I. INTRODUCTION

Due to its large mass, the top quark is speculated to play a special role in electroweak symmetry breaking (EWSB). New physics connected with EWSB can manifest itself in top-quark observables. For instance, top-quark couplings can be modified significantly in some extensions of the Standard Model (SM). A measured yield of top-quark pair production in association with a photon ($t\bar{t}\gamma$) can constrain models of new physics, for example those with composite production in association with a photon ($\gamma$) (SM). A measured yield of top-quark pair production in association with a photon ($t\bar{t}\gamma$) can be modified significantly in some extensions of the SM. For instance, top-quark couplings to new physics connected with EWSB can manifest itself in a special role in electroweak symmetry breaking (EWSB).

Observation of top-quark pair production in association with a photon and measurement of the $t\bar{t}\gamma$ production cross section at $\sqrt{s} = 7$ TeV using the ATLAS detector

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A search is performed for top-quark pairs ($t\bar{t}$) produced together with a photon ($\gamma$) with transverse energy greater than 20 GeV using a sample of $t\bar{t}$ candidate events in final states with jets, missing transverse momentum, and one isolated electron or muon. The data set used corresponds to an integrated luminosity of 4.59 fb$^{-1}$ of proton-proton collisions at a center-of-mass energy of 7 TeV recorded by the ATLAS detector at the CERN Large Hadron Collider. In total, 140 and 222 $t\bar{t}\gamma$ candidate events are observed in the electron and muon channels, to be compared to the expectation of 79 ± 26 and 120 ± 39 non-$t\bar{t}\gamma$ background events, respectively. The production of $t\bar{t}\gamma$ events is observed with a significance of 5.3 standard deviations away from the null hypothesis. The $t\bar{t}\gamma$ production cross section times the branching ratio (BR) of the single-lepton decay channel is measured in a fiducial kinematic region within the ATLAS acceptance. The measured value is $\sigma_{t\bar{t}\gamma}^{\text{fid}} \times \text{BR} = 63 \pm 8 \text{(stat)} +13_{-12}^{+17} \text{(syst)} \pm 1 \text{(lumi)} \text{fb}$ per lepton flavor, in good agreement with the leading-order theoretical calculation normalized to the next-to-leading-order theoretical prediction of 48 ± 10 fb.

The paper is organized as follows. The ATLAS detector is briefly described in Sec. II. The data and Monte Carlo simulation samples used in the analysis are described in Sec. III, followed by a description of the event selection in Sec. IV. The definition of the fiducial phase space used in the measurement is presented in Sec. V. The cross section is extracted from a template-based profile likelihood fit using the photon track-isolation distribution as the discriminating variable. Section VI details the overall strategy of the measurement, and describes how prompt-photon and background templates are obtained. Background estimates are discussed in Sec. VII. An overview of the systematic uncertainties in the measurement is presented in Sec. VIII. Section IX presents the results of the measurement, followed by conclusions in Sec. X.

II. DETECTOR

A detailed description of the ATLAS detector can be found in Ref. [3]. The innermost part of the detector is a tracking system that is immersed in a 2 T axial magnetic field and measures the momentum of charged particles within a pseudorapidity range of $|\eta| < 2.5$. The inner detector (ID) comprises silicon pixel and microstrip...
detectors, and a transition radiation tracker. The calorimeter system is composed of sampling electromagnetic and hadronic compartments with either liquid argon or scintillator tiles as the active media. It resides outside the ID, covering $|\eta| < 4.9$. The outermost system is a muon spectrometer that is used to identify and measure the momentum of muons in a toroidal magnetic field in the region $|\eta| < 2.7$, with detectors used for triggering within $|\eta| < 2.4$. A three-level trigger system selects the potentially interesting events that are recorded for offline analysis.

### III. DATA AND MONTE CARLO SAMPLES

Data recorded by the ATLAS detector in 2011 in $pp$ collisions at $\sqrt{s} = 7$ TeV are considered for analysis. Requirements are imposed on the collected data to ensure the quality of the beam conditions and detector performance. The total integrated luminosity of the analyzed data sample is $L = 4.59 \pm 0.08$ fb$^{-1}$ [4].

Monte Carlo simulation samples are used to study signal and background processes, using the ATLAS detector simulation [5] based on the GEANT4 program [6]. To simulate events of multiple $pp$ interactions per bunch crossing (“pileup”), all Monte Carlo events are overlaid with additional inelastic events generated with PYTHIA [7] using the AMBT1 set of parameters (tune) [8]. The events are then reweighted to match the distribution of the mean number of interactions per bunch crossing in the data. Simulated events are reconstructed in the same manner as the data.

Signal $t\bar{t}\gamma$ events with single-lepton ($\ell\nu_q q \bar{q} b\bar{b} \gamma$, $\ell \equiv e, \mu, \tau$) or dilepton ($\ell\nu_\ell \ell'\nu_\ell \bar{b} \bar{b} \gamma$, $\ell/\ell' \equiv e, \mu, \tau$) final states are simulated with two independent leading-order (LO) matrix element (ME) Monte Carlo generators, WHIZARD v1.93 [9,10] and MADGRAPH v5.1.5.12 [11], both using the CTEQ6L1 [12] LO parton distribution function (PDF) set. Both calculations take into account interference effects between radiative top-quark production and decay processes. Details on the generator-level settings of the two signal Monte Carlo samples are available in Sec. A1. In the $t\bar{t}\gamma$ and inclusive $t\bar{t}$ samples the top-quark mass is set to $m_t = 172.5$ GeV.

The WHIZARD sample is interfaced to HERWIG v6.520 [13] for the parton showering and JIMMY 4.31 [14] is used for the underlying-event simulation. The AUET2 tune [15] is used. The MADGRAPH sample is interfaced to either the PYTHIA v6.425 parton shower using the PERUGIA 2011 C tune [16], or with HERWIG v6.520 and JIMMY 4.31 for the parton showering and the underlying-event simulations, respectively. PYTHIA QED final-state radiation (FSR) from charged hadrons and leptons is switched off and instead PHOTOS v2.15 [17] is used.

To compare with the experimental measurement, the LO calculations of WHIZARD and MADGRAPH are normalized to the next-to-leading-order (NLO) cross section, obtained for $\sqrt{s} = 7$ TeV at the renormalization and factorization scales of $m_t$. The NLO QCD calculation of top-quark pair production in association with a hard photon is detailed in Sec. A 2. The systematic uncertainty on the NLO cross section is obtained by simultaneous renormalization and factorization scale variations by a factor of two ($m_t/2$ and $2m_t$) around the central value ($m_t$), and is calculated to be 20% [18]. The NLO/LO correction ($K$-factor) calculation is performed in a phase-space region close to the one defined by the analysis kinematic selection criteria (see Sec. A 2 for details). The dependence of the $K$ factor on the kinematic variables is small compared to the scale uncertainty [18].

The effect of the variations of photon radiation settings in MADGRAPH is studied using a sample generated with a minimum separation in $\eta-\phi$ space between the photon and any other particle of $\Delta R > 0.05^2$ instead of $\Delta R > 0.2$ used in the default sample (see Sec. A 1). For this sample, PYTHIA QED FSR is switched off and no additional photon radiation is produced by PHOTOS v2.15. In addition to the default MADGRAPH+PYTHIA Monte Carlo sample generated at the scale of $m_t$, samples at scales of $m_t/2$ and $2m_t$ are produced to study the effect of scale variations.

The simulated sample for inclusive $t\bar{t}$ production is generated with MC@NLO v3.1 [19,20] (NLO ME $2 \to 2$) interfaced to HERWIG v6.520 for the parton showering and fragmentation and to JIMMY 4.31 for the underlying-event simulation, using the CTEQ6L1 [21] PDF set, with additional photon radiation simulated with PHOTOS v2.15. This sample is used to validate distributions of kinematic variables in $t\bar{t}$ candidate events as described in Sec. IV.

Initial- and final-state QCD radiation (ISR/FSR) variations are studied using inclusive $t\bar{t}$ samples generated with ACERMC v3.8 [22] interfaced to PYTHIA v6.425 with the CTEQ6L1 PDF set. In these samples the parameters that control the amount of ISR/FSR are set to values consistent with the PERUGIA Hard/Soft tune in a range given by current experimental data [23]. ACERMC v3.8 $t\bar{t}$ samples interfaced to PYTHIA v6.425 are also used to study variations of color reconnection using the PERUGIA 2011 C and PERUGIA 2011 NO CR tunes [16]. The underlying-event variations are studied using ACERMC v3.8 interfaced to PYTHIA v6.425 with two different underlying-event settings of the AUET2B [24] PYTHIA generator tune. In all these ACERMC v3.8 samples, photon radiation is simulated with PHOTOS v2.15 [17]. The inclusive $t\bar{t}$ signal samples are normalized to a predicted Standard Model $t\bar{t}$ cross section of $\sigma_{t\bar{t}} = 177^{+10}_{-11}$ pb for a top-quark mass of 172.5 GeV, as obtained at next-to-next-to-leading order (NNLO) in QCD including resummation.

\[ \Delta R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2} \]
of next-to-next-to-leading-logarithmic (NNLL) soft gluon terms with Top++ v2.0 [25–30].

Background samples of W and Z bosons (including W + b̄b and Z + b̄b processes) are generated with ALPGEN v2.13 [31] interfaced to HERWIG v6.520, using the CTEQ6.1L PDF set. The ALPGEN matrix elements include diagrams with up to five additional partons. The MLM [31] parton-jet matching scheme is applied to avoid double counting of configurations generated by both the parton shower and the LO matrix-element calculation. In addition, overlap between heavy-flavor quarks that originate from ME production and those that originate from the parton shower is removed. Diboson (WW, WZ, and ZZ) production is modeled using HERWIG v6.520 and the MRST LO** PDF set [32]. The Wγ + jets and Zγ + jets (with up to three partons including b̄b, c̄c, e) processes are generated with SHERPA v1.4.0 [33] and the CT10 [34] NLO PDF set. Single-top-quark production is modeled using ACERMC in the t channel and MC@NLO v3.41 [35] for the Wt and [36] s channels.

Multijet samples with jet pT thresholds of 17, 35 and 70 GeV are generated using PYTHIA v6.421 with the AUET2B [24] generator tune.

IV. OBJECT AND EVENT SELECTION

Events for the analysis are selected by requiring a high-pT single-electron or single-muon trigger [37] for the electron and muon channels, respectively. The pT threshold for the muon trigger is 18 GeV, the thresholds for the electron trigger are 20 or 22 GeV, depending on the data-taking period due to changing LHC luminosity conditions. The event reconstruction makes use of kinematic variables such as transverse momentum (pT), energy in the transverse plane (E_T) and pseudorapidity (η) of photons, leptons (e and μ) and jets (j) as well as b-tagging information, and missing transverse momentum (E_T^{miss}).

The selected events are required to contain a reconstructed primary vertex with at least five associated tracks, each with pT > 0.4 GeV. The primary vertex is chosen as the vertex with the highest \( \sum p_T^2 \) over all associated tracks.

Photons are required to have E_{T} > 20 GeV and [\eta] < 2.37, excluding the transition region between the barrel and end-cap calorimeters at 1.37 < |\eta| < 1.52, and must satisfy tight identification criteria [38,39]. Specifically, requirements on the electromagnetic shower shapes [40] are applied to suppress the background from hadron decays (e.g., \( \pi^0 \to \gamma \gamma \) decay leads to two overlapping showers as opposed to a single shower produced by a prompt photon).

Electrons [41] are reconstructed by matching energy deposits in the electromagnetic calorimeter with tracks in the ID, and are required to have E_{T} > 25 GeV and [\eta] < 2.47, excluding the transition region between the barrel and end-cap calorimeters. Muons [42] are reconstructed by matching tracks in the ID with tracks measured in the muon spectrometer, and are required to have p_{T} > 20 GeV and [\eta] < 2.5.

Leptons are required to be isolated to reduce the number of lepton candidates that are misidentified hadrons or nonprompt leptons. To calculate the isolation of electrons in the calorimeter, the E_{T} deposited in the calorimeter in a cone of size ΔR = 0.2 around the electron is summed, and the E_{T} due to the electron itself is subtracted. The scalar sum of p_{T} of tracks with p_{T} > 1 GeV originating from the primary vertex in a cone of ΔR = 0.3 around the electron direction is also measured, excluding the electron track. Selection requirements are parameterized as a function of the electron η and E_{T} and applied to these two isolation variables to ensure a constant efficiency of the isolation criteria of 90% (measured on Z → e⁺e⁻ data) over the entire (η, E_{T}) range. For muons, the transverse energy deposited in the calorimeter in a cone of ΔR = 0.2 around the muon direction is required to be less than 4 GeV, after subtraction of the E_{T} due to the muon itself. The scalar sum of the transverse momenta of tracks in a cone of ΔR = 0.3 is required to be less than 2.5 GeV after subtraction of the muon track p_{T}. The efficiency of the muon isolation requirements is of the order of 86% in simulated \( \tilde{t}\tilde{t} \) events in the muon + jets channel.

Jets [43] are reconstructed from topological clusters [44,45] of energy deposits in the calorimeters using the anti-k, [46] algorithm with a distance parameter R = 0.4. Jets selected for the analysis are required to have p_{T} > 25 GeV and [\eta] < 2.5. In order to reduce the background from jets originating from pileup interactions, the jet vertex fraction, defined as the sum of the p_{T} of tracks associated with the jet and originating from the primary vertex divided by the sum of the p_{T} from all tracks associated with the jet, is required to be greater than 0.75. Since electrons and photons deposit energy in the calorimeter, they can be reconstructed as jets. The jet closest to an identified electron in η-ϕ space is rejected if ΔR(e, j) < 0.2 [47]. Similarly, any jet within ΔR(γ, j) = 0.1 of an identified photon is discarded. To suppress muons from heavy-flavor hadron decays inside jets, muon candidates within ΔR(μ, j) < 0.4 are rejected [47].

Jets containing a b-hadron are identified with a b-tagging algorithm [48–50] using impact parameter and vertex position measurements from the inner detector as inputs to a neural network; b-tagged jets are required to satisfy a selection that is 70% efficient for b-quark jets in simulated \( \tilde{t}\tilde{t} \) events. The misidentification rate of light-flavor partons (u, d, s quark or gluon) is in the range from 1% to 3%, depending on the jet p_{T} and η [48].

The transverse momentum of the neutrinos produced in the top-quark decay chains, measured as missing transverse momentum, is reconstructed from the vector sum of the transverse momenta corresponding to all calorimeter cell energies contained in topological clusters [43] with [\eta] < 4.9, projected onto the transverse plane.
Contributions to $E_T^{\text{miss}}$ from the calorimeter cells associated with physics objects (jets, leptons, photons) are calibrated according to the physics object calibration [51]. The contribution to $E_T^{\text{miss}}$ from the $p_T$ of muons passing the selection requirements is included. Calorimeter cells containing energy deposits above noise and not associated with high-$p_T$ physics objects are also included. Top-quark-pair candidate events are selected by requiring exactly one lepton $\ell$ (where $\ell$ is an electron or muon) and at least four jets, of which at least one must be $b$-tagged. To reduce the background from multijet processes, events in the electron channel are required to have $E_T^{\text{miss}} > 30$ GeV, where $E_T^{\text{miss}}$ is the magnitude of the missing transverse momentum $E_T^{\text{miss}}$, and a $W$-boson transverse mass $m_T(W) > 35$ GeV. This $W$-boson transverse mass is defined as $m_T(W) = \sqrt{2p_T^\ell \times E_T^{\text{miss}}(1 - \cos \phi)}$, where $p_T^\ell$ is the transverse momentum of the lepton and $\phi$ is the azimuthal angle between the lepton direction and the missing transverse momentum vector. Similarly, events in the muon channel are required to have $E_T^{\text{miss}} > 20$ GeV and $m_T(W) + E_T^{\text{miss}} > 60$ GeV. Representative distributions of kinematic variables for this selection are shown in Fig. 1.

The analysis of $t\bar{t}\gamma$ production is performed on the subset of selected $t\bar{t}$ candidate events that contain at least one photon candidate. To suppress the contributions from photons radiated from leptons, photon candidates with $\Delta R(\gamma, \ell) < 0.7$ are discarded. Events with a jet closer than $\Delta R(\gamma, j) = 0.5$ in $\eta-\phi$ space to any photon candidate are discarded, as those photons have a reduced identification efficiency. In addition, to suppress the contribution from $Z(\rightarrow e^+e^-)$ + jets production with one electron misidentified as a photon, the $e\gamma$ invariant mass $m_{e\gamma}$ is required to be $|m_{e\gamma} - m_Z| > 5$ GeV, where $m_Z = 91$ GeV. This selection yields totals of 140 and 222 events in data in the electron and muon channels, respectively. In Fig. 2 the photon candidate $E_T$ distributions for this selection are compared to predictions for the electron and muon channels.

Corrections are applied to simulated samples when calculating acceptances to account for observed differences between predicted and observed trigger, photon and lepton reconstruction and identification efficiencies and jet $b$-tagging efficiencies and mistag rates, as well as smearing to match jet [52], photon and lepton energy resolutions in data [42,53].

V. DEFINITION OF THE FIDUCIAL PHASE SPACE AND CROSS SECTION

To allow a comparison of the analysis results to theoretical predictions, the cross section measurement is made within a fiducial phase space defined in Monte Carlo simulation for $t\bar{t}\gamma$ decays in the single-lepton (electron or muon) final state. The particle-level prediction is constructed using final-state particles with a lifetime longer than 10 ps.

Photons are required to originate from a nonhadron parent, which is equivalent to the requirement for photons to originate from a top-quark radiative decay or top-quark radiative production. Photons are required to have $p_T > 20$ GeV and $|\eta| < 2.37$.

Leptons are defined as objects constructed from the four-momentum combination of an electron (or muon) and all nearby photons in a cone of size $\Delta R = 0.1$ in $\eta-\phi$ space centered on the lepton. Leptons are required to originate
from a nonhadron parent, which is equivalent to the requirement for leptons to originate from the $t \rightarrow Wb \rightarrow ℓνb$ decays. Leptons are required to have $p_T > 20$ GeV and $|η| < 2.5$.

Decays of $t\bar{t}γ$ to the dilepton final states, as well as decays to the single-lepton final state with an electron or muon coming from a $t \rightarrow ℓν$ decays, are considered as nonfiducial and are corrected for when calculating the cross section.

The anti-$k_t$ [46] algorithm with a distance parameter $R = 0.4$ is used to form particle-level jets from all particles with a lifetime longer than 10 ps, excluding muons and neutrinos. Particles arising from pileup interactions are not considered. Jets are required to have $p_T > 25$ GeV and $|η| < 2.5$.

The removal of overlapping particles is performed in a manner consistent with the object and event selection described in Sec. IV. Any jet with $ΔR(ℓ, j) < 0.2$ or $ΔR(γ, j) < 0.1$ is discarded; any muon with $ΔR(μ, j) < 0.4$ is discarded. To suppress the contribution of photon radiation off a charged lepton, photons within $ΔR(γ, ℓ') < 0.7$ are discarded.

For the determination of the $t\bar{t}γ$ fiducial cross section $σ_{t\bar{t}γ}^{fid}$, exactly one lepton (electron or muon), at least one photon, and four or more jets are required. At least one jet must match a $b$-hadron. All simulated $b$-hadrons that are generated with $p_T > 5$ GeV are considered for the match, and are required to satisfy $ΔR(b$-hadron, $j) < 0.4$. Events with $ΔR(γ, j) < 0.5$ are discarded.

The fiducial cross section $σ_{t\bar{t}γ}^{fid}$ is calculated as $σ_{t\bar{t}γ}^{fid} = N/(e \cdot L))$. The number of estimated $t\bar{t}γ$ signal events is $N_s = N - N_b$, where $N$ and $N_b$ are the number of observed $t\bar{t}γ$ candidate events in data and the estimated number of background events, respectively. The efficiency $ε$ is determined from $t\bar{t}γ$ Monte Carlo simulation as the ratio of the number of all events passing the $t\bar{t}γ$ event selection to the total number of events generated in the fiducial region. It is $17.8 \pm 0.5$ (stat)% for the electron channel and $34.3 \pm 1.0$ (stat)% for the muon channel. These numbers include kinematic and geometric acceptance factors, as well as trigger, reconstruction and identification efficiencies. The efficiency values also account for migrations into and out of the fiducial phase space.

VI. ANALYSIS STRATEGY

After the selection more than half of the events do not come from $t\bar{t}γ$ production. The track-isolation distribution of the photon candidates is used to discriminate between signal photons and neutral hadron decays to final states with photons and hadrons misidentified as photons. For simplicity, neutral hadron decays to diphoton final states and hadrons misidentified as photons are referred to hereafter as “hadron-fakes.”

The photon track-isolation variable $p_T^{iso}$ is defined as the scalar sum of the transverse momenta of selected tracks in a cone of $ΔR = 0.2$ around the photon candidate. The track selection requires at least six hits in the silicon pixel and microstrip detectors, including at least one hit in the innermost layer in the pixel detector (except when the track passes through one of the 2% of pixel modules known to be not operational), track $p_T > 1$ GeV, longitudinal
TABLE I. Estimates of the number of selected events with prompt photons, or electrons misidentified as photons, from various backgrounds to $\eta\gamma$ production, including statistical and systematic uncertainties.

<table>
<thead>
<tr>
<th>Background source</th>
<th>Electron channel</th>
<th>Muon channel</th>
</tr>
</thead>
<tbody>
<tr>
<td>$e \rightarrow \gamma$ misidentification</td>
<td>29.4 ± 3.0</td>
<td>41.5 ± 4.6</td>
</tr>
<tr>
<td>Multijet + $\gamma$</td>
<td>1.4 ± 1.2</td>
<td>1.9 ± 1.1</td>
</tr>
<tr>
<td>$W\gamma$ + jets</td>
<td>5.4 ± 1.9</td>
<td>15.6 ± 4.4</td>
</tr>
<tr>
<td>Single top quark + $\gamma$</td>
<td>1.8 ± 0.3</td>
<td>3.8 ± 0.4</td>
</tr>
<tr>
<td>$Z\gamma$ + jets</td>
<td>2.3 ± 1.6</td>
<td>4.2 ± 3.1</td>
</tr>
<tr>
<td>Diboson</td>
<td>0.1 ± 0.1</td>
<td>0.4 ± 0.1</td>
</tr>
</tbody>
</table>

impact parameter $|z_0| < 1$ mm and transverse impact parameter $|d_0| < 1$ mm computed with respect to the primary vertex. The tracks from photon conversions are excluded.

Prompt-photon and background track-isolation templates are obtained from data as described in Sec. VI B and VI C. The total number of events with prompt photon-like objects (for simplicity referred to as “prompt photons” unless noted otherwise) is extracted using a template-based profile likelihood fit. The expected number of non-$\eta\gamma$ events with prompt photons, as summarized in Table I, is subtracted to calculate the fiducial cross section $\sigma_{\eta\gamma}^{\text{fid}}$. These steps are incorporated in a likelihood fit.

A. Likelihood description

A binned template fit maximizes the following extended Poisson likelihood function, representing the Poisson probability to observe $N$ data events given an expectation of $(N_s + N_b)$ events:

$$L(p_T^{\text{iso}}|N_s, N_b) = \frac{(N_s + N_b)^N}{N!} e^{-(N_s + N_b)} \times P(p_T^{\text{iso}}|N_s + N_b) \times \prod_{i=1}^{n} P(N_{b_i}|\hat{N}_{b_i}) \times P_{\text{eff}}(\hat{e} | \hat{e}) \times P_{\text{lum}}(\hat{L} | \hat{C}).$$

For a given variable $x$, $P(x | \hat{x})$ is the probability of $x$ given $\hat{x}$, where $\hat{x}$ denotes the unconditional maximum-likelihood estimate of $x$. Therefore, $P_{\text{eff}}(\hat{e} | \hat{e})$ describes the systematic uncertainties affecting the combined signal efficiency and acceptance $\hat{e}$; $P_{\text{lum}}(\hat{L} | \hat{C})$ describes the uncertainty on the integrated luminosity $\hat{C}$; $P(N_{b_i}|\hat{N}_{b_i})$ describes the uncertainty on the $i$-th background component $b_i$; $n$ is the number of background sources, $N_b = \sum_{i=1}^{n} N_{b_i}$.

The modeling of the signal and the different background sources can be expressed as:

$$P(p_T^{\text{iso}}|N_s + N_b) = f_{sb} F_s(p_T^{\text{iso}}) + (1 - f_{sb}) \sum_{i=1}^{n} F_{b_i}(p_T^{\text{iso}}),$$

where $F_s(p_T^{\text{iso}})$ and $F_{b_i}(p_T^{\text{iso}})$ are the probability density functions (pdf) for the signal and the $i$-th background source, respectively, with $f_{sb} = N_s/(N_s + N_b)$ being the signal purity. Each $F_{b_i}$ is normalized to the corresponding background expectation $N_{b_i}/N_{b}$. Every systematic uncertainty is taken into account as an independent nuisance parameter modeled by a Gaussian pdf $N$. In the likelihood, $\hat{e} = (e_{\text{electron channel}}, e_{\text{muon channel}})$ and $\hat{N}_{b_i}$ are considered to be functions of the nuisance parameters $\theta$ and $\hat{\alpha}_i$, respectively. Taking into account the probability distribution functions modeling the different parameters, the expanded form of the likelihood used to fit $N_{b_i}$ of the $p_T^{\text{iso}}$ distribution for an expectation of $N_j$ events in each bin $j$ spanning the range $V_j$ reads

$$L(p_T^{\text{iso}}|\sigma_{\eta\gamma}^{\text{fid}}, \hat{e}(\theta), \hat{L}, N_{b_1}(\hat{\alpha}_1), \ldots, N_{b_s}(\hat{\alpha}_s)) = \prod_{j=1}^{N_b} \frac{N_{b_j}(\hat{\alpha}_j, \sigma_{\alpha_j})}{\mathcal{N}(\theta_k|\hat{\theta}_k, \sigma_0)} \times \frac{\mathcal{N}(L|\hat{L}, \sigma_{\hat{L}})}{\mathcal{N}(\hat{L}|L, \sigma_l)},$$

where $\nu_j$ is defined as

$$\nu_j = \nu_j(\sigma_{\eta\gamma}^{\text{fid}}, e(\theta), \hat{L}, N_{b_1}(\hat{\alpha}_1), \ldots, N_{b_s}(\hat{\alpha}_s)) = \epsilon(\theta) \frac{\sigma_{\eta\gamma}^{\text{fid}}}{\epsilon(\theta)} \int_{V_j} dp_T^{\text{iso}} F_s(p_T^{\text{iso}}) \; dp_T^{\text{iso}} F_{b_1}(p_T^{\text{iso}}|N_{b_1}(\hat{\alpha}_1)),$$

with $c \equiv \{\text{electron channel, muon channel}\}$, and $i = 1, \ldots, N_{\text{bkg-syst}}$ and $k = 1, \ldots, N_{\text{syst}}$ denoting the systematic uncertainties on the background and the signal efficiency/acceptance, respectively. The normal pdf, modeling the nuisance parameter $x$, is denoted by $N(x | \hat{x}, \sigma_x)$. The $p_T^{\text{iso}}$ binning is chosen to minimize the statistical uncertainty.

Finally, a profile likelihood ratio $\lambda_s$ is built [54,55] by considering the cross section as the parameter of interest and all other parameters to be nuisance parameters:

$$\lambda_s(\sigma_{\eta\gamma}^{\text{fid}}, \nu_j) = \frac{L(p_T^{\text{iso}}|\sigma_{\eta\gamma}^{\text{fid}}, \hat{e}(\theta), \hat{L}, \hat{N}_b(\hat{\alpha}))}{L(p_T^{\text{iso}}|\sigma_{\eta\gamma}^{\text{fid}}, \hat{e}(\theta), \hat{L}, \hat{N}_b(\hat{\alpha}))}.$$
B. Prompt-photon template

The prompt-photon template models the $p_T^{iso}$ distribution of prompt photons as well as electrons misidentified as photons, from $t\bar{t}\gamma$ and background processes. While the same template is used for prompt photons and electrons misidentified as photons, the possible differences are covered by alternative templates used to estimate the systematic uncertainties as discussed below.

Since electron and photon track-isolation distributions are expected to be very similar, the electron template $T_{sig}^{\text{data},e}$ is extracted from the electron $p_T^{iso}$ distribution in $Z \rightarrow e^+e^-$ candidate data events. The prompt-photon template $T_{sig}^{\text{data}}$ is then derived taking into account the differences between electron and photon $p_T^{iso}$ distributions as well as differences between the $Z \rightarrow e^+e^-$ and $t\bar{t}\gamma$ event topologies, as photons from $t\bar{t}\gamma$ events are less isolated than electrons from $Z \rightarrow e^+e^-$ events. To obtain the prompt-photon template, the electron $p_T^{iso}$ distribution in $Z \rightarrow e^+e^-$ candidate data events is corrected using weights ($w_i$) and templates obtained from $Z \rightarrow e^+e^-$ ($T_{MC,e}^{\text{sig},i}$) and $t\bar{t}\gamma$ ($T_{MC,\gamma}^{\text{sig},i}$) Monte Carlo simulations in twelve $p_T \times \eta$ bins (indexed by $i$):

$$T_{sig}^{\text{data}} = T_{sig}^{\text{data},e} + \sum_{i=p_T\times\eta\text{-bins}} w_i(T_{MC,\gamma}^{\text{sig},i} - T_{MC,e}^{\text{sig},i}).$$

The three $p_T$ bins are defined as $20 \text{ GeV} \leq p_T < 30 \text{ GeV}$, $30 \text{ GeV} \leq p_T < 50 \text{ GeV}$, $p_T \geq 50 \text{ GeV}$. The four $\eta$ bins are defined as $0.0 \leq |\eta| < 0.6$, $0.6 \leq |\eta| < 1.37$, $1.52 \leq |\eta| < 1.81$ and $1.81 \leq |\eta| < 2.37$. The relative weight for each bin $i$ is calculated from the photon $E_T$ and $\eta$ spectra of the $t\bar{t}\gamma$ Monte Carlo sample. The prompt-photon template, labeled as “Nominal,” is shown in Fig. 3. It is shown along with an electron $p_T^{iso}$ template obtained from $Z(\rightarrow e^+e^-)+4$-jets candidate data events, and a prompt-photon $p_T^{iso}$ template obtained directly from $t\bar{t}\gamma$ Monte Carlo simulation. The latter two templates are used to estimate systematic uncertainties on the measured cross section due to the choice of the prompt-photon template.

C. Background template

Contributions from background sources with nonprompt photons are described by a single template. This background template is extracted from a multijet data sample by inverting requirements on photon shower shape variables as described in Sec. VI C 1. This set of events is referred to as the “hadron-fake control region.” A correction is applied to account for the prompt-photon contribution in the background template as described in Sec. VI C 2.

1. Derivation

The hadron-fake control region is obtained from multijet events that are required to have either at least two jets with $p_T > 40 \text{ GeV}$ and at least two additional jets with $p_T > 20 \text{ GeV}$, or at least five jets with $p_T > 20 \text{ GeV}$. Nonprompt photon candidates are identified by inverting requirements on the electromagnetic shower shapes [40]. The background template shapes are determined separately in the four photon $\eta$ bins and three photon $E_T$ bins defined in Sec. VI B. The photon $E_T$ distributions are consistent across different $\eta$ regions, so $\eta$ and $E_T$ dependencies of the background template are treated separately.

To match the expected $p_T$ and $\eta$ distributions of nonprompt photons in the signal region, these seven templates are weighted using $\eta$ and $p_T$ distributions of nonprompt photon candidates in $t\bar{t}$ candidate events in data. The resulting background template (labeled as “Nominal template $T_{bkg}^{\text{data}}$”) is shown in Fig. 4.

2. Prompt-photon contribution to the background template

While the nominal background template is extracted using a data-based procedure as described above, the prompt-photon contamination in the background template is obtained using a combination of data and Monte Carlo information.

Multijet simulation is used to obtain a Monte Carlo template modeling the isolation distribution of hadrons misidentified as photons, $T_{MC}^{jj}$, by applying the same object and event selection as for the nominal background template, as described in Sec. VI C 1. A subset of the events used to construct $T_{MC}^{jj}$ is selected by the requirement that those events do not contain any simulated true high-$p_T$ prompt photons. This subset is used to build a template ($T_{MC}^{\text{prompt}}$) which models the isolation distribution of hadrons misidentified as photons without any true prompt-photon contribution.
between modeling the systematic uncertainty due to the differences of prompt photons. The parameter \( f_{\text{MC}} \) expectation of a nuisance parameter template is included in the general likelihood by means uncertainties are obtained at the 68% confidence level (C.L.).

Figure 4 shows the comparison of \( T_{jj}^{\text{MC}} \) to the data-based background template. The systematic uncertainty in each \( p_T^{\text{iso}} \) bin of \( T_{\text{bkg}}^{\text{data}} \) is assigned so that data \( (T_{\text{bkg}}^{\text{data}}) \) and simulation \( (T_{\text{MC}}^{\text{data}}) \) are in agreement. This uncertainty is conservatively taken to be the same for all \( p_T^{\text{iso}} \) bins and is evaluated to be 27\% on values of \( T_{\text{bkg}}^{\text{data}} (p_T^{\text{iso}}) \).

The prompt-photon contamination is then extracted from data by maximizing the following extended likelihood function \( L_f \), representing the probability to observe \( N \) data events in the hadron-fake control region given an expectation of \( n_{\text{exp}} \):

\[
L_f = \frac{n_{\text{exp}}^N}{N!} e^{n_{\text{exp}}} \times \hat{\theta} \left( 1 - f \right) T_{jj}^{\text{MC}} + f T_{\text{sig}}^{\text{data}} \times \mathcal{N}(\theta; \tilde{\theta}, \sigma_\theta),
\]

where \( T_{\text{sig}}^{\text{data}} \) is the prompt-photon template and \( f \) is the fraction of prompt photons. The parameter \( \tilde{\theta} \) is the nuisance parameter modeling the systematic uncertainty due to the differences between \( T_{\text{bkg}}^{\text{data}} \) and \( T_{jj}^{\text{MC}} \). The fraction of prompt photons is distributed according to a Gaussian pdf \( \mathcal{N}(\theta; \tilde{\theta}, \sigma_\theta) \) with mean \( \tilde{\theta} = 1 \) and width \( \sigma_\theta = 27\% \). The result of the fit is shown in Fig. 5, and \( f \) is determined to be \( (6.1^{+1.7}_{-0.9}) \times 10^{-2} \). The uncertainties are obtained at the 68\% confidence level (C.L.) by constructing the confidence belt with the Feldman-Cousins technique [56] using pseudoexperiments.

Finally, the signal contamination in the background template is included in the general likelihood by means of a nuisance parameter \( \alpha_{\text{fake}} \) modeling the strength of the correction:

\[
T_{\text{corr}_{\text{bkg}}} = \left( \frac{1}{1 - \alpha_{\text{fake}} \cdot f} \right) \left[ T_{\text{bkg}}^{\text{data}} - \alpha_{\text{fake}} \cdot f \times T_{\text{sig}}^{\text{data}} \right].
\]

The strength factor \( \alpha_{\text{fake}} \) is constrained to 1 by a Gaussian pdf with width \( \sigma_\alpha = 28\% \) corresponding to the largest of the estimated asymmetric uncertainties on \( f \). It is then determined from the general likelihood fit in a data-based way.

VII. PROMPT-PHOTON BACKGROUNDs

To identify prompt-photon and isolated-electron background contributions to the events selected in the \( t\bar{t} \) analysis, data-based methods and Monte Carlo simulation are used. These background estimates are summarized in Table I and described below.

A. Electron misidentified as a photon

The contribution from events with an electron misidentified as a photon is estimated using data by applying the \( e \to \gamma \) misidentification rate to \( t\bar{t} + e \) candidate events. The measurement of this misidentification probability and cross-checks of the method are described below.

The sample of events with an electron and a photon approximately back-to-back in the transverse plane (in \( \phi \)) with an electron–photon invariant mass \( m_{\gamma\gamma} \) close to the Z-boson mass is dominated by \( Z \to e^+e^- \) decays in which
one of the electrons radiates a high-$E_T$ photon while traversing detector material. The probability for an electron to be misidentified as a photon is determined in data as a function of the electron transverse momentum and pseudorapidity using the $e\gamma$ and $e^+e^-$ mass distributions. One electron (tag) is required to match the single-electron trigger. Another electromagnetic object (probe), an electron or photon, is then required to be present and give a di-object mass with the tag close to the $Z$-boson mass. The $e\gamma$ and $e^+e^-$ mass distributions are fit with the sum of a Crystal Ball function (for the signal part) and a Gaussian function (for the background part) to obtain the numbers of $ee$ and $e\gamma$ pairs, $N_{ee}$ and $N_{e\gamma}$, to which several pairs per event can enter. The probability of an electron being misidentified as a photon is measured in $\eta$ and $p_T$ bins as $f_{e\rightarrow\gamma} = N_{e\gamma}/N_{ee}$. The nominal selection for the signal $t\bar{t}\gamma$ region is modified by replacing the photon requirement by an extra-electron requirement. This extra electron ($e_t$) must fulfill the photon kinematic selection, $E_T(e_t) > 20$ GeV and $|\eta(e_t)| < 2.37$, excluding the transition region between the barrel and end-cap calorimeters at $1.37 < |\eta(e_t)| < 1.52$. To estimate the contribution from an electron misidentified as a photon, these $t\bar{t} + e$ events are reweighted according to the probability of the extra electron being misidentified as a photon. This procedure gives 29.4 ± 3.0 and 41.5 ± 4.6 events in the electron and muon channels, respectively.

The misidentification probability $f_{e\rightarrow\gamma}^{MC}$ is also estimated in $Z \rightarrow e^+e^-$ Monte Carlo simulation, so that a closure test can be performed. The number of background events in simulation that pass the $t\bar{t}\gamma$ event selection is estimated using generator-level information about how the photon is produced. These events are weighted with the data-to-simulation correction factors $s_{e\gamma} = f_{e\rightarrow\gamma}/f_{e\rightarrow\gamma}^{MC}$ found typically to be within 10% of unity. This estimate is found to be in agreement with reweighting the events that pass the $t\bar{t} + e$ event selection in Monte Carlo simulation according to $f_{e\rightarrow\gamma}$, i.e., effectively using the data-based approach in the Monte Carlo simulation.

B. Multijet + photon

The background contribution from multijet events with associated prompt-photon production is estimated using the data-based matrix method discussed in more detail in Ref. [59]. In this method, two sets of lepton selection criteria are defined. The “tight” selection criteria are used to identify leptons in $t\bar{t}\gamma$ candidate events. In the “loose” selection criteria, the lepton isolation requirements are disregarded, and looser identification requirements [40] are applied for electrons.

The number of selected $t\bar{t}\gamma$ candidate events is expressed as a sum of those with prompt leptons and those with “fake leptons” (nonprompt leptons or hadrons misidentified as leptons). Identification efficiencies for prompt leptons are measured in $Z \rightarrow \ell^+\ell^-$ ($\ell \equiv e, \mu$) data candidate events, whereas the efficiency for fake leptons to be identified as “tight” leptons is measured in a multijet data sample. The number of $t\bar{t}\gamma$ candidate events with at least one nonprompt lepton candidate is estimated using this information [59].

A template fit to the photon $p_T^{\gamma}$ distribution is used to determine the prompt-photon fraction in selected multijet+ $\gamma$ events. The multijet + $\gamma$ event selection is similar to the $t\bar{t}\gamma$ selection except that “loose” lepton identification criteria are used instead of the “tight” criteria. Assuming that the prompt-photon fraction does not depend on the lepton identification criteria (“loose” or “tight”), this prompt-photon fraction is then used to estimate the contribution of the multijet + prompt-photon process to the $t\bar{t}\gamma$ event selection. This results in $1.4 \pm 1.2$ and $1.9 \pm 1.1$ events expected for the electron and muon channels, respectively.

C. $W\gamma +$ jets production

Background from $W\gamma +$ jets production is estimated by extrapolating the number of $W\gamma +$ jets candidate events in data from a control region (CR) to the $t\bar{t}\gamma$ signal region (SR) using $W\gamma +$ jets Monte Carlo simulation [60]. In the control region the lepton, photon, $E_T^{\text{miss}}$ and $m_T(W)$ selection criteria are the same as in the nominal $t\bar{t}\gamma$ selection. To enrich the control region in $W\gamma +$ jets, events are required to have one, two or three jets, and a $b$-tagging veto is applied.

To estimate the prompt-photon fraction, it is assumed that the fraction of prompt photons is the same in the CR and SR. To verify this assumption, a template fit to the photon $p_T^{\gamma}$ distribution is performed, and the prompt-photon fraction in data and simulation is found to be independent of the jet multiplicity.

To suppress the $Z +$ jets background contribution in the CR, the $m_{\gamma}$ requirement is extended to $|m_{\gamma} - m_Z| > 15$ GeV. The multijet + $\gamma$ contribution to the $W\gamma +$ jets background in the CR is estimated using the matrix method as described in Sec. VII B. The number of $W\gamma +$ jets events with prompt photons in the CR is estimated using a template fit to the photon $p_T^{\gamma}$ distribution.

Other contributions to the $W\gamma +$ jets CR are estimated using simulation, where events are separated into two classes, one with a prompt photon, the other with an electron misidentified as a photon. To obtain the $e \rightarrow \gamma$ contribution, the $s_{\gamma\gamma}$ correction factors (Sec. VII A) are used. A comparison of data and expectation in the CR is presented in Table II.

The number of $W\gamma +$ jets candidate events in the CR (≤ 3 jets) is extrapolated to the jet multiplicity of the SR, ≥ 4 jets [59]. To extrapolate from the $W\gamma +$ jets event selection, which has a $b$-tagging veto, to the SR, the heavy-flavor quark content is studied in data in events with a $W$ boson and two jets. The heavy-flavor quark content is then extrapolated from the $W\gamma + 2$-jets region into the SR using
which may lead to different event rates after differences in the per-flavor event tagging probabilities, the resulting number of \( W \gamma \) candidate data events, as well as the MC prediction for the number of \( W \gamma \) events are shown. To obtain the \( W \gamma \) + jets background to the \( t\bar{t} \gamma \) selection, the number of \( W \gamma \) candidate data events is extrapolated into the signal region using Monte Carlo simulation. The uncertainties include both the statistical and systematic uncertainties.

### TABLE II. Data and simulated background yields in the \( W \gamma \) + jets data control region.

<table>
<thead>
<tr>
<th></th>
<th>Electron channel</th>
<th>Muon channel</th>
</tr>
</thead>
<tbody>
<tr>
<td>( W \gamma ) + jets control region</td>
<td>3410</td>
<td>8394</td>
</tr>
<tr>
<td>Events with prompt ( \gamma )</td>
<td>2412</td>
<td>5540</td>
</tr>
<tr>
<td>( t\bar{t} \gamma )</td>
<td>82 ± 16</td>
<td>161 ± 32</td>
</tr>
<tr>
<td>( Z + ) jets</td>
<td>160 ± 90</td>
<td>620 ± 330</td>
</tr>
<tr>
<td>Diboson</td>
<td>13 ± 3</td>
<td>26 ± 7</td>
</tr>
<tr>
<td>Single top quark</td>
<td>9 ± 2</td>
<td>20 ± 5</td>
</tr>
<tr>
<td>( e \to \gamma ) misidentification</td>
<td>380 ± 110</td>
<td>330 ± 40</td>
</tr>
<tr>
<td>Multijet + ( \gamma )</td>
<td>60 ± 30</td>
<td>350 ± 70</td>
</tr>
<tr>
<td>Total background</td>
<td>700 ± 140</td>
<td>1510 ± 340</td>
</tr>
<tr>
<td>( W \gamma ) estimate</td>
<td>1710 ± 180</td>
<td>4030 ± 390</td>
</tr>
<tr>
<td>( W \gamma ) MC expectation</td>
<td>1860 ± 200</td>
<td>3930 ± 390</td>
</tr>
</tbody>
</table>

the \( W \gamma \) + jets simulation [59,60]. This extrapolation accounts for the difference in flavor composition between the \( W \gamma \) + 2-jet and \( W \gamma \) + \( \geq 4 \)-jet samples as well as for differences in the per-flavor event tagging probabilities, which may lead to different event rates after \( b \)-tagging. The \( W \gamma \) + jets background estimate is 5.4 ± 1.9 and 15.6 ± 4.4 events for the electron and muon channels, respectively.

Monte Carlo modeling uncertainties in the estimate of the background from \( W \gamma \) + jets production include contributions from the estimated number of events with electrons misidentified as photons, as well as the efficiency uncertainty due to the normalization of \( Z \) + jets in the four-jet bin from the Berends-Giele scaling [60]).

### D. Other background sources

The single-top-quark, \( Z + \) jets, and diboson contributions are estimated from simulation and normalized to theoretical calculations of the inclusive cross sections.

The single-top-quark production cross section is normalized to the NLO + NNLL prediction: the \( t \) channel to 64.6\(^{+2.6}_{-1.7} \) pb [61], the \( s \) channel to 4.6 ± 0.2 pb [62], and the \( Wt \) channel to 15.7 ± 1.2 pb [63]. The \( Z + \) jets background is normalized to the NNLO QCD calculation for inclusive \( Z \) production [64] and the diboson background is normalized to the NLO QCD cross section prediction [65].

### VIII. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties may affect the shapes of the \( p_{T}^{\text{iso}} \) prompt-photon and background templates, the estimates of background components with prompt photons and with electrons misidentified as photons, as well as the efficiencies, acceptance factors and the luminosity.

The total effect of each systematic uncertainty on the cross section is evaluated using ensemble tests. For each systematic uncertainty \( i \), pseudodata are generated from the full likelihood while keeping all parameters fixed to their nominal values except for the nuisance parameter corresponding to the systematic uncertainty source. For each set of pseudodata, a template fit is performed allowing all parameters of the likelihood (nuisance parameters, signal cross section) to vary. The distribution of cross sections obtained form a Gaussian pdf with a width that gives the uncertainty in the cross section due to the \( i \)-th systematic uncertainty. This method provides an estimate of the effect of each uncertainty on the cross section as shown in Table III. Uncertainties obtained with this method are by construction symmetric. All systematic uncertainties are described in the following.

#### A. Template shapes

The contribution to the systematic uncertainty on \( \sigma_{\text{fid}}^{\bar{t}\bar{t}\gamma} \) due to the template shape modeling amounts to 7.6% in total. Of this, the background template shape modeling uncertainty amounts to 3.7% of the cross section, and the prompt-photon template uncertainty amounts to 6.6%.

The prompt-photon template shape systematic uncertainty is estimated with pseudoeperiments by replacing the nominal prompt-photon template with alternative templates shown in Fig. 3: (a) an electron \( p_{T}^{\text{iso}} \) template obtained from \( Z(\rightarrow e^{+}e^{-}) + \geq 4 \)-jets candidate data events (4.1% systematic uncertainty is obtained) and (b) a prompt-photon \( p_{T}^{\text{iso}} \) template obtained directly from \( t\bar{t}\gamma \) Monte Carlo simulation (6.6% systematic uncertainty is obtained). The larger of the two uncertainties is used as the systematic uncertainty.

#### TABLE III. Summary of systematic uncertainties on the \( \bar{t}\bar{t}\gamma \) fiducial cross section, \( \sigma_{\text{fid}}^{\bar{t}\bar{t}\gamma} \).

<table>
<thead>
<tr>
<th>Uncertainty source</th>
<th>Uncertainty [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background template shapes</td>
<td>3.7</td>
</tr>
<tr>
<td>Signal template shapes</td>
<td>6.6</td>
</tr>
<tr>
<td>Signal modeling</td>
<td>8.4</td>
</tr>
<tr>
<td>Photon modeling</td>
<td>8.8</td>
</tr>
<tr>
<td>Lepton modeling</td>
<td>2.5</td>
</tr>
<tr>
<td>Jet modeling</td>
<td>16.6</td>
</tr>
<tr>
<td>( b )-tagging</td>
<td>8.2</td>
</tr>
<tr>
<td>( E_{T}^{\text{miss}} ) modeling</td>
<td>0.9</td>
</tr>
<tr>
<td>Luminosity</td>
<td>1.8</td>
</tr>
<tr>
<td>Background contributions</td>
<td>7.7</td>
</tr>
</tbody>
</table>
The systematic uncertainty associated with the reweighting of the background template is estimated by varying within their uncertainties the nonprompt photon $p_T$ and $\eta$ distributions that are used for reweighting. The effect of this systematic uncertainty on the cross section measurement is found to be negligible. To estimate the systematic uncertainty due to the amount of prompt-photon contamination in the background template (as described in Sec. VI C), the corresponding nuisance parameter $\alpha_{\text{fake}}$ is sampled using a Gaussian pdf with a width of $\alpha_{\text{fake}} = 28\%$ corresponding to its estimated uncertainty. The systematic uncertainty on the cross section is estimated to be 3.7%. All template-shapes uncertainties are taken as fully correlated between the electron channel and the muon channel.

B. Signal modeling

The uncertainty on the $t\bar{t}\gamma$ cross section (as defined in Sec. V) due to the modeling of the signal is estimated to be 8.4%. The estimate is obtained by varying the selection efficiency with respect to the nominal $t\bar{t}\gamma$ Monte Carlo sample which includes event migrations into and out of the fiducial region. This uncertainty includes a comparison of MADGRAPH with WHIZARD (1.7%), as well as a comparison of the MADGRAPH $t\bar{t}\gamma$ samples with different QED FSR settings (3.4%) as explained in Sec. III. The renormalization and factorization scales are also varied, leading to an uncertainty of 1.1%. To assess the effect of different parton shower models, predictions from the MadGraph + HERWIG sample are compared to predictions from the MadGraph + PYTHIA sample, leading to an uncertainty of 7.3%. In addition, studies of $t\bar{t}$ samples with varied color reconnection (0.2%) and underlying event (0.9%) settings lead to small contributions. The uncertainty associated with the choice of the CTEQ6L1 PDF set is evaluated from an envelope of calculations using the PDF4LHC prescription [66] by reweighting the CTEQ6L1 LO PDF used in the generation of the $t\bar{t}\gamma$ WHIZARD sample with MSTW2008 [67,68], CT10 [34,69] and NNPDF2.0 [70] NLO PDF sets and amounts to 1.1%. All signal-modeling uncertainties are taken as fully correlated between the electron channel and the muon channel.

C. Detector modeling

The systematic uncertainty on the cross section due to photon modeling is 8.8%. It is estimated from the photon identification (7.3%) [38], the electromagnetic energy scale (2.7%) and the resolution (4.0%) systematic uncertainties [53].

The systematic uncertainty on the cross section due to lepton modeling is 2.5%. It is estimated separately for the electron and muon channels from the lepton trigger (0.3% and 1.7%), reconstruction (0.5% and 0.4%) and identification (1.2% and 1.0%) efficiency uncertainties, as well as from those on the energy scale (0.3% and 0.3%) and resolution (0.1% and 0.7%).

D. Background contributions

The total systematic uncertainty originating from the non-$t\bar{t}\gamma$ background contributions with prompt photons or electrons misidentified as photons is estimated to be 7.7%. This uncertainty includes the following: electrons misidentified as photons (5.0%), $W\gamma$ + jets (5.4%), as well as multijet + photon (1.5%), $Z\gamma$ + jets (1.3%), diboson (0.4%) and single-top-quark (0.4%) processes. The various sources of uncertainty on the background estimates quoted above are described in the following paragraphs.

For background estimates obtained using simulation, uncertainties on the cross section predictions are taken into account. Cross section systematic uncertainties are considered as fully correlated between the electron and the muon channels. However, the corresponding statistical uncertainty is taken as uncorrelated. For $Z\gamma$ + jets, single-top-quark and diboson contributions the cross section systematic uncertainty is negligible with respect to the statistical uncertainty.

The systematic uncertainty on the probability of an electron to be misidentified as a photon as described in Sec. VII A is obtained by varying the fit functions and the
TABLE IV. Number of $t\bar{t}\gamma$ signal and background events extracted from the likelihood fit, which is performed for the electron and muon channels simultaneously. The uncertainties are statistical and systematic. The total number of $t\bar{t}\gamma$ candidate events observed in data is also shown.

<table>
<thead>
<tr>
<th>Contribution</th>
<th>Electron chan.</th>
<th>Muon chan.</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Signal</td>
<td>52 $\pm$ 14</td>
<td>100 $\pm$ 28</td>
<td>152 $\pm$ 31</td>
</tr>
<tr>
<td>Hadrons</td>
<td>38 $\pm$ 26</td>
<td>55 $\pm$ 38</td>
<td>93 $\pm$ 46</td>
</tr>
<tr>
<td>Prompt photons</td>
<td>41 $\pm$ 5</td>
<td>65 $\pm$ 9</td>
<td>106 $\pm$ 10</td>
</tr>
<tr>
<td>Total background</td>
<td>79 $\pm$ 26</td>
<td>120 $\pm$ 39</td>
<td>199 $\pm$ 47</td>
</tr>
<tr>
<td>Total</td>
<td>131 $\pm$ 30</td>
<td>220 $\pm$ 48</td>
<td>351 $\pm$ 59</td>
</tr>
<tr>
<td>Data candidates</td>
<td>140</td>
<td>222</td>
<td>362</td>
</tr>
</tbody>
</table>

$ee$ and $e\gamma$ mass windows in $Z \to e^+e^-$ candidate events in data. This uncertainty is estimated to be about 10% of the background estimate and it is taken as fully correlated between the electron channel and the muon channel.

For the multijet + photon background described in Sec. VII B, the uncertainty is about 90% for the electron channel and 60% for the muon channel. It is dominated by the statistical uncertainty due to the small number of events in the data samples and the systematic uncertainties on the matrix method (50% for the electron channel and 20% for the muon channel) [59]. Those uncertainties are taken as uncorrelated between the two channels.

The systematic uncertainties on the $W\gamma +$ jets background are dominated by the extrapolation from the control region (dominated by $W\gamma +$ jets) to the signal region due to different event topologies in the two regions in terms of the total number of jets and the number of heavy-flavor jets. The uncertainties due to the extrapolation are 27% in the electron channel and 23% in the muon channel and are dominated by the uncertainty on the knowledge of the flavor compositions of the $W +$ jets events and the overall $W +$ jets normalization for different jet multiplicities [59,60]. Those uncertainties are taken as fully correlated between the electron channel and the muon channel. The statistical uncertainty on the number of events in the $W\gamma +$ jets control region is taken as uncorrelated between the two channels. Systematic uncertainties on the multijet + photon contribution to the $W\gamma +$ jets event selection, as well as uncertainties on Monte Carlo modeling of $t\bar{t}$, $Z +$ jets, diboson, and single-top-quark processes are taken into account [47].

IX. RESULTS

Totals of 140 and 222 $t\bar{t}\gamma$ candidate data events are observed in the electron and muon channels, respectively. The numbers of background events extracted from the combined likelihood fit are 79 $\pm$ 26 for the electron channel and 120 $\pm$ 39 for the muon channel. The numbers of $t\bar{t}\gamma$ signal events are determined to be 52 $\pm$ 14 and 100 $\pm$ 28. The results include statistical and systematic uncertainties. These numbers are summarized in Table IV, and the $p_T^{\gamma}$ distributions are shown in Fig. 6.

Using the asymptotic properties [72] of the likelihood model, the test statistic for the no-signal hypothesis is extrapolated to the likelihood ratio value observed in data (14.1) to determine the p-value of $p_0^{\text{obs}} = 5.73 \times 10^{-8}$. The process $t\bar{t}\gamma$ in the lepton-plus-jets final state is observed with a significance of $5.3\sigma$ away from the no-signal hypothesis.

The $t\bar{t}\gamma$ fiducial cross section together with its total uncertainty is obtained from the profile likelihood ratio fit to be $63^{+10}_{-16}$ fb. The total systematic uncertainty is extracted from $\sqrt{\left(\sigma_{\text{syst(stat)}}\right)^2 - \sigma_{\text{stat}}^2} = 3^{+17}_{-13}$ fb, where $\sigma_{\text{stat}}$ is the luminosity uncertainty; $\sigma_{\text{stat}}$ is the pure statistical uncertainty.
uncertainty, evaluated from the profile likelihood without including nuisance parameters; $\sigma_{\text{syst}}/\sigma_{\text{stat}}$ is the total uncertainty extracted from the 68% C.L. of the profile likelihood fit (including nuisance parameters), as shown in Fig. 7.

The $t\bar{t}$ inclusive cross section times $\text{BR}$ per lepton flavor, as defined in Sec. V, is determined to be $\sigma_{\text{fid}} \times \text{BR} = 63 \pm 8 \text{(stat)} +17 \text{(syst)} \pm 1 \text{(lumi)}$ fb, where BR is the $t\bar{t}$ branching ratio in the single-electron or single-muon final state. Good agreement is found with the predicted cross sections [18,73] of $48 \pm 10 \text{ fb}$ and $47 \pm 10 \text{ fb}$ obtained from the WHIZARD and MADGRAPH Monte Carlo generators, respectively, and then normalized by the corresponding NLO/LO $K$ factors. In addition, the cross section measurements are performed separately in the electron and muon channels and give $\sigma_{\text{fid}} \times \text{BR} = 76_{-15}^{+16} \text{(stat)} +22 \text{(syst)} \pm 1 \text{(lumi)}$ fb and $\sigma_{\text{fid}} \times \text{BR} = 55_{-9}^{+10} \text{(stat)} +11 \text{(syst)} \pm 1 \text{(lumi)}$ fb, respectively.

**X. SUMMARY**

The production of $t\bar{t}$ final states with a photon with transverse energy greater than 20 GeV is observed with a significance of $5.3\sigma$ in proton–proton collisions at $\sqrt{s} = 7$ TeV using the ATLAS detector at the CERN LHC. The data set used corresponds to an integrated luminosity of 4.59 fb$^{-1}$. The $t\bar{t}$ cross section per lepton flavor, determined in a fiducial kinematic region within the ATLAS acceptance defined in Sec. V, is measured to be $\sigma_{\text{fid}} \times \text{BR} = 63 \pm 8 \text{(stat)} +13 \text{(syst)} \pm 1 \text{(lumi)}$ fb in good agreement with the theoretical prediction.

**APPENDIX: $t\bar{t}$ MONTE CARLO SAMPLES**

Signal $t\bar{t}$ events with single-lepton ($\ell\nu_qq^c\bar{b}\bar{b}_f$, $\ell \equiv e, \mu, \tau$) or dilepton ($\ell\nu\ell\nu\bar{b}\bar{b}_f$, $\ell/\ell' \equiv e, \mu, \tau$) final states are simulated with two independent leading-order (LO) matrix element (ME) Monte Carlo generators, WHIZARD v1.93 [9,10] and MADGRAPH v5.1.5.12 [11], both using the CTEQ6L1 [12] LO parton distribution function (PDF) set. Both calculations take into account interference effects between radiative top-quark production and decay processes.

1. **Leading-order calculations: WHIZARD and MADGRAPH**

In the WHIZARD $t\bar{t}$ sample, the minimum transverse momentum of all outgoing partons except for the photon is set to 10 GeV. The transverse momentum of the photon is required to be larger than 8 GeV. The invariant mass of the photon and any charged particle ($u, d, c$ and $s$ quarks,
electrons, muons, and \( \tau \) leptons) is required to be larger than 5 GeV. To avoid infrared and collinear divergences, the following invariant masses are also required to be larger than 5 GeV: \( m(q_1, q_2), m(q_1, q_3), m(q_2, q_3), \) and \( m(q_2, q_3) \), where \( q_1 \) and \( q_2 \) are the quarks from the hadronic decay of one W boson, and \( q_1 \) and \( q_2 \) are the gluons initiating the \( gg \rightarrow \tilde{t}\tilde{\gamma} \) process. For each incoming quark \( Q_i \), \( i = u, d, c, s, \) and \( b \) quark, the invariant mass \( m(Q_i, q_j) \) is required to be larger than 5 GeV if \( q_j \) is the same type of parton as \( Q_i \). The renormalization scale is set to \( 2\mu_r \), and the factorization scale is set to the partonic center-of-mass energy \( \sqrt{s} \). The cross section is 445 fb when summing over all three lepton flavors for the single-lepton \(( e, \mu, \tau \) and 188 fb for the dilepton \( \tilde{t}\tilde{\gamma} \) final states.

In the MadGraph \( \tilde{t}\tilde{\gamma} \) sample, the minimum transverse momentum is set to 15 GeV for \( u, d, c \) and \( s \) quarks, as well as for photons, electrons, muons and \( \tau \) leptons. The distance in \( \eta-\phi \) space between all these particles is required to be \( \Delta R > 0.2 \). For \( b \) quarks, no requirement is placed on the transverse momentum or on the pseudorapidity. Leptons and photons are required to have \( |\eta| < 2.8 \), while \( u, d, c \) and \( s \) quarks are required to have \( |\eta| < 5.0 \). The renormalization and factorization scales are set to \( \mu_r \). The cross section is 445 fb when summing over all three lepton flavors for the single-lepton and 131 fb for the dilepton \( \tilde{t}\tilde{\gamma} \) final states.

2. Next-to-leading-order calculation

The NLO QCD calculation of top-quark pair production in association with a hard photon is described in Ref. [73] for \( \sqrt{s} = 14 \) TeV. A dedicated calculation at \( \sqrt{s} = 7 \) TeV both at LO and at NLO has been performed for this analysis [18] for the \( pp \rightarrow b\mu^+\nu_\mu, \bar{b}jj\gamma \) channel using the same settings for the renormalization and factorization scale as in the WHIZARD \( \tilde{t}\tilde{\gamma} \) calculation.

The following NLO input parameters are used: top-quark mass \( m_t = 172 \) GeV, top-quark width \( \Gamma_t = 1.3237 \) GeV, W-boson mass \( m_W = 80.419 \) GeV, W-boson width \( \Gamma_W = 2.14 \) GeV, fine-structure constant \( \alpha = 1/137 \). The strong-coupling constant \( \alpha_s(\mu) \) is evaluated using the two-loop running from \( \alpha_s(m_Z) \) as specified in the MSTW2008 NLO PDF. Jets are defined using the anti-\( k \)-algorithm with a distance parameter \( R = 0.4 \). The photon is required to be separated from hadronic activity as defined in Ref. [74].

The phase-space requirements used in the \( \sqrt{s} = 7 \) TeV theory LO and NLO calculations are described below. The muon is required to have \( p_T(\mu) > 20 \) GeV and \( |\eta(\mu)| < 2.5 \). The missing transverse momentum is required to be \( E_T^{\text{miss}} > 25 \) GeV and \( E_T^{\text{miss}} + m_W^2 > 60 \) GeV, where \( m_W \) is the W-boson transverse mass. Jets are required to have \( p_T(j) > 25 \) GeV and \( |\eta(j)| < 2.5 \). The photon is required to be separated in \( \Delta R : \Delta R(\text{jets}) > 0.4, \Delta R(\mu, \text{jets}) > 0.4, \Delta R(\gamma, \mu) > 0.4, \Delta R(\gamma, \text{jets}) > 0.5 \). The event is required to have \( N_{\text{jets}} \geq 4 \).

With the above setup and assuming 100% efficiencies, \( \sigma^{\text{NLO}}_{pp} = 24.5^{+5.6}_{-4.9} \) pb and \( \sigma^{\text{LO}}_{pp} = 14.7^{+3.8}_{-2.8} \) pb. Upper and lower values correspond to scale variations by a factor of two around \( \mu = m_t \). Therefore, for \( \mu = m_t \) the NLO/LO \( K \) factor is 1.67. Similarly, for the WHIZARD Monte Carlo sample scales and NLO calculation at the scale of \( \mu = m_t \), the NLO/LO \( K \) factor is 2.53.

The LO cross sections calculated with the WHIZARD and MadGraph Monte Carlo generators are multiplied by the corresponding \( K \) factors in order to compare with the experimental measurement.

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