peak flux comparable to that of these radius expansion bursts (see Table 2) and therefore might be expected to show some evidence of radius expansion as well. Indeed, burst 6 shows a clear bump in radius accompanied by a slight dip in temperature (Fig. 1), and bursts 4 and 5 have only one 0.25 s point were the radius peaked and the temperature dipped. Because the effects are marginal, hereafter we shall count those bursts as having no radius expansion. Bursts 13–18 show a gradual increase in blackbody radius for the entire duration of the burst but no simultaneous decrease in blackbody temperature. This is not classical radius expansion but might be either a real increase in the X-ray burning area (see, e.g., Kong et al. 2000) or an effect similar to that seen just after the radius contraction phase of bursts 8–12 (see below).

Bursts 8–12 show an unexpected spectral behavior (see burst 9 in Fig. 1). After the radius contraction phase, the blackbody radius reaches a minimum value followed by an increase. This behavior has previously been seen in bursts from several other sources (e.g., Hoffman, Cominsky, & Lewin 1980; Tawara et al. 1984; van Paradijs et al. 1990; Kaptein et al. 2000), although we note that the durations of those bursts were all long (>60 s). The behavior could perhaps be due to a spectral hardening effect caused by electron scattering in the neutron star atmosphere, which depends mainly on the ratio $L/L_{\text{Edd}}$ (see for a discussion Kaptein et al. 2000). Kaptein et al. (2000) try to correct the temperature and radius for a burst in 1RXS J171824.2–402934 and find that when corrected the increase in radius after the minimum is substantially less (however, the effect does not disappear after correction).

From the spectral fits of the burst and the persistent emission, we can determine the classical burst parameters such as the maximum flux (bolometric blackbody flux plus the persistent emission integrated between 0.01–100 keV; $F_{\text{peak}}$), the blackbody temperature at 10% of the Eddington flux ($kT_{\text{b,10}}$), the rise time ($t_{\text{rise}}$), and the fluence ($E_b$). As an indicator of the temperature of a burst, we use the temperature in the time bin closest to 10% of the Eddington flux in Figure 1. The Eddington flux, $F_{\text{Edd}}$, is defined by the highest peak flux from all the radius expansion bursts (i.e., that of burst 9: $12.6 \times 10^{-8}$ ergs cm$^{-2}$ s$^{-1}$; at a distance of 4.3 kpc and assuming that the burst emission is isotropic, this leads to $L_{\text{Edd}} = 2.79 \times 10^{38}$ ergs s$^{-1}$). To determine $E_b$,

### Table 2

<table>
<thead>
<tr>
<th>Burst Number</th>
<th>$F_{\text{peak}}$ ($10^{-8}$ ergs s$^{-1}$ cm$^{-2}$)</th>
<th>$E_b$ ($10^{-7}$ ergs cm$^{-2}$)</th>
<th>$kT_{\text{b,10}}$ (keV)</th>
<th>$t_{\text{rise}}$ (s)</th>
<th>$\gamma$</th>
<th>$\alpha$</th>
<th>$t_{\text{rise}}$ (s)</th>
<th>Radius Expansion</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10.0(1)</td>
<td>5.3(2)</td>
<td>1.53(5)</td>
<td>5.8(1)</td>
<td>0.089(4)</td>
<td>&gt;33</td>
<td>0.41</td>
<td>Y</td>
</tr>
<tr>
<td>2</td>
<td>10.4(1)</td>
<td>5.35(2)</td>
<td>1.42(5)</td>
<td>5.6(1)</td>
<td>0.086(3)</td>
<td>&gt;32</td>
<td>0.47</td>
<td>Y</td>
</tr>
<tr>
<td>3</td>
<td>6.3(1)</td>
<td>2.70(1)</td>
<td>1.59(5)</td>
<td>4.9(1)</td>
<td>0.153(6)</td>
<td>&gt;84</td>
<td>1.28</td>
<td>N</td>
</tr>
<tr>
<td>4</td>
<td>9.5(1)</td>
<td>4.77(2)</td>
<td>1.39(5)</td>
<td>5.5(1)</td>
<td>0.097(4)</td>
<td>&gt;29</td>
<td>0.41</td>
<td>N*</td>
</tr>
<tr>
<td>5</td>
<td>9.8(1)</td>
<td>4.71(2)</td>
<td>1.41(5)</td>
<td>5.3(1)</td>
<td>0.100(4)</td>
<td>&gt;23</td>
<td>0.41</td>
<td>N*</td>
</tr>
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<td>1.44(5)</td>
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<td>0.089(3)</td>
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<td>0.44</td>
<td>N*</td>
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<td>1.57(5)</td>
<td>5.0(1)</td>
<td>0.079(3)</td>
<td>&gt;2.7</td>
<td>0.50</td>
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</tr>
<tr>
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<td>5.11(2)</td>
<td>1.71(5)</td>
<td>5.0(1)</td>
<td>0.072(3)</td>
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<td>0.47</td>
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</tr>
<tr>
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<td>7.46(4)</td>
<td>1.73(4)</td>
<td>6.2(1)</td>
<td>0.050(3)</td>
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<td>1.28</td>
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<td>7.48(4)</td>
<td>1.71(4)</td>
<td>6.8(1)</td>
<td>0.053(3)</td>
<td>&gt;15</td>
<td>1.47</td>
<td>Y</td>
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<tr>
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<td>7.09(3)</td>
<td>1.66(5)</td>
<td>6.2(1)</td>
<td>0.060(3)</td>
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<td>6.2(1)</td>
<td>0.055(3)</td>
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<td>3.84(2)</td>
<td>1.36(4)</td>
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<td>0.121(1)</td>
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<td>1.03</td>
<td>N</td>
</tr>
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<td>2.29(4)</td>
<td>1.54(5)</td>
<td>5.5(2)</td>
<td>0.18(1)</td>
<td>&gt;119</td>
<td>1.38</td>
<td>N</td>
</tr>
<tr>
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<td>6.7(1)</td>
<td>2.95(1)</td>
<td>1.51(5)</td>
<td>5.0(1)</td>
<td>0.14(1)</td>
<td>&gt;5</td>
<td>0.56</td>
<td>N</td>
</tr>
<tr>
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<td>3.06(2)</td>
<td>1.41(5)</td>
<td>5.5(1)</td>
<td>0.15(1)</td>
<td>&gt;100</td>
<td>0.72</td>
<td>N</td>
</tr>
<tr>
<td>17</td>
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<td>2.23(2)</td>
<td>1.49(5)</td>
<td>6.2(1)</td>
<td>0.21(1)</td>
<td>&gt;89</td>
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</tr>
<tr>
<td>18</td>
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<td>3.22(1)</td>
<td>1.51(5)</td>
<td>5.5(1)</td>
<td>0.12(1)</td>
<td>&gt;51</td>
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<tr>
<td>19</td>
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<td>1.24(1)</td>
<td>1.66(5)</td>
<td>2.3(1)</td>
<td>0.12(1)</td>
<td>&gt;44</td>
<td>0.31</td>
<td>N</td>
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<td>1.60(4)</td>
<td>5.0(1)</td>
<td>0.062(2)</td>
<td>&gt;20</td>
<td>0.53</td>
<td>Y</td>
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<tr>
<td>21</td>
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<td>5.23(2)</td>
<td>1.56(5)</td>
<td>5.4(1)</td>
<td>0.066(3)</td>
<td>&gt;10</td>
<td>0.31</td>
<td>Y</td>
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</tbody>
</table>

Notes.—Listed for each burst are the burst number, the maximum flux ($F_{\text{peak}}$), the fluence ($E_b$), the temperature at 10% of the Eddington flux ($kT_{\text{b,10}}$), the standard burst parameters $\gamma = [F_{\text{pers}}/(F_{\text{peak}} - F_{\text{pers}})]$, $\tau = [E_b/(F_{\text{peak}} - F_{\text{pers}})]$, and a lower limit (because of South Atlantic Anomaly passages and Earth occultations) for $z = [F_{\text{pers}}(E_b/\Delta t)]$, the rise time ($t_{\text{rise}}$), and whether or not the burst shows radius expansion. For radius expansion terms marked with an asterisk (*), see § 2.1.
Fig. 1.—Results of the spectral fitting during the burst for four representative bursts (bursts 6, 9, 18, and 21). Plotted from top to bottom are the bolometric blackbody flux, the blackbody temperature, the blackbody radius (at 4.3 kpc) and the reduced $\chi^2$. Burst 21 shows classical radius expansion, burst 6 shows a hint of classical radius expansion (see §2.1), burst 9 shows radius expansion with unusual radius variations (see §2.1), and burst 18 shows no classical radius expansion.
Fig. 2.—Atlas of burst oscillations in 4U 1728−34. Shown are time-overlapping dynamic power spectra and associated PCA light curves (top frames) and fractional rms amplitudes of the oscillations (bottom frames). Arrows indicate 97.5% confidence upper limits. The first five bursts plotted (1, 2, 7, 20, and 21) are the radius expansion bursts. Burst sequential numbers are indicated.
we sum the flux from the start of the burst until the end of the available data. To compensate for the missing fluence at the end of the burst (since the burst flux decays exponentially, it finishes at infinite times), we fit the burst tail with an exponential function that we integrate from the end of the trigger file to infinity. We calculate the standard burst parameters (see, e.g., Lewin et al. 1993) \( \gamma = F_{\text{pers}}/(F_{\text{peak}} - F_{\text{pers}}) \), where \( F_{\text{pers}} \) is the persistent flux just before the burst, \( \tau = E_b/(F_{\text{peak}} - F_{\text{pers}}) \), and a lower limit (because of South Atlantic Anomaly passages and Earth
occultations) for $\alpha [= F_{\text{pers}}/(E_b/\Delta t)$, where $\Delta t$ is the time since the previous burst]. To determine the rise time, $t_{\text{rise}}$, we use the PCA light curve over the full PCA energy band with a time resolution of 0.0312 s (see Fig. 2). We define $t_{\text{rise}}$ as the time for the burst to increase from 25% to 90% of the peak rate. All burst parameters are shown in Table 2.

We can compare our values of $F_{\text{peak}}$ with the peak bolometric flux found by Franco (2001; see also our note added
to the present manuscript) for the same set of bursts. Although Franco does not include the persistent emission in her listed values and extracts spectra of 0.125 s instead of the 0.25 s that we use, the two sets of results are in agreement.

The profile of burst 19 deviates strongly from all the other bursts (see Fig. 3). About 15 s before the burst really goes off, the flux goes up, and 9 s before the burst rise, a small precursor occurs. The burst itself has a small fluence and is extremely short ($\tau = 2.0$ s) compared to the other
bursts (τ > 4.3 s). Including the preburst rise, emission increases the fluence by only ~ 30%, so it remains low.

### 2.2. Burst Oscillations

To get a first indication of which bursts show oscillations, we made Leahy normalized power spectra (Leahy et al. 1983) starting a few seconds before the burst with a Nyquist frequency of 2048 Hz and a frequency resolution of 0.25 Hz. We used a PCA data mode with a 125 µs time resolution and no energy resolution (the PCA is sensitive in the 2–60 keV range). We determine if there is any power between 360 and 365 Hz (based on previous results by Strohmayer et al. 1998b) that is more significant than 3σ (single trial). We find oscillations in 15 out of the 21 bursts. These preliminary detections were confirmed in our further analysis (see below).

We then examined the bursts with oscillations more closely. We made Leahy normalized dynamical power spectra starting about 4 s before the rise and extending to about 12 s after the rise. The dynamical power spectrum is composed of individual power spectra, each covering a 4 s interval. These intervals overlap, each new interval starting 0.125 s later than the previous one, increasing the time resolution at the expense of introducing correlations. We initially looked for oscillations between 300 and 400 Hz but found no evidence for oscillations outside the 360–365 Hz interval. We show the dynamical power spectra between 360 and 365 Hz for the bursts that show oscillations in Figure 2. For each individual power spectrum, there are 21 frequency bins between 360 and 365 Hz. Due to the overlaps, adjacent power spectra are correlated; after each 4 s, the power spectra become uncorrelated. In a dynamical power spectrum with a total duration of 16 s, there are four independent power spectra, which leads to a total of 84 (21 × 4) independent powers. For clarity we plot only those powers above a value of 9.2, the 99% confidence detection level for a single trial. In each plot about one independent power can be expected to exceed this level due to only Poisson noise fluctuations. Such a power fluctuation can show up in several adjacent power spectra. In each plot we include the PCA light curve over the full PCA energy band.

The light curve and power spectra are aligned such that each point in the dynamical power spectrum represents a power spectrum taken over 2 s before and 2 s after the corresponding point in the light curve.

For the four strongest frequency tracks (4, 5, 14, and 17), we list the frequency shift and frequency endpoint of the tracks seen in Figure 2 in Table 3. We note that these values might be influenced by noise powers (on average, one per plot; see above) accidentally situated near the beginning or end of a frequency track.

Because the frequency of the oscillation drifts during the 4 s interval for which each power spectrum is computed, the power spreads over a number of frequency bins. To compute the total power of the oscillation for each power spectrum, we first find the highest power, \( P_{\text{max}} \), between 360 and 365 Hz. We then determine the Poisson level, \( P_{\text{pois}} \), by averaging between 1000 and 1500 Hz and add up all powers \( P_{\text{tot}} \) above the Poisson level in an interval of 4 Hz around the frequency bin containing \( P_{\text{max}} \). As the oscillation signal is deterministic, the error in the power of each frequency bin is equal to \( P_{\text{pois}} \), so the error in the total power is obtained by quadratically adding these powers over the 4 Hz interval. From the resulting total oscillation power we calculate the rms fractional amplitude plotted in the bottom frames of Figure 2. We plot the rms fractional amplitude only when the corresponding \( P_{\text{max}} \) is larger than 9.2 and the corresponding \( P_{\text{tot}} \) differs more than 1σ from 0. When this is not the case, we calculate an upper limit in the same way as for the bursts that show no oscillations (see below).

For the bursts that show no significant oscillations, we perform an identical dynamic power spectral analysis as above. No significant oscillations are present. We add up all powers above the Poisson level between 360 and 365 Hz, \( P_{360–365} \), calculate the 1σ error in this power in the same way as for \( P_{\text{tot}} \) (see above), and use this to obtain a 97.5% confidence upper limit on \( P_{\text{tot}} \) (\( P_{\text{u.l.}} = P_{360–365} + 2 \times \)error).
3. RESULTS

Previous studies of spectral burst parameters in 4U 1728–34 have been made with HEAO 1 (Hoffman et al. 1979), Einstein (Grindlay & Hertz 1981), EXOSAT (Foster et al. 1986), ASTRON Kaminker et al. (1989), and Ginga (Day & Tawara 1990). The most extensive study was done with SAS 3 by Basinska et al. (1984) and included 96 bursts detected in ~48 days of observations between 1976 March and 1979 March. In Figure 4 we plot our values of $E_b$ versus $F_{\text{peak}} - F_{\text{pers}}$ together with those of Basinska et al. (1984). We have also included two points obtained with Ginga (Day & Tawara 1990), one with HEAO 1 (Hoffman et al. 1979), and one with ASTRON (Kaminker et al. 1989). Basinska et al. (1984) observed a strong, approximately linear, correlation between $E_b$ and $F_{\text{peak}} - F_{\text{pers}}$ at low $E_b$ levels; at higher $E_b$ values there was a turnover at $7 \times 10^{-8}$ ergs cm$^{-2}$ s$^{-1}$, and they suggested that the source had reached a critical luminosity. In our sample the strong correlation extends to $F_{\text{peak}} - F_{\text{pers}}$ values up to $12 \times 10^{-8}$ ergs cm$^{-2}$ s$^{-1}$. We do not observe a turnover, and $F_{\text{peak}} - F_{\text{pers}}$ clearly exceeds $7.5 \times 10^{-8}$ ergs cm$^{-2}$ s$^{-1}$. We note that the measured values of $F_{\text{peak}} - F_{\text{pers}}$ depend on the size of the used time bins. However, this cannot account for the much larger $F_{\text{peak}} - F_{\text{pers}}$ that we observe.

We find $\tau$ ranging between 4.7 and 6.8 s, with the exception of burst 19, which has $\tau = 2.3$ s. Excluding the so-called super burst (Basinska et al. 1984; see Fig. 4), which has $\tau = 19.9$ s, Basinska et al. (1984) found $\tau$ to range between 5.1 and 12.3 s and that the rise times were, with one exception, all short ($<5$ s); this is consistent with our results.

We determine the positions of the bursts in the color-color diagram produced by Di Salvo et al. (2001) by taking the weighted average in hard and soft color for 10 16 s points from Standard 2 data prior to the burst. The hard color in Di Salvo et al. (2001) is defined as the count rate in the energy band 9.7–16.0 keV divided by the rate in the energy band 6.4–9.7 keV and the soft color as that in the energy band 3.5–6.4 keV divided by the rate in the energy band 2.0–3.5 keV. In burst 11, due to Earth occultation, only four 16 s points were available prior to the burst, leading to larger errors in the colors. The position of each burst in the color-color diagram is shown in Figure 5.

For each burst, we find the rank number as used by Di Salvo et al. (2001) to mark the position in the color-color diagram. The soft color, hard color, rank number, and count rate in the 2.0–16.0 keV band are listed in Table 1. To study the correlation between the various burst spectral properties and position in the color-color diagram, we plot several parameters versus their rank number in Figure 6. $E_b$ and $F_{\text{peak}}$ (and thus $\gamma$) clearly correlate with the position in the color-color diagram, both decreasing with rank number (while $\gamma$ increases). Although $kT_{\text{e,1}}$ and $\tau$ change only marginally, they also appear to decrease with rank number.

In the right-hand panel of Figure 5, we mark the bursts with radius expansion with open symbols. The bursts with radius expansion that show the unusual radius variations described in § 2.1 are marked with open diamonds. All the bursts in the island state, some of the bursts on the lower banana, and none of the bursts on the upper banana show radius expansion. In the left-hand panel of Figure 5, the bursts with oscillations are marked with filled circles, the ones without with pluses. The five bursts with rank numbers below 7 (island state) show no oscillations. These are precisely bursts 8–12, which exhibited the unusual radius variations (see § 2.1). The bursts with rank numbers greater than 9 (the edge of the island state and the banana branch) all show oscillations (except the weak burst 3 at rank number 14, whose oscillation upper limit is consistent with the oscillation strength seen in the other bursts). These oscillating bursts therefore include all bursts with radius expansion that had no unusual radius variations, as well as all bursts (except burst 3) without radius expansion.

Upper limits indicate that oscillations in the island state, if any, really have a lower rms than those on the banana branch and are not just harder to detect due to lower count rates there. To demonstrate this, we find the rms fractional amplitude corresponding to the largest $P_{\text{rms}}$ or $P_{\text{u.l.}}$ in each burst. From this we exclude the first 4 s of Figure 2 where the resulting rms fractional amplitudes are systematically high because the summed count rate over 4 s contains a fraction of counts from the persistent emission. The peak rms fractional amplitudes and upper limits are plotted in Figure 7. The higher peak rms fractional amplitudes tend to occur at higher rank numbers.

The dynamical power spectra of the bursts with oscillations (Fig. 2) show several different types of frequency tracks. A remarkable difference can be seen between the frequency tracks of the bursts with oscillations with radius expansion (1, 2, 7, 20, and 21) and those without (4–6 and 13–19). In the first group, with one exception (burst 21),...
oscillations appear only after the burst has reached its maximum flux, whereas in the second group the oscillations always appear right at the start of the burst. Note that for burst 6, while we see the oscillations at the start of the burst, they appear later than in the other bursts with early oscillations. Burst 6 is also the burst that in its group has the strongest hint of radius expansion.

Previously, all oscillations observed in the tails of bursts appeared after the contraction phase of a radius expansion episode (Smith et al. 1997; Muno et al. 2000). Here we observe tail oscillations both in bursts with (e.g., burst 1) and without (e.g., burst 17) radius expansion. All bursts without radius expansion exhibited oscillations in the burst rise; the radius expansion bursts with oscillations (except burst 21) did not. So, in radius expansion bursts, as reported before, the oscillations appear after radius "touchdown" at the end of the radius expansion phase, but contrary to other sources (4U 1636–54, Strohmayer et al. 1998c; KS 1731–260, Muno et al. 2000), in 4U 1728–34 there is a strong tendency for them to be entirely undetectable in the burst rise. Remember that the gray-scale power amplitudes in Figure 2 refer to the 4 s around the point where they are plotted.

Bursts 4, 5, and 17 show a "complete" frequency track, where in about 10 s the frequency rises by $\sim 3.5$ Hz before converging asymptotically to $\sim 364$ Hz. The initial rise in frequency seems to be steeper in burst 17 than in the other two. In all other bursts it seems that we observe only part of a full track such as seen in bursts 4, 5, and 17. The oscillations in these bursts always show up in the time frequency position where one would expect them based on the shape of the frequency track in either bursts 4 and 5 or burst 17. We do not observe frequency decreases such as seen in one burst in 4U 1636–53 (Miller 2000; Strohmayer 1999) and one burst in KS 1731–260 (Muno et al. 2000).

4. DISCUSSION

There have been several previous studies linking burst parameters to inferred mass accretion rate. Some studies used the persistent flux as an indicator for mass accretion rate (e.g., EXO 0748–676, Gottwald et al. 1986; 4U 1608–53, Murakami et al. 1980; van Paradijs, Penninx, & Lewin 1988). However, studies of the kilohertz QPOs and timing features at low frequency have shown that for the LMXBs the position in the color-color diagram is a better correlator to the timing properties and hence may be a better indicator of mass accretion rate than the persistent flux (Hasinger & van der Klis 1989; for a review see van der Klis 2000). For 4U 1636–52 and 4U 1705–44, it was shown earlier that the correlation between burst parameters $kT_\text{e}$ and $\tau$ and position of the source in the color-color diagram was strong, while the correlation with the persistent flux was lacking (van der Klis et al. 1990). In 4U 1728–34 we find no preference for the position in the color-
FIG. 6.—Plotted vs. rank number are the fluence ($E_b$), the peak flux ($F_{peak}$), the blackbody temperature at 10% of the Eddington flux ($kT_{0.1}$), $\tau$ [$=E_b/(F_{peak} - F_{pers})$], $\gamma$ [$=F_{pers}/(F_{peak} - F_{pers})$], and the rise time ($t_{rise}$). The short burst (No. 19) with $\tau = 2.1$ s was excluded from the $\tau$-plot; it was located at rank No. 15. Two points at rank No. 5 coincide in the top frame.

FIG. 7.—The rms fractional amplitude of the burst oscillations during each burst plotted vs. rank number.

color diagram over the persistent flux as a correlator with the burst spectral properties as there was with properties of the kilohertz QPOs (Méndez & van der Klis 1999) and with properties of several low-frequency features (Di Salvo et al. 2001). Perhaps this is due to the relatively large intrinsic scatter in the burst parameters. In this work we use the position in the color-color diagram, as in view of the results

<table>
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<td>A COMPARISON BETWEEN 4U 1728 – 34 AND KS 1731 – 260</td>
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<td>PARAMETER</td>
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<td>$\tau$ (s)</td>
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<td>$F_{peak}$ ($10^{-8}$ ergs s$^{-1}$ cm$^{-2}$)</td>
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<td>$E_b$ (in $10^{-7}$ ergs cm$^{-2}$)</td>
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**Notes.**—Changes in burst properties from the island state to the banana branch for both 4U 1728 – 34 and KS 1731 – 260. Listed are $\tau$, $F_{peak}$, $E_b$, the occurrence of burst oscillations, and the occurrence of radius expansion. Also shown is whether the bursts show the characteristics of unstable pure He or mixed H/He burning. The arrows between island and banana for 4U 1728 – 34 indicate a smooth transition between the island state and the banana branch. The arrow between Y and N for radius expansion in the banana state of 4U 1728 – 34 indicates the presence of radius expansion in the lower banana and its absence in the upper banana. For the unusual radius variation denoted with an asterisk (*), see § 2.1.
for other sources (see above) we expect this to be the more robust correlator.

We now compare our results with those recently obtained for KS 1731−260 by Muno et al. (2000). In Table 4 we compare several properties of KS 1731−260 and 4U 1728−34. KS 1731−260 showed only two distinct states, the island state and the banana branch, with no data covering the transition between these two states. The bursts in the island state were longer (τ ≈ 15 s) than those on the banana branch (≈ 7 s). The peak flux was slightly lower (≈ 4 × 10−8 ergs cm−2 s−1) in the island state than on the banana branch (≈ 5 × 10−8 ergs cm−2 s−1), and $E_b$ was higher (≈ 7 × 10−7 ergs cm−2) in the island state than on the banana branch (≈ 4 × 10−7 ergs cm−2). Radius expansion bursts were observed on the banana branch but not in the island state.

In 4U 1728−34, contrary to the case of KS 1731−260, we observe a smooth transition between the island state and the banana branch. Di Salvo et al. (2001) found that power spectra with rank numbers 1−11 are typical of the island state, number 14 corresponds to the lower banana, and number 19 to the upper banana. We find that from island to banana τ changes only marginally, from ≈ 6 s in the island state to ≈ 5 s on the banana branch. Another source for which τ is about constant (and also short, with τ = 4.2 ± 1.2) over a wide range of $F_{\text{peak}}$ and $E_b$ (and we know that in 4U 1728−34, $F_{\text{peak}}$ and $E_b$ depend on rank number) is 4U 1735−44 (Lewin et al. 1980). However, most sources show the same behavior as KS 1731−260; namely, τ is several tens of seconds at low inferred mass accretion rate and about 5 s at high inferred mass accretion rate (e.g., EXO 0748−676, Gottwald et al. 1986; 4U 1636−53, van der Klis et al. 1990; 4U 1705−44, van der Klis 1989). We note that a previous study of 4U 1728−34 by Basinska et al. (1984) did show a larger range in τ (5.1−12.3 s).

Another difference with KS 1731−260 is that in 4U 1728−34 the bursts in the island state show radius expansion (albeit with unusual radius variations) and have a higher $F_{\text{peak}}$. As the source moves from the lower toward the upper banana, the radius expansion episodes disappear, and $F_{\text{peak}}$ becomes smaller (see Figs. 5 and 6). The sources EXO 0748−676 (Gottwald et al. 1986) and 4U 1705−44 (Langmeier et al. 1987), like KS 1731−260 but contrary to 4U 1728−34, both show higher peak fluxes at higher inferred mass accretion rates. The fluence in 4U 1728−34 does show a similar behavior to KS 1731−260: it changes gradually from about 7 × 10−7 ergs cm−2 in the island state to ≈ 3 × 10−7 ergs cm−2 on the banana branch (see Fig. 6).

In KS 1731−260 oscillations were found only to occur on the banana branch and not in the island state (Muno et al. 2000). For 4U 1728−34 we also observe that burst oscillations appear at the higher inferred mass accretion states (see Fig. 5). Because we see a gradual transition between island and banana state, we can ascertain that oscillations are already detectable when the power spectrum of the persistent emission (Di Salvo et al. 2001) still indicates an island state (see above).

Cumming & Bildsten (2000) explain the presence/absence of burst oscillations in KS 1731−260 in terms of the absence/presence of an H-rich region. They show that if an oscillation is generated near the burning layers, it can escape coherently from a helium-rich region but not from an H-rich region. The bursts in KS 1731−260 show characteristics of pure He ignition (short duration, radius expansion, and high peak flux) when the source is in the banana state and of mixed H/He ignition when the source is in the island state, and oscillations occur only when there is pure He ignition. However, in 4U 1728−34 in the island state we observe that the burst oscillations disappear while the bursts still have all characteristics of pure He ignition.

In KS 1731−260 the presence of burst oscillations and radius expansion were nearly perfectly correlated: all but one of the bursts with burst oscillations also had radius expansion, and none of the bursts without oscillations showed radius expansion. In contrast, in 4U 1728−34 radius expansion bursts occur below a certain inferred mass accretion rate level and burst oscillations above another level, and in the middle both phenomena occur in the same bursts. It is striking that the bursts with radius expansion that show the unusual radius variations described in § 2.1 are exactly the bursts from which the oscillations are absent. We cannot from our data determine if unusual radius variations and absence of oscillations have a causal relation or are both just a characteristic of bursts occurring at low inferred mass accretion rate. Nevertheless, while there may not be a good correlation between the occurrence of radius expansion and burst oscillations, the way the radius expansion occurs may in fact be physically connected to the occurrence of oscillations. Perhaps the unusual radius variations, which occur only in our most energetic bursts, are an indication that the magnetic fuel containment near the magnetic poles (a possible explanation for late burst oscillations; Miller 1999) is less efficient in stronger bursts.

So it seems that both in KS 1731−260 and in 4U 1728−34 the timing as well as the spectral parameters of the bursts depend monotonically on the position of the source in the color-color diagram. Also, both in KS 1731−260 and in 4U 1728−34, the presence/absence of the burst oscillations depends on the position in the color-color diagram in more or less the same way. However, the dependence of most of the spectral burst parameters on the position in the color-color diagram shows a clear discrepancy between the two sources, from which we are led to conclude that the correlations between spectral burst parameters and the occurrence of oscillations suggested from the KS 1731−260 data is not universal.

To summarize:

1. The burst oscillations become significantly weaker (and in fact undetectable) in the island state without the characteristics of the bursts switching from pure He to mixed H and He unstable burning, as occurs in KS 1731−260.
2. Radius expansion per se does not determine the presence or absence of burst oscillations. Both are more likely to occur at lower inferred mass accretion rates.
3. Contrary to what was noted in Muno et al. (2000) for other sources, we do observe oscillations in the tails of non-radial expansion bursts.
4. Among our bursts with radius expansion, the most energetic ones at the lowest inferred mass accretion rate, which show an unexpected spectral behavior with a double-peaked radius curve, do not show burst oscillations, while the others do.
5. Among our bursts with oscillations, the radius expansion bursts (with one exception) show no oscillations during the burst rise, whereas non-radius expansion bursts do.
As the only two sources studied until now already show remarkable differences in their behavior, further studies of correlated spectral and timing behavior of other type I X-ray bursters showing burst oscillations are necessary to come to a full understanding of just what determines whether, and if so, in which part of its profile, a burst oscillates.

Note added in manuscript.—Just before this paper was submitted, we became aware of a paper in preparation by Franco (2001) on the burst oscillations in 4U 1728—34. Where between the two papers conclusions overlap, they are consistent. To avoid confusion, we note that our definition of a “complete frequency” track is more restrictive than “a burst with oscillations in the rise and the tail” used in Franco (2001). We call a frequency track “complete” only when the oscillations are present essentially throughout the entire burst (≥ 14 s). We would like to thank Lucia Franco for her willingness to exchange manuscripts before publication.

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