A review on electrokinetically induced seismo-electrics, electro-seismics, and seismo-magnetics for Earth sciences

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Received: 15 July 2015 – Published in Solid Earth Discuss.: 18 September 2015
Revised: 23 December 2015 – Accepted: 4 January 2016 – Published: 12 February 2016

Abstract. The seismo-electromagnetic method (SEM) can be used for non-invasive subsurface exploration. It shows interesting results for detecting fluids such as water, oil, gas, \(\text{CO}_2\), or ice, and also help to better characterise the subsurface in terms of porosity, permeability, and fractures. However, the challenge of this method is the low level of the induced signals. We first describe SEM’s theoretical background, and the role of some key parameters. We then detail recent studies on SEM, through theoretical and numerical developments, and through field and laboratory observations, to show that this method can bring advantages compared to classical geophysical methods.

1 Introduction

Current methods of subsurface exploration are based on either seismic or electrical geophysical principles. The seismo-electromagnetic method (SEM) combines both approaches, with the resolution of the seismics and the sensitivity of the electromagnetic methods to the fluids. It offers a non-invasive structure characterization of the near-surface Earth from first few hundred metres up to a depth of the order of 1000 m, in terms of fluids (water, oil, gas). Therefore it is a method supporting the management of water, oil and gas resources, specially the study of hydraulic and hydrocarbon reservoirs, of geothermal or fractured reservoirs, the resource prospection in glaciated regions, and \(\text{CO}_2\) storage. SEM may characterise not only the depth and the geometry of the reservoir (Fig. 1 from Thompson et al., 2007), but also the fluid content.

It is usual to use different terms, according to the used source: seismo-electrics (SE) involves generating a seismic wave and measuring the electrical field either contained within or generated by it (Fig. 2 from Thompson et al., 2005), while electro-seismics (ES) does the opposite by injecting a large amount of current into the ground and measuring the resulting seismic energy. In this review we use the term SEM in general, and the terms SE and ES when mentioning specific studies. The electromagnetic signal related to the relative motion between the fluid and the rock matrix is called electrokinetic phenomenon. In a porous medium the electric current density, linked to the ions within the fluid, is coupled to the fluid flow (Overbeek, 1952) so that the streaming potentials are generated by fluids moving through these kinds of media (Jouniaux et al., 2009). This effect is related to the existence of an electrical double layer between the rock and the fluid, developed at the contact between the pore wall and the electrolyte. This electric double layer (Debye and Huckel, 1923) is made up of the Stern layer (Stern, 1924) where cations are adsorbed onto the surface, and the Gouy diffuse layer (Gouy, 1910) where the number of counterions exceeds the number of anions (Adamson, 1976; Davis et al., 1978; Hunter, 1981). The streaming current, due to the motion of the diffuse layer, is induced by a fluid pressure difference along the interface (second term in Eq. 2). This streaming current is then balanced by the conduction current (first term in Eq. 2), leading to the streaming potential \(V\). More details on the electric double layer are provided in the tutorial of the special issue on electrokinetics in Earth sciences by Jouniaux and Ishido (2012), with the description of the electric potential within the electric double layer.
Figure 1. Geometry of a gas reservoir (in blue) deduced from electro-seismics (from Thompson et al., 2007).

Figure 2. Electro-seismics method: an electric current is applied at the surface, and when it encounters a contrast in physical properties it induces a seismic wave which is measured at the surface (from Thompson et al., 2005).

Two kinds of SEM conversions are distinguished (Haines et al., 2003): (1) the first one is called the coseismic conversion when the electric field is contained within the seismic wave and travels at the same speed; (2) the second kind is called the interface response (IR) when a seismic wave encounters a boundary in physical properties between two media and travels at the velocity of the electromagnetic signal in the medium. This electromagnetic field can be received synchronously at multi-locations. The reader should keep in mind that (in the frequency range considered in all works analysed in this review) and in conductive media such as the soil, the electromagnetic waves are highly dispersive and strongly attenuated, and their propagation could also correctly be described—as many authors do—as electromagnetic diffusion (Løseth et al., 2006).

The second kind of conversion can be potentially used to detect contrasts in permeability in the crust (Garambois and Dietrich, 2002). A seismic source induces a seismic wave propagation downward up to the interface (Fig. 3). Because of the difference in the physical properties there is a charge imbalance that causes a charge separation on both sides of the interface. This acts as an electric dipole which emits an electromagnetic wave that travels with the speed of the light in the medium and that can be detected at the surface (Haines, 2004) (Fig. 4). The characteristic of this interfacial response is a flat event with a reversed polarity (when measuring the
horizontal electric field) at either side of the source, an amplitude which is maximum at offset half of the interface depth, and a quasi-simultaneous arrival on the electrodes. The velocity of the seismic wave propagation may be deduced by surface measurements of the soil velocity. Then the depth of the interface can be deduced by picking the time arrival of the electromagnetic wave. Of course, this procedure may not be straightforward when complex geometries are present. Usually the SE signals show low amplitudes from 100 µV to mV and suffer from low signal-to-noise ratio. Then signal processing needs filtering techniques such as those described in Butler and Russell (1993).

The SEM advantageously in detecting zones of high fluid mobility and contrasts of physical parameters as porosity, geochemical fluids, permeability at depths from a few metres to a few hundred metres (Thompson et al., 2005; Dupuis and Butler, 2006; Dupuis et al., 2007, 2009; Strahser et al., 2007, 2011; Haines et al., 2007a, b); for the characterization of permeable zones along a borehole (Mikhailov et al., 2000) and the groundwater exploration in a fractured rock aquifer (Fourie and Botha, 2001; Fourie et al., 2000). However, surface observations are difficult to use for the exploration of deep formations because of the low efficiency of the seismo-electric conversion and the attenuation within the formations.

Some field studies developed vertical SE profiles having a seismic source below the studied interface allowing for the separation of the IR from the coseismic signal (Russell et al., 1997). Borehole investigations could also detect the location of opened fractures (Hunt and Worthington, 2000), and showed that the electric noise level was reduced at depth (Dupuis et al., 2009).

Previous reviews on SEM described the electrokinetics for geophysics (Beamish and Peart, 1998), the SE monitoring of producing oilfields (Gharibi et al., 2003), several case studies in piezoelectric phenomena in geophysics and SE carried out by Russian and Israeli researchers (Neishtadt et al., 2006), the frequency dependence of streaming potential (Jouniaux and Bordes, 2012), and provided a tutorial on electrokinetics (Jouniaux and Ishido, 2012).

2 History

Seismo-electric techniques are based on electrokinetic coupling, largely studied in colloid and surface science. In Earth sciences, the SE IR was first reported by Ivanov (1939) and was called the effect of second kind or E-effect. Ivanov (1939) proposed that this effect can be induced by the streaming potential phenomenon in the moist soil. The first theoretical study on SE effect was published in 1944 by a Russian scientist (Frenkel, 1944); this work was re-published in 2005 as an outstanding historical contribution (Frenkel, 2005).

The propagation of seismic waves in a porous medium saturated with a viscous fluid is described by a theory developed by Biot (1956a, b). According to this theory the propagating waves are two dilatational waves and one rotational wave. Two kinds of dilatational waves are distinguished: the first kind corresponds to the solid and fluid moving in phase; the second kind corresponds to the solid and fluid moving out of phase. The latter propagates at a lower velocity than the former, and is referred to as the Biot slow wave. In the seismic frequency range these slow waves are dissipative and die out rapidly with distance from the source.

The streaming potential was observed by Quincke (1861), as the reciprocal of the electro-osmosis phenomenon first observed by Reuss (1809) and Wiedemann (1852). The origin of this phenomenon was explained through the existence of an electric double layer acting as a condenser (von Helmholtz, 1879; Briggs, 1928). And anomalous behaviour of the zeta-potential in dilute solutions or in small capillaries had already been explained by the effect of surface conductance by McBain et al. (1929); Urban and White (1932); Rutgers (1940), and White et al. (1941).

First attempts on the seismic-electric effect were actually ES measurements, as an electric current was injected through the Earth. The observed effect was thought to be due to changes in the resistivity of the Earth under the influence of seismic waves. A first explanation was proposed to be linked to the fluctuations in the current through the electrolytic cell because of variations of the electro-chemical conditions at the surface of the electrodes, induced by the mechanical vibrations (Thyssen et al., 1937). Then different experimental set-ups could eliminate the effect of electrode surface (Thompson, 1939); and later on, Pride (1994); Butler et al. (1996) showed that the resistivity modulation was not the relevant mechanism of the observed SE signals.

Martner and Sparks (1959) reported field measurements showing an IR generated at the base of a weathered layer, characterized by a change in seismic velocity but not necessarily associated with the top of the water table. Long and Rivers (1975) measured the electrical conductivity variations induced by seismic excitation. The measured an electric signal, of 100 to 300 µV (mm s\(^{-1}\))\(^{-1}\), correlated most strongly with the Rayleigh waves. However, the estimate of the resistivity change was only 0.015 %, so that the authors concluded that although the physical processes generating the signal was not elucidated, it was undoubtedly related to the condition of water in the pore spaces and the state of stresses of the rock matrix. Russell et al. (1997) measured also an IR signal generated at a boundary between road fill and glacial till at about a depth of 3 m using a seismic source set in a borehole below this boundary, at a depth of 5.5 m (at Haney, Canada). The SE data showed higher frequency than the seismic one, attributed to the fact that the SE wave is propagating with much less attenuation. These authors also characterized the SE signals induced in a zinc-rich ore body at the Lynx mine (British Columbia, Canada), and interpreted them to have been caused by microfracturing. The electromagnetic field was measured in the frequency domain, up to 5 MHz. The authors showed high-frequency content of the signals.
with oscillations at 1.3 MHz. It was concluded that these results were consistent with results from Russian researchers proposing that each type of ore/mineral has distinctive spectral peaks.

In the 1970s, laboratory experiments were performed to better understand the effect of salinity, of moisture, of porosity, and of frequency on the coseismic signal (Parkhomenko and Tsze-San, 1964; Parkhomenko and Gaskarov, 1971; Gaskarov and Parkhomenko, 1974; Migunov and Kokorev, 1977), which are detailed below and compared to more recent studies.

The generalization of Biot Theory including the electrokinetic effects was described by Neve and Yeatts (1989), based on the coupling equations of Onsager (1931). At the same time in 1993/94 successful field experiments of SE conversion detected from an interface gas–water at a depth of 300 m were published by Thompson and Gist (1993), and the theory for the coupled electromagnetism and poroelasticity was developed by Pride (1994). Later, the Pride study was extended by including in the equations the effects of anisotropy, by Pride and Haartsen (1996). These works lead to further developments in this method.

3 Theoretical background

We present in this section how different authors contributed to derive the coupling equations from the Biot theory and the Maxwell equations; then we detail further developments on the equivalent electric dipole, and on the transfer function between seismic and electromagnetic energy.

3.1 Frequency-dependence electrokinetics

The electrokinetic effect is due to fluid flow in porous media because of the presence of ions within the fluid which can induce electric currents when water flows. The general equation coupling the different flows is as follows:

\[ \mathbf{J}_i = \sum_{j=1}^{N} \mathcal{L}_{ij} \mathbf{X}_j, \]  

(1)

which links the forces \( \mathbf{X}_j \) to the macroscopic fluxes \( \mathbf{J}_i \), through transport coupling coefficients \( \mathcal{L}_{ij} \) (Onsager, 1931). Notice that boldface is used to denote vector quantities.

Considering the coupling between the hydraulic flow and the electric flow, assuming a constant temperature, and no concentration gradients, the electric current density \( \mathbf{J}_e \) [A m\(^{-2}\)] can be written as the following coupled equation (Allègre et al., 2012):

\[ \mathbf{J}_e = -\sigma_0 \nabla V - \mathcal{L}_{ek} \nabla \mathbf{P}, \]  

(2)

where \( \mathbf{P} \) is the pressure that drives the flow [Pa], \( V \) is the electrical potential [V], \( \sigma_0 \) is the bulk electrical conductivity [S m\(^{-1}\)], \( \mathcal{L}_{ek} \) the electrokinetic coupling [A Pa\(^{-1}\) m\(^{-1}\)]. Thus the first term in Eq. (2) is Ohm’s law. The coupling coefficients must satisfy Onsager’s reciprocal relation in the steady state. This reciprocity has been verified on porous materials (Miller, 1960; Auriault and Strzelecki, 1981) and on other natural materials (Beddias et al., 2002).

When the electrokinetic effect is induced by seismic wave propagation, which leads to a relative motion between the fluid and the rock matrix, the electrokinetic coefficient depends on the frequency \( \omega \) as the dynamic permeability \( k(\omega) \) (Smeulders et al., 1992). The theory for the coupled electromagnetics and acoustics of porous media was developed by Pride (1994). The transport relations (Pride, 1994, Eqs. 250 and 251) are the following:

\[ \mathbf{J}_e = \sigma(\omega) \mathbf{E} + \mathcal{L}_{ek}(\omega) \left( -\nabla \mathbf{P} + \omega^2 \rho_f \mathbf{u}_f \right), \]  

(3)

\[ -i \omega \mathbf{J}_f = \mathcal{L}_{ek}(\omega) \mathbf{E} + \frac{k(\omega)}{\eta_f} \left( -\nabla \mathbf{P} + \omega^2 \rho_f \mathbf{u}_f \right), \]  

(4)

where an \( e^{-i\omega t} \) time dependence has been assumed; we keep this convention throughout the review. The electrical fields and mechanical forces which induce the electric current density \( \mathbf{J}_e \) and the fluid flow \( \mathbf{J}_f \) are, respectively, \( \mathbf{E} \) and \( (-\nabla \mathbf{P} + i \omega \rho_f \mathbf{u}_f) \), where \( \mathbf{P} \) is the pore-fluid pressure, \( \mathbf{u}_f \) is the solid displacement, \( \mathbf{E} \) is the electric field, \( \rho_f \) is the pore-fluid density, \( \eta_f \) the dynamic viscosity of the fluid [Pa s\(^{-1}\)], and \( \omega \) is the angular frequency.

The electrokinetic coupling \( \mathcal{L}_{ek}(\omega) \) describes the coupling between the seismic and electromagnetic fields and is complex and frequency-dependent (Pride, 1994; Reppert et al., 2001):

\[ \mathcal{L}_{ek}(\omega) = \]  

\[ \mathcal{L}_{ek} \left[ 1 - \frac{i \omega}{\omega_c} \frac{m}{4} \left( 1 - 2 \frac{d}{\Lambda} \right)^2 \left( 1 - i \frac{3}{2} \frac{d}{\Lambda} \sqrt{\frac{\phi \eta}{\rho_0 k_0}} \right) \right]^{-\frac{1}{2}}, \]  

(5)

where \( m \) and \( \Lambda \) are geometrical parameters of the pores (\( \Lambda \) is defined in Johnson et al., 1987, and \( m \) is in the range 4–8), and \( d \) is the Debye length. The electrokinetic coupling is an important parameter: if this coupling is zero, then there is no seismo-electric nor electro-seismic conversion. The transition frequency \( \omega_c \) defined in Biot’s theory separates the viscous and inertial flow domains and depends on the intrinsic permeability \( k_0 \) [m\(^3\)]. The transition angular frequency \( \omega_c \) is defined as (Dutta and Odé, 1983):

\[ \omega_c = \frac{\phi \eta}{\alpha_\infty k_0 \rho_f}, \]  

(6)

where \( \phi \) is the porosity, \( \alpha_\infty \) the tortuosity.

The electrokinetic coupling can not be directly quantified in the laboratory, whereas it is possible to measure the streaming potential \( C_{sd} \) induced by a pressure gradient. Both are related through (Schoemaker et al., 2008)

\[ \mathcal{L}_{ek}(\omega) = -\sigma_0 C_{sd}(\omega). \]  

(7)
So the frequency dependence of the streaming potential coefficient has been studied (Packard, 1953; Cooke, 1955; Groves and Sears, 1975; Sears and Groves, 1978; Chandler, 1981; Reppert et al., 2001; Schoemaker et al., 2007, 2008) mainly on synthetic samples, and recently on sand (Tardif et al., 2011), and on unconsolidated materials (Glover et al., 2012). In 1953 Packard (1953) proposed a model for the frequency-dependent streaming potential coefficient for capillary tubes, assuming that the Debye length is negligible compared to the capillary radius, based on the Navier–Stokes equation:

\[ C_{s0}(\omega) = \frac{\Delta V(\omega)}{\Delta P(\omega)} = \left( \frac{e \zeta}{\eta \sigma} \right) \left[ \frac{2}{a \sqrt{\frac{\omega \rho_i}{\eta}}} J_1 \left( \sqrt{\frac{\omega \rho_i}{\eta}} \right) e^{-i \omega t} \right], \]

where \( a \) is the capillary radius, \( J_1 \) and \( J_0 \) are the Bessel functions of the first order and the zeroth order, respectively, and \( \rho_i \) is the fluid density, and the transition angular frequency for a capillary is the following:

\[ \omega_c = \frac{\eta}{\rho_i a^2}. \]

The absolute magnitude of the streaming potential coefficient normalized by the steady-state value was calculated by Packard (1953) as follows:

\[ f(Y_a) = \frac{-2 i \sqrt{\frac{Y_a}{r}} J_1 \left( \sqrt{\frac{Y_a}{r}} a \right) e^{-i \omega t}}{Y_a \ J_0 \left( \sqrt{\frac{Y_a}{r}} a \right)}, \]

which is equal to Eq. (8), but expressed as a function of the parameter \( Y_a = a \sqrt{\frac{\omega \rho_i}{\eta}} \), the transition frequency being obtained for \( Y_a = 1 \). The real part and the imaginary part of Packard’s theoretical streaming potential coefficient (Eq. 8) was calculated for different capillary radii by Reppert et al. (2001) (Fig. 5). It can be seen that the larger the radius, the lower the transition frequency, as shown above by the different theories. The streaming potential coefficient is constant up to the transition angular frequency, and then decreases with increasing frequency.

In 2001, Reppert et al. (2001) used the low- and high-frequency approximations of the Bessel functions to propose the following formula, which corresponds to their Eq. (26) corrected with the right exponents \(-2 \) and \(-1/2\):

\[ C_{s0}(\omega) = \left( \frac{e \zeta}{\eta \sigma} \right) \left[ 1 + \left( \frac{2}{a \sqrt{\frac{\omega \rho_i}{\eta}} \left( \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} i \right)} \right)^{-2} \right]^{-1/2}, \]

with the transition angular frequency

\[ \omega_c = \frac{8 \eta}{\rho_i a^2}. \]

Figure 5. The real and imaginary part of the Packard model (Eq. 8) calculated by Reppert et al. (2001) for three capillary radii: 100 µm (continuous line), 50 µm (dashed line), 10 µm (point line) (modified from Reppert et al., 2001).

and showed that this model was not very different from the model proposed by Packard (1953).

More recently, Walker and Glover (2010) proposed a simplified equation of Pride’s development assuming that the Debye length is negligible compared to the characteristic pore size, and assuming the parameter:

\[ m = 8 \left( \frac{\Lambda}{r_{eff}} \right)^2, \]

leading to the equation:

\[ \mathcal{E}_{ek}(\omega) = \mathcal{E}_{ek} \left[ 1 - 2 i \frac{\omega}{\omega_c} \left( \frac{\Lambda}{r_{eff}} \right)^2 \right]^{-\frac{1}{2}}, \]

with \( r_{eff} \) the effective pore radius, and a transition angular frequency

\[ \omega_c = \frac{8 \eta}{\rho_i r_{eff}^2}. \]

Moreover Schoemaker et al. (2012) showed that the theoretical amplitude values of the dynamic streaming potential coefficient are in good agreement with their normalized experimental results over a wide frequency range, without assuming a frequency dependence of the bulk conductivity. More details on the frequency-dependent streaming potentials are provided by the review of Jouniaux and Bordes (2012) including a description of different experimental apparatus.

3.2 Theoretical developments

The mechanisms involved in the subsurface electrokinetic coupling have been summarized by Beamish (1999) in Fig. 6.

The coseismic field measured on the surface can be associated with surface waves, including the direct (compressional) wave and the surface/Rayleigh wave, travelling along the ground surface.
The interfacial response can be induced by (i) a first mechanism occurring in the first Fresnel zone, when a spherical $P$ wave traverses an interface directly beneath the source: this is the IR providing instantaneous arrivals across arrays of surface dipoles. This mechanism occurs at interfaces between different streaming potential coefficients. (ii) A second mechanism related to the refracted-head wave travelling along the interface, which generates an electromagnetic field providing time-dependent arrivals at arrays of surface dipoles. This mechanism occurs at interfaces with a difference in both acoustic and electrokinetic properties.

The electromagnetic field induced by an interface excited by a seismic pulse can be approximated to an electric dipole located directly under the source (Thompson and Gist, 1993). Indeed a spherical seismic wave incident on a horizontal interface induces circular regions, called the Fresnel zones, of positive and negative displacement moving outward along the interface. The first Fresnel zone is the part of the horizontal interface reached by the seismic wave within one half wavelength from the initial arrival, successive Fresnel zones being excited at later times. So that a number of electric dipoles are finally excited. As the electric field falls off with distance $r$ as $1/r^3$ for a dipole and $1/r^5$ for an octupole, the electric field from higher-order Fresnel zone can be neglected compared to the one of the first Fresnel zone (Thompson and Gist, 1993). Moreover Thompson and Gist (1993) calculated a signal-to-noise ratio for the maximum of the IR of still about 50 for an interface gas–water at a depth of 300 m for a seismic pulse centre frequency of 50 Hz.

Garambois and Dietrich (2001) calculated the electric field radiated by two interfaces at depths of 2 m and 10 m by summing the individual contributions of all dipoles contained within the Fresnel zones, which are circular surfaces of radii 3.75 and 7.07 m for depths of the interface of 2 and 10 m, respectively. The results show that the horizontal electric field has a dipolar property with a change of polarity on opposite sides of the shot point. Moreover, the maximum of the horizontal electric field decreases as the depth of the interface increases (Fig. 7).

Fourie and Botha (2001) noticed that the first Fresnel zone is large, so that the recorded signal will include the lateral variations of the interface on about 40 m distance from its centre, for an interface at 50 m depth. The ES Fresnel zones are larger than the seismic Fresnel zone, twice as large for interfaces at depths much greater than the dominant wavelength, because only the one-way distance to the interface is important, the EM wave propagating several orders of magnitude faster than the seismic waves (Fourie, 2006). By modelling an interface consisting in a ring-shaped zone between two media of different seismic velocities, Fourie and Botha (2001) calculated the horizontal electric field at a short distance from the seismic source (0.5 m). The authors showed that the amplitude of the electric field is decreasing for increasing inactive distance (the inner radius of the ring-shaped zone). They showed that when the source is a Ricker wavelet, the maximum of the electric field occurs for an inactive zone of 4 m radius (for an interface at 40 m depth), rather than for a full active ring-shaped zone. But this maximum was only about 1 % greater than the electric field calculated for the full active ring-shaped zone. So that the assumption that the IR signal is generated at a position vertically below the seismic source is rather valid. However, the lateral resolution of surface seismo-electric measurements will remain weaker than for seismics.

Dupuis et al. (2009) proposed a near field analysis of the spatial and temporal variations of the polarity and amplitude of the SE conversions observed in boreholes. They noted that the lateral extent of the seismic source at the interface is the Fresnel radius, while the vertical extent is the dominant wavelength of the compressional seismic wave. Therefore, if the electric dipoles are short in comparison to the height of the source zone, it is possible to measure the vertical electric
field within this zone, which has a reverse polarity of the field observed above and below the source zone.

The ability of the SE method to detect thin embedded layers depends on the constructive and destructive interferences of the signal induced at its bottom and its top interfaces (Grobe and Slob, 2014). The SE response from a thin fluid-saturated layer may be enhanced by the constructive interferences (Haartsen and Pride, 1997). The embedded layer needs to be thicker than half the dominant wavelength to be resolvable. Fourie (2006) showed that for both fast and slow waves (corresponding to a wavelength of about 29 and 0.8 m respectively), beds with thicknesses less than one quarter of the wavelength, result in a total response weaker than the response from the upper interface alone.

The transfer functions between the coseismic electric field, the coseismic magnetic field, and the acceleration and displacement, have been also theoretically derived, in an isotropic and homogeneous whole space (Pride and Haartsen, 1996), considering a plane-wave solution of the governing equations.

The two main cases first considered are the relation between the electric field and the displacement for the compressional waves and the relation between the magnetic field and the displacement for shear waves. The other combinations are small or zero. Indeed, the electric field associated with transverse waves does not result from a charge separation, but it is induced by the induction of the magnetic field and has a small amplitude. For the transverse mode two different polarizations exist: the SH–TE case corresponds to SH-shear waves and a horizontally polarized transverse electric mode of EM waves that are both horizontally polarized in the cross-line direction; the SV–TM case, on the other hand, consists of vertically polarized SV shear waves and a horizontally polarized transverse magnetic mode of EM waves.

Moreover, there is no magnetic field associated to compressional waves (Garambois and Dietrich, 2001).

Garambois and Dietrich (2001) studied the low frequency assumption valid at seismic frequencies, meaning at frequencies lower than Biot’s frequency separating viscous and inertial flows and gave the coseismic transfer function for low frequency longitudinal plane waves. In this case, and assuming Biot’s moduli \( C \ll H \), they showed that the SE field \( \mathbf{E} \) is proportional to the grain acceleration for longitudinal fast \( P \) waves:

\[
\mathbf{E} \simeq - \frac{C_{ek}}{\sigma_0} \rho \ddot{u} = \frac{\varepsilon \kappa}{\eta \sigma_0} \rho \ddot{u}. \tag{16}
\]

Equation (16) shows that transient seismo-electric magnitudes will be affected by the density of the fluid, the water conductivity and the zeta potential (which depends on the water pH), the dielectric constant and viscosity of the fluid.

These authors also showed that the magnetic field is proportional to the grain velocity for displacements associated to transverse SH and SV waves as follows:

\[
|\mathbf{H}| \simeq \frac{1}{F} \frac{\varepsilon \kappa}{\eta} \rho \varepsilon \sqrt{\frac{G}{\rho}} |\dot{u}|. \tag{17}
\]

In Eq. (17), \( G \) is the shear modulus of the framework and \( \rho \) the bulk density.

The definitions of the \( C \) and \( H \) moduli are those of Biot (1962). Therefore the magnetic field depends also on the density of the fluid, the zeta potential (which depends on the water pH), the dielectric constant and viscosity of the fluid, but also on the shear modulus of the framework, the bulk density and the formation factor, so indirectly on the permeability.

Recently Bordes et al. (2015) derived the transfer functions \( \psi \) for the SE field, neglecting the Biot slow waves, in the dynamic domain (as a function of frequency), associated both to compressional \( P \) waves and shear \( S \) waves:

\[
\mathbf{E}(\omega) = \psi_{p-dyn} \ddot{u}_p(\omega) + \psi_{s-dyn} \ddot{u}_s(\omega). \tag{18}
\]

For the low frequency assumption, the authors showed that

\[
E(\omega) = - C_{s0} \rho \varepsilon \left[ \left( 1 - \frac{\rho}{\rho_0} \frac{C}{H} \right) \ddot{u}_p(\omega) - i \frac{\mu}{\omega} \frac{\rho}{\rho_0} \frac{\sigma}{\sigma_0} \ddot{u}_s(\omega) \right]. \tag{19}
\]

Following the approach of Warden et al. (2013), by introducing the effective fluid model into Pride’s theory, and replacing \( C_{s0} \) by \( C_{s0}(S_w) \), the authors generalized the transfer function formulation for unsaturated conditions. They tested different models of the streaming potential water-content dependency and plotted the results of the dynamic transfer function of the electric field as a function of water saturation (Fig. 8). It is shown that the transfer function is not monotonously decreasing with decreasing water content, but first increases with decreasing water saturation, up to a saturation between 0.9 and 0.5, according to the different hypotheses of frequency domain and saturation dependency of the streaming potential coefficient (SPC). Note that even the SPC is decreasing monotonously with decreasing saturation (case of model from Guichet et al., 2003, for example), the transfer function still shows a non-monotonic behaviour.

### 4 Role of key parameters

We present here the role of key parameters of electrokinetic coupling such as zeta potential, formation factor, permeability, surface conductivity, temperature, and water content.

#### 4.1 Role of key parameters on the steady-state electrokinetic coupling

The steady-state electrokinetic coupling is defined as (Schoemaker et al., 2008):

\[
\mathcal{L}_{ek} = - \sigma_0 C_{s0}. \tag{20}
\]
The influencing parameters on this streaming potential coefficient are therefore the dielectric constant of the fluid $\epsilon_r$, the viscosity of the fluid $\eta_f$, the fluid conductivity $\sigma_f$ and the zeta potential $\zeta$.

### 4.1.1 Effect of zeta potential

The zeta potential is defined as the electric potential at the slipping plane within the electric double layer. The zeta potential itself depends on rock, fluid composition, and pH (Ishido and Mizutani, 1981; Jouniaux et al., 1994, 2000; Jouniaux and Pozzi, 1995; Lorne et al., 1999; Guichet et al., 2006; Maineult et al., 2006; Jaafar et al., 2009; Vinogradov et al., 2010).

The charge density at the surface of the minerals results from surface complexation reactions. The quartz surface can be modelled with silanol > SiOH group (Davis et al., 1978). The potential-determining ions OH$^-$ and H$^+$ are adsorbed onto the surface of the mineral and determine the charge density on the inner plane. The surface charge is therefore dependent on the pH.

There is a pH for which the total surface charge is zero: this is the point of zero charge and this pH is called pH$_{pzc}$ (Davis and Kent, 1990; Sposito, 1989). In this case this electrokinetic effect is zero. The charge is positive for pH < pH$_{pzc}$ and negative for pH > pH$_{pzc}$. The pH$_{pzc}$ for quartz is in the range of 2 < pH$_{pzc}$ < 4 (Parks, 1965; Lorne et al., 1999). The calcite surface can be modelled with > CaOH and > CO$_3$H groups. Carbonate ions and Ca$^{2+}$ are the determining-potential ions. The electrokinetic behaviour on carbonates is more complicated. The pH$_{pzc}$ varies from 7 to 10.8 according to the authors (VanCappellen et al., 1993). It is possible to model simple interfaces and to calculate the zeta potential in simple cases (Guichet et al., 2006). This modelling can be performed assuming the triple-layer model (TLM) which distinguishes three planes to describe the electric double layer: the inner Helmholtz plane for counter ions directly bound to the mineral (assumed to be chemically adsorbed), the outer Helmholtz plane for weakly bound counter ions (assumed to be physically adsorbed), and a $d$ plane associated with the smallest distance between the mineral surface and the counter ions in the diffuse layer. It has been proposed that the slipping plane lies near the distance of closest approach of dissociated ions and that the $\zeta$ potential can be calculated as the potential on this plane (Davis and Kent, 1990).

At a given pH, the most influencing parameter on the streaming potential coefficient is the fluid conductivity. It has been proposed that $C_{s0} = -1.2 \times 10^{-8} \sigma_f^{-1}$ (Allègre et al., 2010), based on data collected in the literature on sandstones and sands (Fig. 9), which leads to a zeta potential equal to $-17$mV, assuming Eq. (22) and that zeta potential, dielectric constant, and viscosity do not depend on fluid conductivity. These assumptions are not exact, but the value of zeta is needed for numerous modellings which usually assume the dielectric constant and viscosity independent of the fluid con-
4.1.2 Effect of formation factor and permeability

Note that assuming the Helmholtz–Smoluchowski equation (Pride and Morgan, 1991) based on quartz minerals rather than on electrolyte concentration. Another formula is often used (Pride and Morgan, 1991) based on quartz minerals rather than on sands and sandstones, which may be less appropriate for field applications.

4.1.3 Effect of surface conductivity

When the surface conductivity can not be neglected, the streaming potential coefficient can be written as follows:

\[ C_{s0} = \frac{\epsilon \eta \zeta}{\eta \sigma_r + \sigma_s}, \]

where \( \sigma_s \) the surface conductivity (S m\(^{-1}\)) (Rutgers, 1940). It is difficult and time-consuming to determine experimentally the surface conductivity of one sample, because it needs measurements with different salinities including very low ones. Therefore this parameter is often deduced from \( \sigma_s = 2 \Sigma_s / R \), with \( \Sigma_s \) the surface conductance (S) and \( R \) the hydraulic radius of the rock or the pore radius (Rutgers, 1940; Alkaifeef and Alajmi, 2006; Wang and Hu, 2012). It has been shown that the surface conductivity in Fontainebleau sand is less than \( 2 \times 10^{-4} \) S m\(^{-1}\) (Guichet et al., 2003). Typical values of the surface conductance for quartz or sandstone range from \( 8.9 \times 10^{-9} \) to \( 4.2 \times 10^{-8} \) S (Block and Harris, 2006) and \( 2.5 \times 10^{-9} \) S for clays (Revil and Glover, 1998). The surface conductivity can neither be neglected in clay layers, nor when the hydraulic radius is of the order of the Debye length. This latter case can be encountered when the fluid is not very conductive, as below \( 2 \times 10^{-3} \) S m\(^{-1}\) in sandstones (Pozzi and Jouniaux, 1994). In that case the streaming potential coefficient can be lowered compared to the expected value. Since the hydraulic radius can be indirectly connected to the permeability, the effect of surface conductivity can explain some observations of permeability-dependence of the streaming potential coefficient (Jouniaux and Pozzi, 1995).

The effect of surface conductivity can also be taken into account if the formation factor \( F \) is known, and if the rock conductivity \( \sigma_r \), possibly with a surface component, is also known, as (Jouniaux et al., 2000):

\[ C_{s0} = \frac{\epsilon \eta \zeta}{\eta \sigma_{eff} / F} = \frac{\epsilon \eta \zeta}{\eta \sigma_r / F}. \]

The advantage of this approach is that neither the surface conductivity nor the conductance are directly needed.
4.1.4 Effect of temperature

The effect of temperature on the streaming potential has been studied both experimentally and theoretically. The streaming potential coefficient on quartz was measured to increase (in absolute value) from $-2$ to $-3 \times 10^{-6}$ V Pa$^{-1}$ between 20 and 70°C (with $10^{-3}$ KNO$_3$ at pH 6.1 at low temperature, and up to pH 4.2 at high temperature) (Ishido and Mizutani, 1981). The authors pointed out, from the equilibrium time needed for the measurements of the order of 20 to 150 h, that the thermal equilibrium of charge distribution near the interface is not reached very quickly. On westerly granite, the streaming potential coefficient was measured to decrease (in absolute value) from $-2.3$ to about $-1.9 \times 10^{-7}$ V Pa$^{-1}$ between 5 and 70°C (with NaCl solution of resistivity 8.5 Ωm at 25°C) (Morgan et al., 1989). The differences between these two studies is that the last one was performed in 4 h for the entire experiment, so that the silica equilibrium was not attained, although the authors mentioned that silica equilibrium takes many days to be established. Taking into account the effect of temperature on the permittivity, the conductivity, and the viscosity, the authors concluded that the zeta potential was constant in this range of temperature, and at this rate of measurements.

Reppert and Morgan (2003a) studied theoretically the effect of temperature on the different parameters of the streaming potential coefficient. They showed that the viscosity is the most dominant term in the temperature-dependent SPC. Then the fluid conductivity also shows a strong dependence on the temperature. The permittivity shows a small dependence on temperature. These effects can be balanced so that assuming a zeta potential constant and a temperature-dependence on the three other parameters, the SPC is roughly independent of the temperature (Reppert and Morgan, 2003a).

However measurements of the SPC on sandstones and granite samples in the temperature range 20–200°C, allowing very long equilibrium times such as 700–1200 h, showed that the SPC is not constant (Reppert and Morgan, 2003b). The SPC is decreasing in magnitude from 20 to 160°C, from about $2 \times 10^{-7}$ to $3 \times 10^{-8}$ V Pa$^{-1}$ (Fontainebleau sandstone) and from about $1 \times 10^{-7}$ to $2 \times 10^{-8}$ V Pa$^{-1}$ (Berea sandstone), before increasing in magnitude up to 200°C, up to $4 \times 10^{-8}$ V Pa$^{-1}$ (Fontainebleau sandstone) and $1 \times 10^{-7}$ V Pa$^{-1}$ (Berea sandstone) for temperatures up to 200°C. The fluid conductivity, initially $10^{-3}$ mol L$^{-1}$ NaCl, was increased from 0.01 to 0.13 S m$^{-1}$ (for Fontainebleau sandstone). The observed SPC on westerly granite, of the order of $5 \times 10^{-8}$ V Pa$^{-1}$, showed the opposite behaviour, increasing in magnitude up to 120°C, and then decreasing with increasing temperature. The interpretation in term of zeta potential behaviour as a function of temperature is very difficult because the pH of the electrolyte is changing with the temperature.

Further measurements of the SPC in the range of 20–200°C were performed on Inada granite, and showed an increase in the SPC magnitude with increasing temperature, this increase being larger using low-concentration electrolyte (Tosha et al., 2003). When the sample is initially saturated by $10^{-3}$ mol L$^{-1}$ KCl the SPC increases from $5 \times 10^{-8}$ to $12 \times 10^{-8}$ V Pa$^{-1}$; when initially saturated by $10^{-2}$ mol L$^{-1}$ KCl the SPC increases from $3 \times 10^{-8}$ to about $7 \times 10^{-8}$ V Pa$^{-1}$; and when the sample is initially saturated by $10^{-1}$ mol L$^{-1}$ KCl the SPC increases from $10^{-8}$ to $2.5 \times 10^{-8}$ V Pa$^{-1}$. Unfortunately the authors did not measure the fluid conductivity after equilibrium, and at the end of the temperature increase. But these results are coherent with those of Reppert and Morgan (2003b). The different behaviour of the SPC in sandstones and granite still needs further explanations, and is probably related to different behaviours in pH, surface charge density and dissociation constant in quartz–water or plagioclase/feldspar–water systems, as possible precipitation of secondary minerals.

Another experiment on quartz-Al-K-N0$_3$ system from Ishido and Mizutani (1981) showed that the magnitude of the zeta potential first increases with temperature up to about 45°C and then decreases with increasing temperature up to 80°C. This behaviour was not understood until the study of Guichet et al. (2003). These authors showed that the solutions are oversaturated with aluminum, and that the precipitation of Al(OH)$_3$ is expected. They showed that a triple layer model (TLM) calculations for a gibbsite-KNO$_3$ system can account for these measurements. These authors concluded that the precipitation of a secondary mineral can hide the electrical properties of the primary rock, and that the interfacial processes of precipitation/dissolution should be taken into account when dealing with the temperature effect.

To interpret SE conversion in a geothermal context the first problem to resolve is the knowledge of the interfacial chemistry of the rock/water system, and to know which secondary minerals are present. Then a zeta potential value can be estimated according to the mineral/water system, and a SPC value deduced. Afterward, the effect of temperature on SPC can be estimated based on observations performed on simple systems at fluid conductivity about 0.1 S m$^{-1}$, as quartz- or granite water showing a decrease of a factor of 5 to 7 of the SPC from 20 to 160°C (Berea and Fontainebleau sandstone, Reppert and Morgan, 2003b), or as an increase of a factor of 3 of the SPC from 20 to 120 to 200°C (Westerly granite, Reppert and Morgan, 2003b; Inada granite, Tosha et al., 2003).

4.1.5 Effect of water content

The effect of water content has been studied on the streaming potential coefficient, but the conclusions are still discussed, mainly because of a possible effect of the flow. Perrier and Morat (2000) were the first to propose that the SPC depends on the relative permeability.
These authors proposed that the electrokinetic coefficient varies as a function of the relative permeability \( k_r \) as follows:

\[
C_{\theta 0}(S_w) = C_{\text{sat}} \frac{k_r(S_w)}{S_w^n},
\]

with \( S_w \) the water saturation, and \( n \) the second Archie exponent (Archie, 1942). Revil et al. (2007) proposed a similar formula, assuming that the excess countercharge density scales inversely with water saturation.

Then Jackson (2010) developed a model for the electrokinetic coefficient for unsaturated conditions through a capillary tubes model, including water or oil as fluid. Jackson (2010) showed that the electrokinetic coefficient depends on the relative permeability, the relative charge density, and the fluid content, assuming that Archie’s law is valid, as follows:

\[
C_{\theta 0}(S_w) = C_{\text{sat}} \frac{k_r(S_w)Q_r(S_w)}{S_w^n},
\]

with \( Q_r \) the relative excess charge density: \( Q_r(S_w) = Q(S_w)/Q(S_w = 1) \). Jackson (2008, 2010) showed that the excess countercharge density does not scale inversely with water saturation, but it depends on the pore scale distribution of fluid and charge.

Finally, Allègre et al. (2012) modelled both Richards’ equation for hydrodynamics and Poisson’s equation for electrical potential for unsaturated conditions, using a 1-D finite element method. They concluded, based on laboratory experiments and using these equations, that the unsaturated electrokinetic coefficient should have a non-monotonous behaviour:

\[
C_{\theta 0} = C_{\text{sat}} \gamma \left[ 1 + \beta (1 - S_c) \right],
\]

where the effective saturation is

\[
S_c = \frac{S_w - S_{wr}}{1 - S_{wr}},
\]

and \( \beta \) and \( \gamma \) are two adjusted parameters, \( \beta \) depending on the initial flow conditions, particularly on the water velocity at the beginning of the drainage phase. A non-monotonous behaviour is supported by the observations of Allègre et al. (2010) and also by the observations of Revil et al. (2007) and Revil and Cerepi (2004) as detailed in Allègre et al. (2011). Recently Allègre et al. (2015) showed that the interface between water and air should also be taken into account, since this interface is negatively charged, as the interface between the rock matrix and the water. Moreover during a drainage the amount of this interface does not decrease with decreasing water saturation, but first increases before decreasing, leading to a non-monotonic behaviour of the resulting SPC (Allègre et al., 2015).

The Table 1 summarises the ratios \( C_{\theta 0}(S_w)/C_{\text{sat}} \) proposed by different authors.

<table>
<thead>
<tr>
<th>Reference</th>
<th>( C_{\theta 0}(S_w)/C_{\text{sat}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Perrier and Morat (2000)</td>
<td>( S_w^2/S_{\text{wr}}^n )</td>
</tr>
<tr>
<td>Guichet et al. (2003)</td>
<td>( S_c )</td>
</tr>
<tr>
<td>Jackson (2010)</td>
<td>( S_c^{L+2+2/\lambda}Q_r(S_w)/S_{\text{wr}}^n )</td>
</tr>
<tr>
<td>Allègre et al. (2012)</td>
<td>( S_c(1 + 32(1 - S_c)^{0.4}) )</td>
</tr>
</tbody>
</table>

### 4.2 Role of key parameters on the transition frequency

The transition angular frequency separating viscous and inertial flows in a porous medium can be rewritten by inserting \( \alpha_\infty = \phi F \) with \( F \) the formation factor that can be deduced from resistivity measurements using Archie’s law, as follows:

\[
\omega_c = \frac{1}{F} \frac{\eta}{k_0 n_\phi},
\]

(31)

It can be also re-written as a function of the hydraulic radius \( R \) as

\[
\omega_c = \frac{\eta}{\rho_\phi C R^2}.
\]

(32)

The Eq. (32) shows that the transition angular frequency in a porous medium is inversely proportional to the square of the hydraulic radius.

It has also been shown by Jouniaux and Bordes (2012) that the transition frequency \( f_c = \omega_c/2\pi \) is inversely proportional to the permeability as follows:

\[
\log_{10}(f_c) = -0.78\log_{10}(k) - 5.5,
\]

(33)

and varies from about 100 MHz for \( k = 10^{-17} \) m² to about 10 Hz for \( k = 10^{-8} \) m², so by 7 orders of magnitude for 9 orders of magnitude in permeability (Fig. 10).

Therefore the transition angular frequency depends on the fluid viscosity, the fluid density, and on both the permeability and the formation factor. Although the permeability and formation factor are not independent factors, it has been shown that the transition frequency is inversely proportional to the permeability.

### 5 Modelling and processing

The methods used to numerically approximate solutions to the seismo-electric/electro-seismic equations could be classified according to the extent of the employed source, which can be either finite or point sources (generating 3-D responses), or infinitely long ones (2-D responses). They can also be classified according to the used approximating
the parameters of the samples, $F$ and $k_0$ are measured from different authors on various samples (from Jouniaux and Bordes, 2012).

methodology; according to this choice, most of the methods use either Green's functions formulations, or are different variations of the generalized reflection and transmission matrix method (GMRT), finite differences methods (FD) or finite element methods (FE).

Before we delve into the works corresponding to this description, we mention some different studies, like the works of White (2005), who used seismic ray theory to determine the linear dependence between the magnitude of the ES or SE responses and the electrokinetic coupling coefficient; while White and Zhou (2006) used Ursin's formalism to model electro-seismic conversions on homogeneous layered media within the frame of a unified treatment of electromagnetic, acoustic and elastic waves. Moreover SE reflection and transmission at fluid/porous medium interfaces were investigated by Schakel and Smeulders (2010) who developed the dispersion relation for SE wave propagation in poroelastic media. These authors proved by means of a sensitivity analysis that electrolyte concentration, viscosity, and permeability highly influence SE conversions.

5.1 3-D response of stratified media

In Pride and Haartsen (1996), the governing equations controlling the electro-seismic wave propagation were presented for a general anisotropic and heterogeneous porous material; uniqueness, energy conservation, and reciprocity were derived. Moreover, the authors derived Green’s functions for the coupled poroelastic and electromagnetic problem for the solid and fluid displacements and the electric field, and obtained responses to a point source in an isotropic and homogeneous whole space. Gao and Hu (2010) extended this work by developing the Green function for the magnetic field and by considering moment tensors as sources. In Haartsen et al. (1998), relative flow Green functions were derived to investigate numerically the effect of porosity, permeability and fluid chemistry on dynamic streaming currents caused by point forces in homogeneous porous media. The authors showed that the induced streaming current diminishes with increasing salinity, that its dependence with porosity is different if it is generated by $P$ waves or $S$ waves, and that its behaviour with respect to permeability is different for sources applied to the elastic frame than for volume-injection sources.

Haartsen and Pride (1997) produced numerical experiments featuring seismic and electromagnetic point sources on horizontally stratified media; they used a global matrix method to obtain their results. They showed that the governing equations can be decoupled in two modes, namely the SHTE (horizontal shear wave transverse electric field) mode, involving the seismic SH and transverse electric TE, and the PSVTM (transverse magnetic field of vertical P and S waves) mode, linking the seismic $P$–$SV$ modes with the transverse magnetic TM mode; they showed that the interface response was similar to the one of a vertical electric dipole situated right beneath the seismic source. In Mikhailov et al. (1997) this algorithm was employed to compare synthetic SE conversions generated at a top soil–glacial till interface with field data. Not only they were able to observe SE conversions on the field, but also the numerical simulations qualitatively reproduced the observations. In Hu and Gao (2011), an extension to this algorithm is performed including a moment tensor point source. In this way, electromagnetic fields induced by a finite fault rupture are studied. Their simulations showed that the rupturing fault generates observable permanent electromagnetic field disturbances; two types of electric field characters were observed: the coseismic oscillatory variation and the post-seismic decaying variation. They also observed that when the fault rupturing stops and the seismic waves are far away, the magnetic field vanishes, while the electric field remains, decaying slowly and lasting for hundreds of seconds.

In a work mainly devoted to show SE field experiments, Garambois and Dietrich (2001) developed transfer functions and showed that the electric field accompanying the compressional waves is approximately proportional to the grain acceleration and that the magnetic field and particle velocity in a seismic shear wave are roughly proportional; Garambois and Dietrich (2002), by extending the GRMT (generalized reflection and transmission matrix method), method to deal with coupled seismic and electromagnetic wave propagation in fluid-saturated stratified porous media, thoroughly analysed SE conversions. The authors concluded that the information contained in signals arose in conversions at interfaces generated by contrasts in porosity, permeability, fluid salinity, and fluid viscosity, should be useful in hydrocarbon exploration and environmental studies. Similarly, Pride and Garambois (2005) produced numerical evidence that compressional or shear waves traversing an interface in which any of the transport properties or elastic moduli change, give...
rise to electromagnetic disturbances that can be measured at the surface. In particular, they observed that the amplitude of the converted electric field at the interface can be drastically increased if there is a thin layer of third material present at the interface (Fig. 11), and suggested that this feature could be exploited in hydrological applications.

Yeh et al. (2006) developed a transition matrix approach for an electro-poroelastic medium, which is based by establishing a relation between coefficients of incident and scattered waves; studying the case of a sphere immersed in an homogeneous medium. However, this methodology has not been used in modelling realistic geophysical situations. Grobbe and Slob (2013) and Grobbe et al. (2014) have developed a layered-Earth analytically based numerical modelling code (making use of a Global Reflection Scheme) similar to the code of Garambois and Dietrich. They have implemented all existing possible seismo-electromagnetic and electro-magneto-seismic source–receiver combinations. The code makes use of stable eigenvector sets, (but can also use the Haartsen and Pride based eigenvectors), and is capable of modelling fluid/porous medium/fluid transitions, thereby enabling modelling typical seismo-electromagnetic laboratory wave propagation experiments.

5.2 2-D modelling in vertically and laterally heterogeneous media

Several works implementing different numerical methods already exist to solve the set of equations modelling both mentioned processes. Among others, Han and Wang (2001) introduced a fast finite-element algorithm to model – in the time domain – diffusive electric fields induced by SH waves, producing responses of 2-D reservoirs. The authors were able to confirm the existence of the conversions at interfaces predicted by the theory, and concluded, as other authors, that the detection of the induced EM fields should be performed with antennas positioned close to targets of interest, preferentially in boreholes. This FE code, however, predicts the existence of a strong coseismic electric field in the analyzed mode – the SH one –, which collides with widely accepted theoretical demonstrations opposing this result.

Haines and Pride (2006) developed a finite-difference algorithm capable to model SE conversions in 2-D heterogeneous media. They solved a quasi-static Poisson-type problem for the electrostatic potential, taking for the source term a divergence of the streaming current. They showed that the SE interface response from a thin layer (at least as thin as 1/20 of the seismic wavelength) is considerably stronger than the response from a single interface, and that the interface response amplitude falls off as the lateral extent of a layer decreases below the width of the first Fresnel zone. The first of these conclusions was also observed in Pride and Garambois (2005), with results obtained using the GRMT.

In a similar fashion to the previous reference, several works considered a quasi-static approximation of the model developed by Revil and Linde (2006); in these studies the current density depends on the volumetric charge density linked to the permeability. For example, in Revil and Jardani (2010) the seismo-electric response of heavy oil reservoirs was studied, and in Revil and Mahardika (2013), this approach was used to study two-phase flow conditions and a numerical application is shown for water flooding of a nonaqueous phase liquid (NAPL, oil) contaminated aquifer. However, Eq. (21) is used in these two studies, which, as explained above, is a strong assumption and has not been validated (Jouniaux and Zyserman, 2015). In Santos (2009) and Santos et al. (2012), a collection of finite-element algorithms was presented to numerically solve both ES SHTE
(electro-seismic horizontal S wave transverse electric field) and PSVTM modes of Pride’s equations. The semi-discrete version was used to analyse seismic responses of partially saturated gas/oil reservoirs in Zyserman et al. (2010), and extended to deal with gas-hydrated subsurface regions in Zyserman et al. (2012). Here the author observed that the electromagnetic seismic-induced interface response is sensitive to the saturation of gas hydrates, as it is shown in the SHTE mode for solid accelerations traces (Fig. 12), for a gas hydrate reservoir located below the permafrost base. In Singarimbun et al. (2009), a finite differences algorithm to calculate 2-D SE responses using the transfer function was presented, and several aquitard geometries analyzed. The proposed methodology was able to image layers from the arrival of the reflected coseismic field. However, the failure of this algorithm on simulating the interface response is a disadvantage. In Ren et al. (2010), a technique extending the Luco–Apsel–Chen (LAC) generalized reflection and transmission method was introduced to simulate coupled seismic waves and EM signals radiated by point sources in layered porous media. Later, Ren et al. (2012) adapted this technique to study coseismic EM fields induced by seismic waves originated by a finite faulting in porous media. They showed that the point source approximation is not accurate in the presented configuration, and also concluded that the porosity, the solid and fluid densities and the frame shear modulus have effects on the velocity and wave amplitude of both seismic waves and coseismic EM fields, whereas the salinity only affects the amplitude of the latter.

Kröger et al. (2014), using a displacement-pressure formulation for the poroelastic part of Pride’s equations, solved their 2-D fully coupled version implementing an implicit time stepping finite element algorithm in a commercial software. They analyzed \( P-TM \) conversions that occur within
and at confined units (Fig. 13). In Fig. 14 the $z$ component of the induced electric field for units with different sizes presenting electric conductivity contrast with the host rock are shown. The authors demonstrated that the various SE fields capture both the structural and functional characteristics of the converting units such as clay lenses embedded in an aquifer or petroleum deposits in a host rock, thereby indicating the potential value of the SE method for exploring confined targets encountered in hydrogeological and/or hydrocarbon studies.

### 5.2.1 Borehole geometries

Several modelling works have been developed in borehole geometries. In Hu and Wang (2000) and Hu and Liu (2002), where simplified versions of Pride’s equations were considered (by ignoring the influence of the converted electric field on the propagation of acoustic wave, i.e. neglecting the electro-osmotic feedback), coseismic electric fields for the compressional waves, Stoneley waves, and radiating electromagnetic fields were predicted. The authors proved that their simplifying assumption did not significantly diminish the quality of the modelled waves, compared to the solutions to Pride’s fully coupled equations. This fact has been afterwards used by several authors, because it greatly facilitates the numerical analysis of the SE conversions. Markov and Verzhbitskiy (2004, 2005) used this hypothesis when developing an analytic approach to calculate the electromagnetic fields induced by an impulse acoustic source. They obtained, in the frequency range of acoustic logging, the relationship between the components of the induced electromagnetic field and the formation porosity and permeability; which they asserted could be potentially used for rock permeability estimation.

Pain et al. (2005) used a time domain mixed displacement-stress finite element method to model electric fields induced by acoustic waves in and around a borehole; for a maximum source displacement of one micrometer within the borehole, they predicted electrical potentials of tens of mV in the surrounding formation; and concluded that this size of signal would make such investigations viable in the field. However, they did not delve in the dependence of the measured signals with properties of the formation, the fluid and other conditions present in the borehole.

Zhan et al. (2006b) performed both laboratory experiments and numerical studies on SE and acoustic signals when studying how to eliminate borehole logging-while-drilling (LWD) tool modes, concluding that LWD SE signals do not contain contributions from the tool modes, and that correlating the LWD SE and acoustic signals, the tool modes can be separated from the real acoustic modes, improving the signal to noise ratio in acoustic LWD data.

Zhou et al. (2014) studied the SE field excited by an explosive point source located at the outside of a borehole; they observed that when the distance from the acoustic source to the axis of a borehole is far enough, the longitudinal and coseismic longitudinal wave packets dominate the acoustic and
electric field, respectively. They asserted that the distance from the point where the maximum amplitude of the axial components of electric field is recorded, to the origin of co-ordinate indicates the horizontal distance from the explosive source to the axis of vertical borehole, and suggested that this knowledge could lead to apply SE in microseismics and crosshole experiments.

Zyserman et al. (2015) modelling shear wave sources in surface to borehole SE layouts, and employing two different models for the saturation dependence of the electrokinetic coefficient, studied the interface response of layers containing different saturations of CO$_2$. They observed that the IR are sensitive to CO$_2$ saturations ranging between 10 and 90%, and that the CO$_2$ saturation at which the IR maxima are reached depends on the aforementioned models. Moreover, the IR are still sensitive to different CO$_2$ saturations for a sealed CO$_2$ reservoir covered by a clay layer.

### 5.2.2 Permeability dependence analysis

In a work combining modelling and field experiments, Mikhailov et al. (2000) measured Stoneley-wave-induced electrical fields in an uncased water well drilled in fractured granite and diorite. Using Biot-theory-based models, the authors concluded that the normalized amplitude of the Stoneley-wave-induced electrical field is proportional to the porosity, and the amplitude vs. frequency behaviour of this electrical field depends on the permeability of the formation around the borehole.

Considering the same geometry, but analyzing the acoustic response to an electromagnetic source, electro-acoustic logging for short, Hu et al. (2007) analytically proved in this context that the electro-filtration feedback, i.e. the generation of an electric current due to the induced pressure gradient, can be neglected in Pride’s equations, so that the associated reciprocal SE phenomenon could also be more easily handled. They distinguished four different mechanical wave groups generated through the conversion; in particular they payed attention to Stoneley waves, observing that their amplitude is permeability and porosity dependent. The authors noticed that the electro-acoustic Stoneley wave amplitude dependence with porosity has different regimes depending on the permeability; namely it increases with porosity in the permeability range of sediment rocks, and decreases with porosity for high permeabilities (several Darcies or higher). Moreover, they noticed that in the last regime there is a threshold permeability beyond which the electro-acoustic Stoneley wave amplitude does not change with porosity, and that its

![Figure 14. Electrograms for the confined unit geometries of Fig. 13: the left column is for $2 \times 6$ m the middle column is for $5 \times 6$ m and the right column is for $10 \times 6$ m. The top row shows the $z$ component of the electric field for the material with electrical conductivity of $0.05$ S m$^{-1}$, the middle row shows the $z$ component of the electric field for a material with electrical conductivity of $10^{-5}$ S m$^{-1}$. The bottom row shows the calculated differences in the amplitudes for both previous models. Notice that all amplitudes are scaled identically and that the electric conductivity is the only medium parameter with contrasts among different units (from Kröger et al., 2014).](image-url)
permeability sensibility is higher than what is observed in conventional acoustic logging.

Guan and Hu (2008) used the mentioned simplification when proposing a finite-difference method with perfectly matched layers (PMLs) as boundary conditions for electro-seismic logging in an homogeneous fluid-saturated porous formation. Since the frequency range in this work was assumed to be of the order of the kHz, the dynamic permeability was assumed to be frequency dependent, as derived in Johnson et al. (1987). Although they did not implement it, they discussed how to extend the finite differences algorithm to deal with stratified media. Recently, Guan et al. (2013) proposed a permeability inversion method through the existing relation between SE logs and formation permeability. By working with the Stoneley wave ratio of the converted electric field to pressure (REP), they noticed that its amplitude is sensitive to porosity, while the tangent of its phase is sensitive to permeability. They performed synthetic experiments which led them to argue that their results improved those provided by the acoustic logging inversion method.

5.2.3 Partially saturated media

An important topic when studying the conversions we are interested in is their behaviour when produced in partially saturated media. The behaviour of the streaming potential coefficient under this condition has been analyzed in Sect. 3.2. Concerning wave propagation in partially saturated soils, Warden et al. (2013) extended Pride’s theory to handle these kinds of soils by making the model parameters – the streaming potential coefficient, bulk electrical conductivity, fluid viscosity, etc. – saturation dependent; they compared the behaviour of these parameters using different saturation laws. Modifying the GRMT method accordingly, they used this extension to analyse the response of a capillary fringe between a totally and a partially saturated layer. The authors concluded that an IR created by a saturation contrast between sand and sandstone may be easier to detect than a SE conversion occurring at the same boundary between sand and sandstone with the two units fully saturated. Moreover, as shown in Fig. 15, they proved that the conversions depend on the type of saturation transition existing between the partially saturated and fully saturated units.

Recently Bordes et al. (2015) used the same approach to derive the transfer function between the electric field and the acceleration as a function of water saturation (see Sect. 3.2).

5.3 Inversion attempts

Jardani et al. (2010) were able to model a finite element algorithm the SE response over a stratified medium including a reservoir partially saturated with oil. Moreover, the authors generated one of the few inverse problem investigations published up to now. Their approach was a 2-D joint inversion of seismic and SE synthetic signals generated in a partially saturated oil reservoir; they concluded that, with this methodology, they could invert the permeability of the reservoir and its mechanical properties. More recently, Mahardika et al. (2012), by using a similar approach, inverted synthetic data corresponding to the occurrence of a fracking event in a two-layers system. The authors concluded that the model parameters are better determined for the joint inversion of seismic and electrical data by comparison with the inversion of the seismic time-series alone. Maas et al. (2015) have carried out a sensitivity analysis using resolution functions as structured first steps towards inversion.

5.4 Full 3-D modelling

The degree of difficulty in numerically modelling both SE and electro-seismic wavefields using finite sources (be they natural or man-made) and 3-D Earth models – mainly because of the need of an extensive computing power – can be estimated by extrapolating from the fact that up to now there is just one published work involving such situations. In Wang et al. (2013), a time domain finite difference algorithm is presented to model 3-D SE responses to slipping faults, which deals with Biot equations using a velocity-stress FDTD algorithm and the PML technique for the truncated boundary, while the EM fields are calculated by the alternating-direction implicit method. This novel methodology was validated against analytic solutions, studying the SE fields induced by a slipping fault – modelled as a double couple – in an otherwise homogeneous semispace. In particular, the vertical component of the electric field near the surface was analyzed, due to its expected high attenuation rate in this region. Contrary to what they observed far from the surface, in its vicinity the numerical vertical electric field departed from the analytical results; the authors attributed this fact to a low precision approximation for the spatial variation of the pressure in their algorithm.

5.5 Data filtering techniques

As already mentioned, the amplitude of the converted SE and ES signals is very small, so it is very important to treat the collected data very carefully, minimizing noise from cables and triggers, and applying specially devised filtering techniques.

5.5.1 Harmonic noise

The first step in processing the SE data is to remove the noise coming from power lines, which can be of the order of $1 \text{ mV m}^{-1}$. The estimate of the harmonic noise can be performed on the data recorded just before the shot, using a pre-trigger recording. The harmonic noise may be reduced by subtracting the noise recorded by a remote dipole, or using the difference between the signal recorded by dipoles symmetrically put on opposite side of the shot. The filtering of this noise can be performed by applying a single frequency
266 L. Jouniaux and F. Zyserman: Seismo-electrics

Figure 15. Comparison of the mean amplitudes of the interface response induced by compressional waves (bottom left) and shear waves (bottom right), for a sharp saturation transition (top left model) between the two considered regions and for a gradual saturation transition, as given for the capillary fringe shown in the top right model. The S-EM IR response is stronger for the capillary fringe than for the sharp saturation transition, while the $P_{T}$-EM IR response is stronger for the sharp concentration transition than for the capillary fringe (from Warden et al., 2013).

adaptive noise cancellation filter. Butler et al. (1996) proposed to apply the techniques of block and sinusoidal subtraction. Note that the most efficient method which is used for most of the observations is to routinely reduce the harmonic noise using the algorithm of Butler et al. (1996, 2007); Butler and Russell (2003), applied to individual shot before the stacking. Wiener and bandpass filters can be used to reduce high-frequency noise (Thompson and Gist, 1993). Supplementary techniques as delay-line filtering in case of severe noise (Szarka, 1987), and low-pass filtering in case of strong high-frequency noise contamination can be used.

Another algorithm for suppressing power line noise is the Hum filter devised by Xia and Miler (2000). Determined using the Levenberg–Marquardt method, this filter can handle cases where power-line noise and its multiples exist simultaneously, and removes them without altering the signals spectra.

5.5.2 Trigger and cables

Noise at the beginning of the records can often be recorded. It can be a problem when trying to detect shallow interfaces. This noise can be induced by the metallic plate hit with a hammer to provide the source. Using a non-metallic plate can resolve this problem (Butler, 1996). Inserting a piece of cardboard between the plate and the hammer can also eliminate this noise (Butler et al., 2007). Using an automatic triggering can also induce spikes in the signal, because there is a large difference of voltage in the cable linking the piezoelectric transducer to the trigger. Therefore a manual triggering is preferred when trying to detect shallow interfaces; otherwise we can be simply mute the first 10 ms. Possible noise from cross-talk cables must also be checked. Finally Butler et al. (2007) noted that the amplitude modulated (AM) radio interference could be reduced by reducing the contact impedance of the electrodes in the ground, using a mixture of water and soil within the holes of the electrodes.

5.5.3 Interfacial response

The interfacial response can provide information about the formations at depth while the co-seismic signal provides only information in the vicinity of the electrodes. The challenge is therefore to isolate the interfacial response, which is often of the order of $1 \mu \text{V m}^{-1}$. Note that the interfacial response can be observed free of the coseismic signal when the electrodes are located below the interface of interest (Dupuis et al., 2007), by measuring the electric field within a borehole. However this situation is not commonly implemented.

Haines et al. (2007b) undertook a series of controlled SE field experiments, from which it was concluded that off-line geometry (e.g. crosswell) surveys offer a promising application of the SE method, because they allow for the separation the IR from the coseismic and source related fields; more-
over, as seismic sources and electrode receivers would be positioned near to targets of interest, the use of high-frequency sources would be possible, and the recording of the signals that rapidly decay with distance because of the nature of the electric dipole field would be facilitated.

The characteristics of the IR is an opposite polarity on opposite sides of the shot -depending on the measured field component-, an amplitude which is maximum at offset half of the interface depth, and a quasi-simultaneous arrival on the electrodes. As the interfacial response arrives simultaneously on the electrode profile (meaning it has almost a zero slowness or infinite velocity), the co-seismic signals propagating with seismic velocities can be eliminated in theory using an F–K or tau–p filter, so that the interfacial response can be isolated. Using the F–K filtering can show good results by differentiating the IR response from the coseismic signal (Strahser et al., 2007). However, such filters require a spatial sampling relatively dense, which is not often encountered. One possibility to overcome this problem has been proposed by Kepic and Rosid (2004) who combined shot records from 24 sensors from adjacent closely spaced shot positions to create a virtual 120 channel record or “super gathers”.

Haines et al. (2007a) proposed a workflow to deal with SE signals, starting with the removal of power line harmonic noise as explained above, followed by using frequency filters to minimize random and source-generated noise. The next step would be to adjust amplitude levels by using time-varying gains, followed by the separation of signal and noise, for which they proposed to use either linear Radon transform filtering or nonstationary prediction-error filters. As a final step, they suggested performing display processing, by means of frequency filtering and gains. In the signal/noise separation stage they observed that mapping to the linear Radon domain with an inverse process incorporating a sparseness constraint worked adequately, but also that this process was ineffective if noise and signal show the same dip. They also noticed that F–K filtering not only fails to remove all source-generated noise but also perturbs signal amplitude patterns. They asserted that prediction-error filters are a better way to separate signal and noise, while also preserving amplitude information, whenever appropriate pattern models can be built for the signal and noise.

More recently, Warden et al. (2012) developed a new fast discrete curvelet transform-based filtering strategy to separate IR from coseismic signals, with the goal of improving the preservation of the IR amplitudes. The authors obtained better results with their technique than when applying Radon transform or F–K filtering, confirming the critics that Haines et al. (2007a) made to the latter. They also argued that standard “dip-based” procedures taking advantage of the high ratio between EM signal propagation velocity and its seismic counterpart, can be used to identify IR. However, as previously noticed in Thompson et al. (2007), they also remarked that this choice, by altering signal amplitudes, removes the possibility of characterize reservoir geometries. Grobbe et al. (2015) discuss a combined multi-component–multi-depth-level way of decomposing SEM data into up/downgoing waves and the different field types; although they did not handle field data, and can be practically adverse because of the many field components that must be measured, their method shows improved theoretical results compared with the performance of the multi-component decomposition scheme.

6 Field observations

Field measurements can, in principle, record both the coseismic and the interfacial signals. Due to the small amplitude of the IR, and to the ambient electric noise, pre-amplifiers are needed to enhance the signal-to-noise ratio. Several geometries can be developed in the field: the source and the electrodes can be implemented on the surface or within a borehole. The field acquisition systems and geometries usually exploit the asymmetry of the IR signal to enhance the separation of the signal from the noise.

We first describe the recommendations for the sources, electrodes, and acquisition. Then we detail results showing interfacial responses, measurements performed in boreholes, electro-seismic observations, and observations for partial-saturation conditions.

Sources

Most of the academic studies are performed using a sledgehammer as the seismic source. Various hammer plates of aluminum, polycarbonate, wood, with various geometries can be used (Haines et al., 2007b). It may be better to use a non-metallic plate to avoid the electrical noise linked to the moving metallic plate into the magnetic field when the plate is in electrical contact with the soil: this Lorentz field has been studied by Haines et al. (2007b). Then, processing the data requires the stacking of about 100 records to be able to detect an interfacial response, even at the typical distance of 20 m (Haines, 2004). Other seismic sources such as explosives (Thompson and Gist, 1993) or accelerated weight drops (Dupuis et al., 2007) are also used. The amplitude of the IR signal was shown to be proportional to the square root of the charge weight, the amplitude of the seismic first break showing the same proportionality (Martner and Sparks, 1959). A vibrator-source tested by Haines (2004) showed too much electrical noise to be used. Several records can be combined to improve the signal-to-noise ratio (Kepic and Rosid, 2004; Dupuis et al., 2007; Strahser et al., 2011). The triggering using the electric signal of the output of an accelerometer mounted on a hammer can generated electromagnetic noise. A manual triggering does not induce this noise. Data acquisition can also be triggered by the light that accompanies cap detonation, and transmitted by a fiber optic cable (Butler et al., 1996), to avoid this noise.
Recently an hydraulic vibrator has been used to increase the source strength (Dean et al., 2012; Valuri et al., 2012) on two sites: in Australia and in Abu Dhabi. The authors showed that the interfacial response due to a water table at depth of about 14 m could be detected without stacking, at offsets of up to 120 m, on the first site (Dean et al., 2012); and that the coseismic signal was clearly shown on a large scale in the arid region of the second site (Valuri et al., 2012). Moreover, when the data were stacked, the interfacial response of the base of the aquifer, at a depth between 40–60 m, was shown on a profile up to 800 m (Dean et al., 2012).

Electrodes

The electrode polarization is less a problem in SE than in other geophysical methods such as audio-magnetotellurics or self-potentials. The SE signals obtained with polarizable (stainless-steel, lead rods) or non-polarizable (Cu/CuSO₄) electrodes do not differ significantly from each other (Beamish, 1999). Electrodes are often stainless steel tubings of 30–50 cm length. The contact impedance between electrodes must be low, which needs the electrodes to be watered when the soil is not wet enough. Some authors suggest to water the electrodes with a mixture of clay and water. The dipole length is usually 1–2 m. The effect of the dipole length between 1 and 10 m has been tested: the amplitude results showed that the received voltages are independent of dipole length when the position of the inner (nearest the shot point) electrode remains at a fixed offset, the inner electrode controlling the amplitude and character of the received voltage (Beamish, 1999), as already mentioned by Martner and Sparks (1959). Data collected with and without geophones present between two electrodes are similar, so that the geophones do not affect the SE signal (Haines, 2004). When measuring the SE conversions within a borehole, Dupuis et al. (2009) used tinned copper wire wrapped around segments of PVC pipe of 10 cm long and 2.5 cm in diameter.

Acquisition

Most of the data acquisition systems are modified and unmodified multichannel seismic systems. Signal conditioning can use fixed or variable gains, and different bandwidths. The data sampling can range from 10 to 20 kHz, the resolution is 16 bit and the typical record length is 4000 points. Pre-amplifiers should be used, with high input-impedance and high common-mode rejection, so that the correct amplitude of the signal can be detected, and can be compared from one observation to another including different soil conductivities. However such pre-amplifiers are not always used, so that the amplitudes of the field observations are often not comparable. At least the impedance across a pair of electrodes should always be tested to be several orders of magnitude less than the input impedance of the acquisition system. Moreover, the acquisition system can be grounded to avoid spurious instrument-related noise.

6.1 Interfacial response observations

Over the past decades, seismo-electromagnetic phenomena have been observed in the field, as recalled above in the History section. Then, over the past 20 years up until recently, increasing successful field experiments have been reported.

Seismo-electrics have been used for mapping a shallow lithological boundary (Butler et al., 1996). These authors could map an interface between permeable organic-rich road fill and impermeable silty glacial till. Using a hammer source or detonation of blasting caps at various depths in a borehole (from the surface to 5 m depth), they could map a dipping interface between 1 and 3.5 m depth. The amplitude of the recorded signals, using a sledgehammer, was in the range of 0.8–2.4 mV for dipoles of 10 m length. When using the detonation source in the borehole, the amplitude of the recorded dipoles at the surface was 3 mV to 20 µV for 2 m dipoles. The maximum offset was about 10–20 m. The water table present at 1 m below the interface or 0.35 m above the interface was not detected by a SE conversion. The authors concluded that seismo-electrics may be used to map the interface of permeable layers.

Seismo-electric surveys were also performed on a subsurface site known by seismic refraction and resistivity (Mikhailov et al., 1997). The authors observed the IR at the top soil–glacial till interface at 0.75 m depth, and also the signal induced by the electric field generated by the seismic head wave travelling along this interface, which shows a moveout on the recordings. They could also detect the water table at 3 m depth and the glacial till–bedrock interface at 9 m depth. After filtering the data the amplitudes of these signals are from 300 to 5 µV from 0.6 to 6 m from the source.

Garambois and Dietrich (2001) measured the IR from a water table at about 1.5 m depth, and the electric signals associated to the Rayleigh surface waves which dominates the observations. The authors showed that the amplitude of this second signal depends on the local properties of the porous medium, as explained by the derivation of the transfer function (see Sect. 3.3). The coseismic signals could therefore help to characterize the properties of the fluid of the local porous medium.

Seismo-electric surveys have also been performed for the exploration of glaciers, as on Tsanfleuron Glacier (Switzerland). The interface between snow and ice at about 22 m depth, with a difference in seismic velocity from 960 to 3650 m s⁻¹, was identified by an IR detection (Kulessa et al., 2006). Moreover, the ice-bed (limestone) interface at about 95 m depth also induced an IR.

Strahsers et al. (2007) performed SE survey in Holocene sediments from Furhtberg forest (northern Germany), by measuring radial, transverse, and vertical components of the SE field. Data were first filtered through F–K transform.
Then the polarization of the seismo-electric field was analysed. The coseismic wave is polarised perpendicularly to the front of the \( P \) wave time derivative, and the IR field is polarised as the field lines of an electric dipole source. The IR from a sand/silt interface at 4 m depth could be detected. The relative amplitude between radial and vertical components of the SE field could be modelled only by taking into account the destructive interference of the IR originating at the interface at 4 m depth and at another interface at 5 m depth. This thin layer would have been remained undetected with one-component measurements.

Dupuis et al. (2007) built a SE profile acquired over 300 m on sedimentary context (Fig. 16), by plotting at each shot location the stack of the traces with offsets between 14 and 40 m. A water table at depth 14 m and a shallower water-retentive layer in sediments were detected. The authors observed a peak amplitude of 1 \( \mu \text{V m}^{-1} \) and the IR was detected at offsets up to 40 m from the seismic source. Note that the shallow water-retentive layer was not mapped by seismic reflection or refraction. The authors concluded that the SE method can be a valuable tool for the characterization of aquifers.

It is possible to record the IR separately from the coseismic field by building two trenches filled with sand and separated by 2 m within a clay-rich soil, as performed by Haines et al. (2007b). These authors performed off-line geometry surveys using seismic shots on the opposite site of the receiver profile, compared to the two trenches, with an angle of 20°. The authors clearly showed the interface signals from the trenches in their correct dip geometry.

### 6.2 IR observations using borehole geometry

A great advantage of a vertical or horizontal SE profile is the possibility to perform the measurements below the studied interface, thereby closer to the interface and allowing for the separation of the IR from the coseismic signal. Electrodes can be deployed within a water-filled borehole. In this case the borehole should have a slotted PVC casing to allow the electric contact between the electrodes and the formation.

Decades ago Martner and Sparks (1959) performed explosive detonation in borehole, at several depths up to 60 m and measured an IR, either by electrodes on the surface or within another hole. They showed that the IR was generated by the base of a weathered layer, at about 3 m, characterized by a change in seismic velocity.

Later on, Butler et al. (1996) could map a shallow lithological boundary using explosive fuse caps within a borehole as the seismic source. The interface between an upper till layer over a glacial till at about 2 m depth was clearly shown by the SE signals measured at the surface. These authors showed that when the source is below the interface, the SE signals have higher amplitude and higher frequency responses than when the source is located above the interface. The authors concluded that it was due to better seismic coupling in the dense glacial till than in the upper layer. Russell et al. (1997) noted that the IR conversion could be detected up to offsets of 16 m, and that the top of the bedrock also induced an IR conversion.

Electrokinetic response in borehole can also be used to detect fractures, as proposed by Hunt and Worthington (2000). These authors used a mechanical source consisting of a steel tube, through which runs a steel shaft attached to a cylindrical nylon block, which was pulled up by a rope up to the surface. This system has the advantage of avoid the electrical noise that may arise from electromechanical mechanism. The induced pressure pulse gives rise to a an electrokinetic signal measured by steel mesh electrodes within the borehole. The authors measured electrokinetic signals up to 1500 mV MPa\(^{-1}\) and showed strong correlations between the electrical signals and the location of opened fractures in the range of 1 mm–5 cm.

More recently Dupuis et al. (2009) could detect a partially cemented layer of 2 m height within unconsolidated sediments at about 13 m depth, by a vertical SE profiling survey, using a sledgehammer seismic source on the surface.
and six electrical dipoles within the borehole. The advantage of this configuration is that the noise level is as low as 0.1–5 \mu V m^{-1}. Over the two locations investigated, only one showed a very clear IR signal, observed over more than a depth of 14 m. This signal was interpreted to be due to a sharp increase in fluid conductivity and a strong impedance contrast from the water table and a coincident partially cemented layer.

6.3 Electro-seismic observations

The electro-seismic surveys use an injection of current into the Earth in the seismic frequency band. The spacing of the electrodes is similar to the depth of investigation. The converted seismic wave is then recorded by geophones on the surface or in a borehole. The commonly understood conversions vary linearly with the input current. Electro-seismic observations are less common than SE ones, maybe because of the difficulty of injecting a large enough current (which can range from 100 to 1000 A) with appropriate characteristics. The challenge in building the electromagnetic source is that the current level can be thousands of A, and the switching time resolution is tens to hundreds of \mu s. The near-surface noise coherent with the source could also be a limitation.

Decades ago, Thompson and Gist (1993) observed conversions from electromagnetic to seismic energy at the sili-ciclastics Friendswood test site (Texas), with the presence of a sequence of high-permeability water sands and low-permeability shales over 300 m depth. Electric currents of 150 A were injected through electrodes of aluminum foil of several metres buried 0.5 m below the surface and separated by 300 m. Pulse frequency signals were applied with a 20 kW audio power amplifier. The hydrophones were shielded to reduce the electromagnetic pick up. Seismic measurements were performed within a borehole located between the two source electrodes. Unfortunately the authors could not have enough data to process an imaging of the interfaces. They showed through modelling that electro-seismics are more sensitive to low-permeability formations, whereas seismo-electrics are most sensitive to high-permeability formations.

Over the last 2 decades, some observations showed that the electro-seismic conversions could yield conversions of higher energy efficiency. First successful demonstration that electro-seismic conversions can distinguish between aquifers and gas sands and can be used at depths up to 1000 m using geophones placed on the surface of the Earth were provided by (Thompson et al., 2007; Hornbostel and Thompson, 2007). Source waveforms have been developed through coded waveforms, both with a linear and non-linear sequence of 60 Hz cycles. These developments were performed to consider the case in which the input current (Hornbostel and Thompson, 2005). Some power waveform synthesizers were developed, each handles 350 kW and weighs 300 kg. Digital accelerometers were used to achieve the low electromagnetic pickup required to detect the small IR signals, and were deployed on the surface or in borehole (Thompson et al., 2007; Hornbostel and Thompson, 2007).

Observations were performed on the Webster field (Gulf coast, Texas) whose gas sands showed porosities of up to 34\% (Thompson et al., 2005). Electro-seismic IR were detected at least for three sand intervals up to 150 m depth. The IR signal was strengthened when the channel was filled with shale. The authors showed through modelling that, because the gas sands are highly resistive, electric currents can steer around so that the IR is weak for a thick layer and strong for a thin layer. Moreover, the observations showed that the high-amplitude electro-seismic conversions were associated with gas sands, and showed the power of resolving fine structure of 5 m difference between shale and gas sand (Thompson et al., 2007). This experiment succeeded to detect gas sands up to 500 m deep with good signal-to-noise ratio.

Another survey was performed in the Turin field (Alberta), having porosities as high as 28\% and permeabilities up to 4 Darcies (Thompson et al., 2005). Both surface and downhole (hydrophones) measurements were performed. At one location, we observed an IR related to the lower limit of a shallow thick (35 m) highly resistive gas cap at 1000 m depth.

A third field was investigated by the same authors: the Bronte field (Texas), which is a deeper carbonate oil reservoir with porosities ranging from 6 to 12\% and permeabilities from 7 to 200 mD. The reservoir was not detected by the linear electro-seismic conversion. Non-linear response was observed showing coherent amplitudes in a portion of the survey area with hydrocarbons where production occurs, which was not well understood (Hornbostel and Thompson, 2007). Further analyses showed that the electro-seismic conversions included source-generated noise (Thompson et al., 2007). The authors processed the signal at double the source frequency to reject the fundamental frequencies of the source waveform. The high-amplitude ES conversion at 1500 m depth was shown to adequately match the seismic studies. The authors concluded that it is not obvious that the electrokinetic conversion process can account for these second-order effects.

6.4 Partially saturated observations

Strahser et al. (2011) observed seismo-electric conversions in the field, as a function of water saturation, and proposed a transfer function between the electric field and the acceleration as a function of the water saturation. The authors proposed that in the low frequency domain, taking into account the water saturation, the SE field and the seismic field are related as follows:

\[
E \sim \frac{\epsilon \xi}{\eta \sigma_r} S_r^{(0.42 \pm 0.25) n} d_f \ddot{u}.
\] (34)
The observations could not be performed in a large range of water content, leading to relatively scattering data. This approach has to be compared with recent results from Bordes et al. (2015) in Sect. 7.1.

6.5 Natural earthquakes

Electromagnetics signals accompanying seismic waves can be observed in the field, recorded most of the time as coseismic signals. Among the possible mechanisms at the origin of these signals, the electrokinetic effect produces the largest ones (Gershenzon et al., 2014). The orders of magnitude of these observed coseismic electric and magnetic signals are usually 1–100 mV km\(^{-1}\) and 0.01–1 nT (Ren et al., 2015). Coseismic electric signals during earthquakes of magnitude above 5 have been observed by Mogi et al. (2000). Coseismic magnetic fields have been reported for the magnitude 6 Parkfield earthquake (Johnston et al., 2006), and for the magnitude 9.4 Sumatra earthquake (Guglielmi et al., 2006). Both electric and magnetic signals have been measured during the Izmit earthquake (Honkura et al., 2002; Matsushima et al., 2002). Many approaches have been developed to model such electromagnetic signals induced by the electrokinetic effect (Gershenzon et al., 2014). Recently Ren et al. (2015) numerically modelled the coseismic signals related to a finite fault displacement. These authors concluded that the electrokinetic effect combined with a surface-charge assumption is a good candidate to explain the EM coseismic signals.

7 Laboratory observations

Due to the low signal-to-noise ratio of the SEM conversions, laboratory measurements are difficult. It is first necessary to exclude the SEM resonance effects caused by mechanical vibrations of the sample itself. It is therefore essential to have a rigid framework. Moreover, the electric and magnetic recorders must be mechanically decoupled from the sample set-up, so that they can not vibrate. Some experimental set-ups include an absorber of acoustic signals which strongly reduces the effect of reflected waves on the results of measurements in the harmonic regime (Migunov and Kokorev, 1977). The electromagnetic noise must be suppressed by shielding the set-up and the wires. Some experiments are carried out in a specially shielded room, or copper mesh Faraday cage can be used to isolate the experimental device from electrical interference and to provide a universal ground. When performing magnetic measurements it is necessary to use non-metallic materials, because of their possible even small displacements within the ambient magnetic field. Measurements performed on dry samples showed that both the electric field and the magnetic field are within the noise level (Zhu et al., 2000; Bordes et al., 2008).

Sources

Due to the scale of the samples used in laboratory, the seismic source is usually higher frequency, in the range of 10–500 kHz, than the frequencies involved in field observations. In most of the studies piezoelectric transducers are used to generate \(P\) waves and \(S\) waves. Although the centre frequencies of the transducers are several hundreds of kHz, the centre of frequencies of the propagating wave can be about 20 kHz (Zhu et al., 2000), because of attenuation. The acoustic transducers are driven by an electric pulse, whose width is adjustable usually to the half period of the recorded acoustic wave and can be in the range of 10–100 µs. This pulse can be a single pulse, a continuous sine wave or a multi-cycle sine burst. In case of a cylindrical sample whose length is very large compared to the diameter the main modes excited can be the extensional and flexural ones.

Electrodes

Different kinds of electrodes can be used. Electrodes can be made of conducting glue of 0.2 cm of diameter (Zhu et al., 2000), of platinum discs, of impolarizable silver/silver chloride rod, or mesh.

Equilibrium time

The equilibrium between the sample and the water must be attained to be able to reach the steady state. This equilibrium should be checked by measuring the pH and the electrical conductivity of the fluid while water is circulating within the sample (Guichet et al., 2006; Schoemaker et al., 2008; Allègre et al., 2010), and performing the electric measurements once the pH and conductivity are constant. If the equilibrium is not attained, the electric measurement can not be constant. Moreover measurements performed at different salinities could be difficult to compare (Schakel et al., 2011, 2012).

7.1 Effect of physical parameters on seismo-electric conversion

In the 1970s, laboratory experiments were performed to better understand the effect of salinity, of moisture, of porosity, and of frequency on the coseismic signal (Gaskarov and Parkhomenko, 1974; Migunov and Kokorev, 1977).

Most of the time, only the longitudinal SE conversion is measured (when the electric field is parallel to the propagation of the elastic wave). Parkhomenko and Topchyan (1995) also measured the transverse seismo-electric effect by measuring the electric field by two electrodes moving along the surface of the sample perpendicular to the wave propagation induced by a piezoelectric transducer. It was shown that the projection of the electric intensity vector on the direction perpendicular to the direction of elastic wave propagation is about 1 order smaller than the projection on the direction of the wave propagation.
The effect of the frequency of the seismic source was studied on limestone samples with about 8–10 % water content, maintaining a constant acoustic intensity. Measurements showed that the magnitude of the SE signal increases with frequency in the range of 5–25 kHz. On the other hand recent results showed that the amplitude of the SE coefficient decreases when the frequency increases in the range of 5–200 Hz on glued glass-tubes samples, and that the phase values also decrease with increasing frequency (Schoemaker et al., 2008). These observations are in accordance with Pride’s theory. Moreover it was also shown that the amplitude of the SE coefficient decreases when the frequency increases in the range of 15–120 kHz on a saturated Berea sandstone with NaCl solutions with conductivities between 0.012 and 0.32 S m\(^{-1}\) (Zhu and Toksöz, 2013), which is in accordance with the theory for saturated conditions (Eq. 8).

For a conductivity of 0.012 S m\(^{-1}\) the SE coefficient is decreased from 0.25 to 0.15 µV for an increasing frequency from 15 to 120 kHz, respectively (Zhu and Toksöz, 2013). The different results of these studies show that the effect of water content may be complex.

Three values of porosity were tested by Migunov and Kokorev (1977): 4, 10, and 12 % at water content 8–10 %, and the slope of the electric signal-frequency curve increases with porosity. The effect of porosity has been studied on the same samples of limestones, and the magnitude of the seismo-electric signal increases with increasing porosity in the range of 4–12 % (Migunov and Kokorev, 1977). But another study showed a decrease of the SE effect with increasing porosity on limestones and sandstones (Ageeva et al., 1999). The effect of porosity was studied on samples of limestone, sandstone, aleurolites, and marl at frequencies of 25 kHz. The authors observed a decrease in the SE effect with increasing concentration C of the NaCl solution or 60 kHz. The authors estimated the transfer function of the electric field (electric field over acceleration) by picking the arrival in time domain, and by a spectral analysis using continuous wavelet transform. Both methods show that these ratios are of the order of 2–7 \(\times 10^{-4} \, \text{V m}^{-2} \text{s}^{-2}\) (depending on the offset to the source) and are rather constant in the water saturation range 0.2–0.9 for imbibition and drainage experiments. None of the tested models for the water-saturation dependence of the SPC could correctly model a constant transfer function in this range of saturation.

7.2 Interfacial response detection

With further developments in the sensitivity of the data acquisition systems, it became possible to detect both the coseismic seismo-electric signal and the interfacial response.

Chen and Mu (2005) developed an experimental set-up composed of a plexiglass box with sand, a piezoelectric transducer excited by an electric square pulse (760 V amplitude and 10 µs width) emitting \(P\) wave with a main frequency of 463 kHz, and platinum disc electrodes (Fig. 17). The elec-
Figure 17. Experimental apparatus. (1) Saturated sand, (2) plexiglass box, (3) shielded wire, (4) ultrasonic source, (5) receiver electrode, (6) reference electrode, (7) free surface (air), (8) receiving set-ups (from Chen and Mu, 2005).

Figure 18. The amplitude of the first kind of seismo-electric conversion as a function of the source–receiver offset. The electrolyte concentration is the NaCl concentration (from Chen and Mu, 2005).

Figure 19. Experimental apparatus with an upper layer of water above a saturated-sand layer (from Block and Harris, 2006).

The electrodes are connected to a preamplifier and the electric field is recorded by an electromagnetic instrument with a sampling rate 0.1 µs. The authors showed that the amplitude of the coseismic conversion within the sand decreases with the increase of the distance between the source and the electrode (Fig. 18) and is in the range of 10–180 µV. According to Eq. (16) the SE signal becomes weaker when the electrolyte concentration is increased, as observed by the authors. Moreover, the SE signal is proportional to the grain acceleration, so it decreases with the increase of the source–receiver offset, the emitting acoustic energy being lower. Chen and Mu (2005) observed both the first kind of seismo-electric conversion in sand, and the interfacial SE conversion between contrast in NaCl solution/NaCl-saturated quartz and water-saturated sand/NaCl-saturated sand. They observed an amplitude of the interfacial response in the range of 5–10 µV.

Another study was performed, by Block and Harris (2006), on sand to detect the interfacial response between water and saturated sand. The experimental set-up developed is a cylindrical PVC tube (2 m height), with nine Ag/AgCl electrodes. The source is a 100 kHz submersible acoustic transducer driven by a sine wave (Fig. 19). The electric signals are amplified 60 dB, averaged 1000 times, and filtered with a band-pass between 2 and 500 kHz to remove unwanted noise. The authors observed the first kind of seismo-electric conversion, which is the transmitted acoustic wave corresponding to the Biot fast wave (Fig. 20), and also the interfacial response (IR). This electric signal is generated at the fluid–sand interface, propagates the velocity of the electromagnetic wave in the fluid and sediment, and is recorded almost simultaneously at each one of the electrodes along the vertical array (Fig. 20). The amplitude of this IR is about 200 µV within the water, about 800 µV within the sediments for a water conductivity of 5.2 × 10⁻³ Sm⁻¹, and about 20 µV within the water and 500 µV within the sand for a water conductivity 7.6 × 10⁻³. The authors deduced the peak of the efficiencies (in nV Pa⁻¹) of the fast wave potentials as a function of the
bulk conductivity (Fig. 21) and the IR responses of about 100 µV correspond to efficiencies greater than 30 nV Pa$^{-1}$.

Liu et al. (2008) detected a SE conversion at a frozen–unfrozen interface. The authors developed an experimental set-up with an upper frozen sand layer over an unfrozen sand layer saturated with water. The acoustic sources are 48 kHz $P$ wave source transducers driven by a square electric pulse with a width of 100 µs. They are located at the surface of the upper layer and can be used as near and far sources. The electric field is measured by six electrodes located at the bottom of the frozen layer. The coseismic conversion linked to the electric field moving along with the acoustic wave propagation in the frozen part was detected, and its amplitude decreases with the increasing temperature of the frozen sand layer from $-8$ to $-4\,^\circ C$. The maximum amplitude is of the order of 100 µV. The authors suggested that this localized signal may have an origin in the electromagnetic induction rather than in local streaming potential because the frozen part is a non-conductive medium. The interfacial response was also detected, but only after 8 h of the interface being formed. The authors concluded that the formation of the electric double layer at the interface requires typically a duration of several hours.

Schakel et al. (2011) detected an interfacial response between water and a glass porous sample inside a water tank. They measured the waveform and the amplitude of the IR parallel and perpendicular to the interface. In this geometry, the electric field is created only by the conversion from the interface, so that there is no interference with the body wave coseismic fields. They showed a decrease of the signal with increasing distance to the interface, and a decrease of the signal on both side of the excitation point along the interface, resembling to the pressure pattern. These waveform and spatial amplitude pattern could be well reproduced by a source pressure modelling based on the Sommerfeld approach and Pride’s theory (Aki and Richards, 2002; Brekhovskikh, 1960), taking into account only the reflected electric potential wave, whereas the approximation of the electric dipole overestimated the amplitude decays.

Recently, using the same experimental set-up, an interface between an oil-saturated and a water-saturated porous glass filter samples was detected (Smeulders et al., 2014). As the oil-water front moved, this initial interface and the corresponding IR vanished. Therefore this experiment showed that a purely mechanical contrast at the interface without electrical contrast in these conditions could not induce a detectable IR. Moreover, the authors could detect an IR between a water-saturated Fontainebieu sandstone and a water or oil layer. The amplitude of the interface rock/water was measured to be about 50–75 µV, and the one of the interface rock/oil was about 10 µV. Although the oil conductivity is
lower than the water conductivity, the electric contrast between the water-saturated sandstone and oil may be lower than the one between the water-saturated sandstone and the water, leading to a decrease of the amplitude of the IR.

7.3 Seismo-magnetic detection

To measure the magnetic field, induction detectors of the solenoidal and toroidal types can be used, making possible to measure the axial and transverse components of the magnetic field. Migunov and Kokorev (1977) showed that the SE signals recorded by the induction detectors have the same form as the signal recorded by electrodes, but are weaker in intensity. Note that it has been already suggested to monitor the magnetic field in boreholes to detect fluid flow variations in an accretionary prism (Jouniaux et al., 1999).

Bordes et al. (2006, 2008) showed the existence of seismo-magnetic conversions, predicted by the theory since 1994. The authors developed an experimental set-up with a remote-controlled seismic source, to induce seismic wave propagation in a saturated sand column (Fig. 22). This study was performed in the Low Noise Underground Laboratory (LSBB-Laboratoire Souterrain a Bas Bruit) providing low-noise environment for the electric, magnetic, and acoustic fields. The magnetic part of the SEM conversions is measured besides the electric field. The seismo-electric field is shown to be coupled to the P wave propagation and extension waves, propagating at a velocity of 1300 m s$^{-1}$. The seismo-magnetic field is shown to be coupled to the transverse S wave, propagating at a velocity of 800 m s$^{-1}$. The observed amplitudes are 10 µV m$^{-1}$ (Bordes et al., 2006) and 0.035 nT for a 1 m s$^{-2}$ seismic source acceleration (0.1 g) (Fig. 23). Therefore these observations confirm the theory from Pride (1994) who demonstrates that the observed coseismic electric field is coupled to the compressional waves and that the observed coseismic magnetic field is coupled to the S waves.

7.4 Crosshole measurements and fracture detection

The seismo-electric conversion was also observed in model wells (Zhu et al., 1999; Zhu and Toksöz, 2003) and it was experimentally shown that seismo-electric logging could be a new bore-hole logging technique. Experimental observations using a piezoelectric source within the borehole showed coseismic signals detected by an electrode in the borehole’s centre or within the borehole wall (Zhu et al., 1999); it was shown that the apparent velocities of the SE signal are the same as those of the seismic waves: the Stoneley wave and the low-frequency component of the P wave. It was also shown that these SE signals were either not detected or were of very low amplitude in material of low porosity and low permeability such as lucite and slate (Zhu et al., 1999).

On the other hand, Zhang et al. (2005) measured a seismo-electric conversion induced by pseudo-Rayleigh waves, in a large borehole experiment of 2 m in length, 0.5 m in diameter, and 1.12 m in borehole diameter. This conclusion was deduced because of two dominant frequency crests observed in the seismo-electric signal. Moreover, contrary to the theory and modelling, only the interfacial response (linked to the borehole wall) was detected. The interfacial response was detected at 500 µV using distilled water, and at about 150–200 µV using a water conductivity of 1 Sm$^{-1}$.

Zhu and Toksöz (2003) investigated the relationship between the interfacial signal induced at the fracture and the fracture aperture. They performed laboratory experiments in...
cross-borehole models using one sample of Lucite and one sample of sandstone separated by a vertical fracture. Both samples are saturated with water and the fracture is filled with water. A $P$ wave, whose energy focuses in the horizontal direction, perpendicular to the well, is applied on the side of the Lucite block. It is shown that the amplitude of the interfacial response at the fracture is increased from 50 to 200 $\mu$V for a fracture aperture from 0.5 to 9 mm, respectively, using tap water of $0.1 \text{ S m}^{-1}$ of conductivity. And it is also shown that the SE interfacial response is induced at the sandstone side of the fracture and is generated mainly by a Stoneley wave excited in the fracture. Zhu and Toksöz (2003) also investigated the effect of a dipping fracture between the boreholes (Fig. 24), and showed that the fracture position can be determined from the SE interfacial response induced at the fracture. The electric signal is measured at a fixed position when the source moves in the first block with 1 cm of increment. The results are shown in Fig. 25: a SE signal is observed with a velocity of 2600 $\text{m s}^{-1}$, which is the $P$ waves velocity of Lucite. This is the interfacial response at the fracture at the sandstone side. The distance from the borehole within the Lucite to the fracture side (at position 1) is calculated from the first arrival time 25.5 $\mu$s (in trace 1), knowing the velocity in Lucite and in water ($1500 \text{ m s}^{-1}$) and is de-
Figure 25. Seismo-electric signals recorded at electrode 2 when the source moves from position 1–8. The amplitude is normalized by 14 µV. The arrival at a velocity 2600 m s\(^{-1}\) is the interfacial response of the fracture at the sandstone side (from Zhu and Toksöz, 2003).

Experimental borehole investigations have also shown the utility of the SE signal to eliminate the Logging While Drilling (LWD) tool mode in order to access to the formation acoustic modes (Zhan et al., 2006b). Indeed the tool waves mode present in the LWD acoustic signal are not present in the SE signal excited by the LWD acoustic waves, because the drill string is grounded during the LWD process. Therefore the acoustic modes can be filtered by correlation between the acoustic signal and the SE signal (Zhan et al., 2006a).

7.5 Permeability deduction

A first attempt to deduce permeability from transient streaming potential measurements was proposed by Chandler (1981) in the quasi-static limit. Streaming potential and fluid pressure have identical temporal behaviour in low-frequency domain. Chandler (1981) showed that the time characteristic of the transient streaming potential could be used to deduce the diffusivity, and then the permeability.

A reliable permeability log within an experimental borehole has been deduced from electrokinetic measurements, using an acoustic source (Fig. 26). It has been shown that the normalized coefficient defined by the electric field divided by the pressure \( [\text{V Pa}^{-1} \text{m}^{-1}] \) depends on the permeability, through a finite element model and laboratory experiments (Singer et al., 2005). A short steel tube near the top of the borehole that was hit on its top with a hammer was used as the source. The main wave propagation is a Stoneley wave which induces the electric field. The logging tool is moved step-by-step within the borehole (Fig. 26). The investigated depth of such a permeability is of the order of centimetres. The normalized coefficient is coherent with the electrokinetic coupling \( L_{ek} \) (Eq. 23) per unit of conductance [S]. Therefore it should increase with increasing permeability. At low permeability the fluid is not easily displaced and the oscillating source induces a larger solid displacement. However, the relative movement between the fluid and the solid is limited, leading to a decrease of the electric field even if pressure increases, so that this normalized coefficient is decreased. The measured amplitude of the normalized coefficient on sandstones is in the range of \( 1.6 \times 10^{-7} \) to \( 2.5 \times 10^{-6} \) [V Pa\(^{-1}\) m\(^{-1}\)], increasing with increasing permeabilities from \( 6.2 \times 10^{-15} \) to \( 2.2 \times 10^{-12} \) m\(^2\). This model
showed that the normalized coefficient could detect a 0.5 m-thick bed of permeability $10^{-15}$ m$^2$ within a formation of permeability $10^{-18}$ m$^2$.

On the other hand, Guan et al. (2013) modelled the co-seismic conversion of Stoneley waves within a borehole and showed that the ratio of the converted electric field to the pressure is sensitive to the porosity rather than to the permeability. This ratio is increased by a factor of 2 for increasing porosity from 10 to 30%. The Stoneley wave being sensitive to the permeability, Guan et al. (2013) further investigated the phase of the ratio of the converted electric field to the pressure, and showed that the tangent of this phase is sensitive to the permeability. They showed that the phase of the electric field always lags behind that of pressure in the frequency range up to 5 kHz and there is a frequency about 1 kHz for which the tangent of thus phase is minimum. At this frequency the tangent can be increased in absolute value by a factor when permeability increased from 500 to 50 mD, leading to a possible permeability inversion method. Such a permeability inversion should be tested from borehole SE signals observed in the field on in laboratory.

### 7.6 Electro-seismic detection

Electro-seismic “coseismic” conversions were observed in experimental saturated borehole with a Lucite block (of porosity zero) and a glued-sand (Zhu et al., 1999). The electric current was injected either within the borehole or in the borehole wall, and the $P$ waves receiver was located within the borehole. It was shown that the induced acoustic field was a Stoneley wave.

Zhu et al. (2008) pointed out that there is an acoustic field near the electrodes of injection, which is not an electro-seismic conversion, but linked to the thermo-dilatation of the water molecules when the current is injected. These authors could observe an electro-seismic conversion at an interface between an epoxy-glued sand saturated with tap water and a Lucite block. The electrodes were buried in the sand and the acoustic receiver was at the bottom of the Lucite block. An electric square pulse of 500 V amplitude and 6 $\mu$s width was applied. In case of a sample immersed in a water tank, with the injection electrodes within the water, the authors suggested to better use a single sine burst wave as an electric source than a continuous sine wave, with a center frequency of 100 kHz.

### 8 Conclusions and perspectives

Since its foundations in the late first half of the last century, seismo-electromagnetics has experienced important developments, contributions to its deeper understanding coming from field and laboratory experiments, as well as theoretical developments and numerical modelling. Nowadays we understand the genesis of the electrokinetic coupling and the influence of the fluids and solid matrix on its behaviour; the characteristics of the electromagnetic properties and mechanical signals involved, their detection and processing, although the challenge of this method still remains the weak signal strength and low signal-to-noise ratio. Indeed a lot of field studies could detect shallow interface responses, whereas few studies could detect deep interfacial responses. Field observations showed the advantages of performing 3-component measurements of the SE field, and vertical SE profiles, to better detect small interfacial responses.

Recent laboratory experiments evidenced the existence of the interfacial response, at interfaces such as water/saturated porous medium; porous media saturated with different fluids (different salinities, oil); or frozen/unfrozen sand. Moreover, the theoretical prediction of the seismo-magnetic conversion coupled to the transverse $S$ wave was also experimentally verified.

Still in terms of absolute amplitudes of the SEM signals, theory/modelling and observations often do not match, indicating that the seismo-electromagnetic theory is not perfect yet and needs improvements and further studying.

The results we summarized in this review show that this research area is a strong and healthy one, and that there are a number of open questions still to be addressed, for example the electrokinetic coupling under partial saturation conditions involving wetting and non-wetting fluids, the interface response related to shear waves, the detection of SEM conversions in the field, crosshole investigations, optimized configuration, strong sources without electromagnetic noise, or enhancement of the electric signals by new electrode configurations. Moreover further numerical developments are needed for 2-D and 3-D full-waveform modelling for heterogeneous media, as for borehole configurations, and to move towards the inversion.

Societal questions involving a better characterization of the fluids, and a better knowledge of the subsurface in terms of porosity, permeability, fractures, such as applications on the environment and energy domains, should gain answers from future research on this method.

**Acknowledgements.** We thank CNRS, CONICET, the University of Strasbourg, and the National University of La Plata. We are also grateful to an anonymous reviewer and to Niels Grobbe, whose detailed comments allowed us to improve our paper.

Edited by: A. Cerda
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