Translating Fork Specifications into Logic Programs

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Abstract

In this work a compiler from fork specifications into logic programs is presented. The technique implemented by the compiler consists of transforming a set of fork equations (with some restrictions) into normal logic programs in such a way that the semantics of the fork equations is preserved. After translating a fork specification, it can be executed by consulting the generated logic program. The fork compiler, a tool for the translation, is also introduced.

1 Introduction

Fork algebras are a kind of algebras of binary relations especially developed for program specification and construction [3]. Every relation in this formalism represents a program, relating the input data (problem domain) with the output data (solutions). Fork algebras have several important properties [4][6]. One of their main features as specification language is their relational nature, which allows to write specifications very easily, especially for non-deterministic tasks [5]. The main property of (abstract) fork algebras as environment for calculating programs is the representability of abstract fork algebras into proper ones [7]; due to this property, the programmer can port knowledge from the problem domain to the abstract calculus.

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However, fork algebras, as many other formal languages, are not widely used, partly because of the absence of software tools for development within the methodology.

There exist some software tools for supporting relational methods, such as RELVIEW [11], RALF [10] and LIBRA [8]. RELVIEW is a relational evaluator, RALF is a theorem prover, and LIBRA, closer to our compiler, is a programming language based on the algebra of binary relations. However, LIBRA is different to our compiler, because it is not focused on an abstract calculus of relations.

Here we present a compiler that allows to translate fork specifications into normal logic programs. Although the semantics of logic programs that we use is not the standard (based on Herbrand models), the resulting programs may be executed by a common Prolog interpreter in a sound way.

2 Fork Algebras

Proper Fork algebras are algebras of binary relations extended with a binary operation called fork. For formally defining proper fork algebras, it is necessary first to define the class of Full*PFA:

**Definition 2.1** A Full*PFA is a two sorted structure with domains $\mathcal{P}(U \times U)$ and $U$

$$\langle \mathcal{P}(U \times U), U, \cup, \cap, \neg, \emptyset, U \times U, \mid, \text{Id}, \cdot, \sum, * \rangle$$

such that

1. $\mid$, $\text{Id}$, $\cdot$ and $\neg$ denote respectively composition of binary relations, the identity relation on $U$, converse of a binary relation and set complementation w.r.t. $U \times U$,

2. $*: U \times U \rightarrow U$ is an injective function,

3. $R\sum S = \{ \langle x, * (y, z) \rangle : x Ry \text{ and } xSz \}$.

**Definition 2.2** The class of FullPFA is defined as $\text{RdFull*PFA}$, where $\text{Rd}$ takes reducts of the similarity type $\langle \cup, \cap, \neg, \emptyset, U \times U, \mid, \text{Id}, \cdot, \sum, * \rangle$, and the class PFA is defined as $\text{SPFullPFA}$, where $\text{S}$ takes subalgebras and $\mathcal{P}$ closes a class under direct product.

The abstract counterpart of the class PFA is the class of abstract fork algebras, which is defined as follows:

**Definition 2.3** An abstract fork algebra is an algebraic structure

$$\langle R, +, \cdot, \neg, 0, 1, \mid, \text{Id}, \cdot, \sum \rangle$$
where +, · , ⊕ are binary operations, − and ′ are unary, and 0, 1, 1′ are constants, and the following set of axioms is satisfied:

Those axioms stating that \( \langle R, +, · , −, 0, 1 \rangle \) is a Boolean Algebra,

\[
\text{Ax. 1) } x; (y;z) = (x;y) ; z,
\]

\[
\text{Ax. 2) } (x+y) ; z = x; z + y;z,
\]

\[
\text{Ax. 3) } (x+y)′ = x + y′,
\]

\[
\text{Ax. 4) } x = x,
\]

\[
\text{Ax. 5) } x;1′ = 1′;x = x,
\]

\[
\text{Ax. 6) } (x;y)′ = y; x′,
\]

\[
\text{Ax. 7) } x; y = 0 \text{ iff } x; y′ = 0 \text{ iff } x′; z = 0 = 0.
\]

\[
\text{Ax. 8) } r \triangledown s = (r; (1′ \triangledown 1)) \cdot (s; (1 \triangledown 1′)) ,
\]

\[
\text{Ax. 9) } (r \triangledown s) ; (t \triangledown q)′ = (r; t′) \cdot (s; q′) ,
\]

\[
\text{Ax. 10) } (1′ \triangledown 1)′ \triangledown (1 \triangledown 1′)′ + 1′ = 1′.
\]

An useful operator for program specification using AFA is the operator cross (denoted by \( \otimes \)), which can be defined from the other operations as

\[
R \otimes S = ((1′ \triangledown 1)′ ; R) \triangledown ((1 \triangledown 1′)′ ; S).
\]

and whose meaning in the standard models of AFA is depicted in Figure 1.

\[
\text{Figure 1: The operator \textit{cross}.}
\]
Also, operations that behave as projections in standard models can be abstractly defined as follows

\[ \pi = (1' \nabla 1) \quad \text{and} \quad \rho = (1 \nabla 1') \]

The interpretation of \( \pi \) and \( \rho \) in the standard models is described pictorially in Figure 2.

2.1 Fork Algebras as Specification Language

Within fork algebras, program specifications are made up by sets of abstract fork equations. The intended meaning of a fork equation is a binary relation that relates data (input) to results (output); hence, relational composition represents sequential composition of programs, relational join represents program joining, and so on. Program transformation rules are the theorems of abstract fork algebras. For example, the term \( t_1 + t_2 \) can be transformed into \( t_2 + t_1 \) due to Commutativity of + (recall that the structure \( \langle R, +, \cdot, \neg, 0, 1 \rangle \) is a Boolean algebra).

Programs are homogeneous relations, so programs can have input or output from multiple data types in this formalism.

Some extra constant relations are included, and its meaning is related to basic operations on datatypes.

During the development process, the fork and cross operations are very important and useful. The reason is that they are convenient for specifying programs composed by subprograms that share data, and, in the case of cross, it allows to perform parallel computations on data constructed by \( \ast \).

Example: Let us consider the operation that sums the elements of a list of natural numbers. Let us suppose further that \( 1'_{L=0} \) is the partial identity on the empty list, and \( 1'_{L>0} \) be the partial identity on nonempty lists, zero be the constant that relates any element with the natural number 0; finally, let add be the relation that sums two natural numbers. The operation \( \text{SUM} \)
can be specified as follows:

\[
SUM = 1'_{L=0}; \; zero \; + \; 1'_{L>0}; \; \bigwedge \; \bigotimes \; ; add
\]

where \(hd\) and \(tl\) yield respectively the head and the tail of a (nonempty) list.

Let us explain the meaning of the above specification. The sum of the elements of the empty sequence is zero; if a list is nonempty we calculate the sum of the tail, and we add the head to that result.

As it is shown in the previous example, the combination of partial identities and the operator + can be used to construct case-like compositions of programs.

3 Logic Programs

Opposed to the untyped setting of common logic programming systems, we consider a typed universe; instead of using the Herbrand universe, we choose a restriction of it, in which the terms are constructed as follows:

Suppose that the language supports types \(\tau_1, \ldots, \tau_k\). Consider a first order language \(\mathcal{L}\) composed by:

- A numerable set of variable symbols,
- A numerable set of predicate symbols,
- for each \(n\)-ary constructor \(f\) from a type \(\tau_i\), we include \(f\) in the alphabet as an \(n\)-ary function symbol of type \(\tau_i\),
- a binary function symbol \(*\), which will be called \textit{star}.

Constructors from types must be injective functions, and the ranges of two different constructors of the same type must be disjoint sets.

\textbf{Definition 3.1} The set of \textit{ur-terms} for language \(\mathcal{L}\) is constructed as follows:

- Each variable symbol is an ur-term,
- each 0-ary function symbol \(f_0\) of type \(\tau_i\) is an ur-term of type \(\tau_i\)
- If \(f\) is a \(k\)-ary function symbol, where \(k \geq 1\), corresponding to a constructor
  \[
  f : \tau_{j_1}, \ldots, \tau_{j_k} \rightarrow \tau_i
  \]
  and \(t_1, \ldots, t_k\) are ur-terms of type \(\tau_{j_1}, \ldots, \tau_{j_k}\) respectively, then \(f(t_1, \ldots, t_k)\) is an ur-term of type \(\tau_i\).
**Definition 3.2** The set of terms for language $\mathcal{L}$ is constructed in the following way:

- If $t$ is an ur-term then it is a term,
- if $t_1, t_2$ are terms, so is $\ast(t_1, t_2)$.

### 3.1 Syntax of Programs

Let $\mathcal{L}$ be a language as described above. If $p$ is an $n$-ary predicate symbol, and $t_1, \ldots, t_n$ are terms, then $p(t_1, \ldots, t_n)$ is an atom. A literal is an atom or a negated atom (it is to say, $\neg(\text{atom})$).

The $S$-base of $\mathcal{L}$, denoted by $B_\mathcal{L}$, is the set of all ground atoms (i.e., the set of all atoms that do not contain variables).

A clause is an expression of the form:

$$p \leftarrow p_1, \ldots, p_n$$

for each $n \geq 0$, where $p$ is an atom and every $p_i, 1 \leq i \leq n$ is a literal.

A program is a pair

$$\langle P, m \rangle$$

where $P$ is a set of clauses and $m$ is a predicate symbol.

We will denote the class of all logic programs by $\text{Prog}$.

### 3.2 Semantics of Programs

Let $S$ be a subset of $B_\mathcal{L}$ and $Cl$ be a set of clauses. We will say that $S$ is a model of $Cl$ if $S$ satisfies every clause in $Cl$. A clause of the form

$$p \leftarrow p_1, \ldots, p_k$$

is interpreted as the universal closure of the formula $p_1 \land \ldots \land p_k \rightarrow p$ (interpreting the symbol $\rightarrow$ as logical negation).

We cannot choose as semantics for our programs the minimal model semantics, because negation is allowed in the body of clauses. This produces that many distinct minimal models could exist for a particular program; it could be worst: a set of clauses could be inconsistent. So, we restrict the class $\text{Prog}$ to a set of programs, called stratified, for which always there exist a minimal model. We consider for these programs the standard model semantics [2], which consists in dividing a program into (monotonic) strata, where each stratum uses negatively only predicates from previous strata, and construct the minimal model of each stratum based on the result on the previous one.

**Definition 3.3** Let $\langle P, m \rangle \in \text{Prog}$. We construct the dependency graph $DG(P)$ for $P$ as follows:
• For every predicate symbol \( q \) occurring in \( P \), there is a node in \( DG(P) \) labeled by \( q \),

• if there exists a clause in \( P \) of the form:

\[
q(...) \leftarrow ..., p(...), ...
\]

then there is an arc in \( DG(P) \) from the node labeled by \( p \) to the node labeled by \( q \),

• if there exists a clause in \( P \) of the form:

\[
q(...) \leftarrow ..., -p(...), ...
\]

then there is an arc in \( DG(P) \) labeled by ‘\(-\)’ from the node labeled by \( p \) to the node labeled by \( q \).

We will say that \( \langle P, m \rangle \) is stratified if \( DG(P) \) has no cycles with an arc labeled by ‘\(-\)’.

We will denote by \( Prog_{\text{strat}} \) the class of all the stratified programs.

**Definition 3.4** Consider a set of clauses \( CL \). \( CL = CL_1 \cup CL_2 \cup ... \cup CL_n \) is called a stratification of \( CL \) if for \( i \in [1, n] \) \( CL_i \) uses

• positively only predicates defined in \( \bigcup_{j=1}^{i} CL_j \),

• negatively only predicates defined in \( \bigcup_{j=1}^{i-1} CL_j \).

**Definition 3.5** Let \( CL \) be a stratified set of clauses. Assume a stratification \( CL = CL_1 \cup CL_2 \cup ... \cup CL_n \), and let \( M|S \), where \( M \subseteq B_L \) and \( S \) is a set of clauses, denote the interpretation \( M \) restricted to predicates in clauses of \( S \). Then, we define:

\( M_1 = \) minimal model for \( CL_1 \),
\( M_2 = \) minimal model for \( CL_2 \) such that \( M_2|CL_1 = M_1 \),
...
\( M_n = \) minimal model for \( CL_n \) such that \( M_n|CL_1 = M_1, ..., M_n|CL_{n-1} = M_{n-1} \).

\( M_n \) is called the standard model of \( CL \).

It is shown in [2] that the standard model is minimal and supported, and that it does not depend on the stratification.

**Definition 3.6** Let \( \langle P, m \rangle \in Prog_{\text{strat}} \). We will call general meaning of \( \langle P, m \rangle \) the standard model of \( P \). The meaning of \( \langle P, m \rangle \), denoted by \( M(\langle P, m \rangle) \) is the set of atoms in the general meaning that have \( m \) as predicate symbol.
4 The Language of Specifications

Basically, a specification is a set of fork equations, where a fork equation has the form

\[ \langle \text{variable} \rangle = \langle \text{term} \rangle \]

An equation may be thought of as the definition of a program module, where the variable is the “name” of the module and the term is its implementation. The term may contain variables, that may be seen as “calls” to other program modules.

A variable is simply an identifier, composed by any sequence of characters, not beginning with ‘\’. A term is a (possibly nonground) abstract fork term, where the names of the fork operations are the following:

\[
\begin{align*}
1 & \quad \text{univ} \\
1' & \quad \text{id} \\
0 & \quad \text{empty} \\
\pi & \quad \text{pi} \\
\rho & \quad \text{rho} \\
arg_1;\arg_2 & \quad \text{arg}_1;\text{arg}_2 \\
\arg_1 + \arg_2 & \quad \text{join}\{\arg_1\}{\arg_2} \\
\arg_1 \cdot \arg_2 & \quad \text{meet}\{\arg_1\}{\arg_2} \\
\arg_1 \nabla \arg_2 & \quad \text{fork}\{\arg_1\}{\arg_2} \\
\arg_1 \otimes \arg_2 & \quad \text{cross}\{\arg_1\}{\arg_2} \\
\text{arg} & \quad \text{conv}\{\text{arg}\} \\
\text{arg} & \quad \text{compl}\{\text{arg}\}
\end{align*}
\]

Example: Consider the following fork specification

\[ \text{TWO}_\text{PARALLEL}_X = 1' \quad X \]

that intuitively performs two parallel computations of \(X\) to the same argument; in our language it is written as follows:

\[ \text{TWO}_\text{PARALLEL}_X = \text{fork}\{\text{id}\}{\text{id}} ; \text{cross}\{X\}{X} \]

4.1 Types

It is obvious that without further constant relations it is not possible to write interesting specifications; in fact, we could not use datatypes if only the basic fork operations are available.

Thus, we include some extra operations whose behavior is related to datatype manipulation.
Natural numbers
The extra relational operations that our language supports for manipulating natural numbers are:

- \textbackslash{}zero: This operation relates any element (an element from any datatype) to the natural number zero.

- \textbackslash{}suc\ell{}: relates a natural number to its successor.

- \textbackslash{}pred: relates a nonzero natural number to its predecessor.

Lists of natural numbers
The relations that act on lists of natural numbers are:

- \textbackslash{}nil: relates any element to the empty list.

- \textbackslash{}cons: Given a pair, constructed by ‘\&’, whose first component is a natural number \(n\) and the second one is a list \(l\), relation \textbackslash{}cons relates this pair to the list constructed by putting \(n\) in front of \(l\).

- \textbackslash{}hd: relates a nonempty list to its head.

- \textbackslash{}tl: relates a nonempty list to its tail.

Booleans
The relations that manipulate boolean values are:

- \textbackslash{}true: relates any element to the boolean value \textit{true}.

- \textbackslash{}false: relates any element to the boolean value \textit{false}.

Binary Trees of natural numbers
The following relations allow to use binary trees:

- \textbackslash{}niltree: relates any element to the empty tree.

- \textbackslash{}maketree: Given a 3-uple (actually is a pair) whose first component is a natural number \(n\), and whose second and third components are binary trees \(b_1\) and \(b_2\) respectively, \textbackslash{}maketree relates this triple to the tree composed by \(b_1\) as left child, \(b_2\) as right child, and \(n\) as root.

- \textbackslash{}lch: relates a nonempty tree to its left child.

- \textbackslash{}rch: relates a nonempty tree to its right child.

- \textbackslash{}root: relates a nonempty tree to its root.

We include also relations that correspond to “filters” on the range of constructor relations, such as \textbackslash{}idnil, which is the partial identity on the empty list. The grammar of our specification language is shown in Figure 3.

Example:
1. Let us consider the following specification:

\[ \text{LENGTH} = 1'_{L=0}; \text{zero} + 1'_{L>0}; \text{tl}; \text{LENGTH}; \text{succ} \]

where \(1'_{L=0}\) is the partial identity on the empty list, \(1'_{L>0}\) is the partial identity on nonempty lists, \text{zero} relates any element to zero, \text{tl} calculates the tail of a list, and \text{succ} adds 1 to a natural number. Clearly, \text{LENGTH} recursively computes the length of a list. In our language it is written as:

\[
\text{LENGTH} = \text{\texttt{\textbackslash join}\{\text{\textbackslash idnil};\text{\textbackslash zero}\}}
\]

\[
\{\text{\texttt{\textbackslash idcons};\text{\texttt{\textbackslash tl};\text{\textbackslash LENGTH};\text{\texttt{\textbackslash succ}}}}\}
\]

2. Let us consider now the following specification:

\[
\text{add} = \begin{array}{c}
\times \rho + \times \rho \times \rho ; \rho ; \times \rho ; \text{\texttt{add}; succ}
\end{array}
\]

\[
1'_{\text{Nat}} = 1'_{\text{Nat}} 1'
\]

where \text{pred} calculates the predecessor of a natural number, and the identities \(1'_{N=0}\), \(1'_{N>0}\), \(1'_{\text{Nat}}\) are respectively filters on the natural zero, nonzero natural numbers and natural numbers. The relation \text{add} computes the sum of two natural numbers. This specification can be written in our language in the following way:

\[
\text{add} = \text{\texttt{\textbackslash join}\{\text{\texttt{\textbackslash cross}\{\text{idzero}\}\text{\texttt{\textbackslash cross}\{\text{idzero}\]\text{\texttt{\textbackslash idsucc}}}}\};\text{\texttt{\textbackslash rho}}\}}
\]

\[
\{\text{\texttt{\textbackslash cross}\{\text{idzero}\}\text{\texttt{\textbackslash idsucc}}};
\text{\texttt{\textbackslash cross}\{\text{pred}\}\text{\texttt{\textbackslash id}}};
\text{\texttt{add}};
\text{\texttt{\textbackslash succ}}
\}
\]

### 4.2 Translation of Specifications

In this section we will briefly show how equations are translated into logic clauses. In order to do this, we first need to show how to translate terms.

#### 4.2.1 Translation of Fork Terms

We will describe the way in which some fork-algebraic operations are translated. The interested reader is referred to [1] for a more detailed description about the translation.

As we have already explained, one assumes some intuitive meaning of the operations when manipulating abstract fork specifications. Our translation follows this intended meaning. For example:
<program>  :  <eqlist>

<eqlist>  :  <equation>
    |  <eqlist> .  <equation>

<equation> :  <VAR>  =  <term_list>

<term_list>:  <term>
    |  <term_list> ;  <term>

<term> :  <VAR>  |  \fork  <arg>  <arg>  |  \join  <arg>  <arg>
    |  \meet  <arg>  <arg>  |  \cross  <arg>  <arg>  |  \cons
    |  \conver  <arg>  |  \compl  <arg>  |  \succ  |  \pred
    |  \hd  |  \tl  |  \dom  <arg>  |  \ran  <arg>  |  \id
    |  \idnil  |  \idcons  |  \idzero  |  \idsucc  |  \univ
    |  \empty  |  \pi  |  \rho  |  \zero  |  \nil  |  \niltree
    |  \maketree  |  \root  |  \leftchild  |  \rightchild
    |  \idniltree  |  \idnvtree  |  \true  |  \false
    |  \idfalse  |  \idtrue

<arg> :  {  <term_list>  }

Figure 3: Grammar of the specification language.
1. Translation of variables: Variables are translated just by using a fixed (binary) predicate symbol:

\[ X \mapsto \langle \emptyset, pX \rangle \]

2. Translation of constants: Constants of abstract fork algebras are translated in the following way:

\[
\begin{align*}
1 & \mapsto \langle \{m(X,Y) \leftarrow \}, m \rangle \\
0 & \mapsto \langle \emptyset, m \rangle \\
1' & \mapsto \langle \{m(X,X) \leftarrow \}, m \rangle
\end{align*}
\]

The constants that were introduced by type definitions are translated using the corresponding constructors. For example, the constant relation zero, which corresponds to the constructor 0, is translated into the following program:

\[ \langle \{m(X,0) \leftarrow \}, m \rangle \]

3. Translation of join: The intended semantics of join is program joining, so the translation of join, denoted here by \( \phi \), is recursively defined by:

\[ R_1 + R_2 \mapsto \langle C_{R_1 + R_2} \cup P_1 \cup P_2, \text{new} \rangle \]

where

\[ \phi(R_1) = \langle P_1, m_1 \rangle \] and \( \phi(R_2) = \langle P_2, m_2 \rangle \)

and \( C_{R_1 + R_2} = \{ \text{new}(X,Y) \leftarrow m_1(X,Y), \text{new}(X,Y) \leftarrow m_2(X,Y) \} \).

4. Translation of fork: The intended semantics of fork is the tupling of outputs of each relation involved. Fork is translated as follows:

\[ R_1 \varnothing R_2 \mapsto \langle C_{R_1 \varnothing R_2} \cup P_1 \cup P_2, \text{new} \rangle \]

where \( C_{R_1 \varnothing R_2} = \{ \text{new}(X,*,Y1,Y2) \leftarrow m_1(X,Y1), m_2(X,Y2) \} \).

Here we can see the usefulness of the \( \star \) function symbol.

5. Translation of composition: Composition is translated in the following way:

\[ R_1; R_2 \mapsto \langle C_{R_1; R_2} \cup P_1 \cup P_2, \text{new} \rangle \]

where \( C_{R_1; R_2} = \{ \text{new}(X,Y) \leftarrow m_1(X,Z), m_2(Z,Y) \} \).
4.2.2 Translation of Equations

Once the right-hand side of the equations is translated, we only need to relate the resulting programs with their corresponding left-hand side variable. This is done by adding clauses of the form:

$$p[V(X, Y) \leftarrow m(X, Y)]$$

for every equation $$V = T$$ in the specification, where $$m$$ is the main predicate in $$\phi(T)$$.

Example: Let us consider the above-mentioned specification of LENGTH. Its right-hand side term is translated into $$\langle P, \text{len} \rangle$$, where $$P$$ is the set:

$$\begin{align*}
\{ & \text{len}(X, Y) \leftarrow \text{idnil}(X, Z), \text{zero}(Z, Y); \\
& \text{len}(X, Y) \leftarrow \text{notnil}(X, Z1), \text{tl}(Z1, Z2), p_{\text{LENGTH}}(Z2, Z3), \text{sig}(Z3, Y); \\
& \text{idnil}(X, Y) \leftarrow \text{nil}(X, Y), \text{id}(X, Y); \\
& \text{tl}(X, Y) \leftarrow \text{cons}(Z, X), \text{rho}(Z, Y) \\
\} 
\end{align*}$$

Now, we relate $$\text{len}$$ with LENGTH by adding the clause:

$$p_{\text{LENGTH}}(X, Y) \leftarrow \text{len}(X, Y)$$

4.3 Restrictions

There exist some restrictions on the specifications. As it is indicated in [1], a set of equations must be stratified with respect to complementation; this means that if a relation $$R$$ depends on the complementation of $$S$$ then $$S$$ cannot depend on $$R$$.

It is also necessary that all the equations from a set have different variables in their left-hand side (no multiple definitions of relations).

4.4 Semantics of Fork Specifications

Although the semantics of fork specifications will not be studied in this paper, it is important to note that, as it is explained and proved in [1], the way in which specifications are defined and translated is completely natural, and yields a straightforward definition for semantics of stratified sets of equations.
5 The Fork Compiler

The fork compiler that we describe in this section is a tool that allows to execute fork specifications. It works translating a fork specification into a normal logic program in such a manner that the semantics of the original specification is preserved.

5.1 Executing a Specification

Once a specification is written, it can be translated into a logic program by using the fork compiler. Then, the programmer can execute the specification by interpreting the generated code in a logic programming interpreter.

For each relation definition of the form

\[ X = T \]

a predicate \( p_X \) is generated in the output logic program, so the programmer may consult predicate \( p_X \) to execute the relational program \( X \).

**Example:** Let us consider the `LENGTH` specification given above. The logic program generated by the compiler include the predicate \( p_{LENGTH} \), which can be used to execute `LENGTH`. If the programmer wants to compute the length of the list \([1, 2, 3, 4]\), he would make the following consult to the generated program:

\[ p_{LENGTH}(\{1, 2, 3, 4\}, X). \]

5.2 Using a Common Prolog Interpreter to Execute Specifications

The declarative meaning of logic programs is given by the standard model semantics [2]; although Prolog does not support this semantics, the refutation procedure [9] (procedural semantics of programs in Prolog) is sound with respect to this meaning. Thus, a Prolog interpreter can be used to evaluate a program generated by the fork compiler. However, two problems could arise if a Prolog interpreter is used to evaluate fork logic programs:

- the refutation procedure could fail to find successful results, especially when the original fork specification use the complementation operation,

- because of the untyped nature of Prolog semantics, a program could yield meaningless terms as results if it is evaluated on a non-well-formed term (it is not controlled by the interpreter). For example, if the relation `pred` (that relates a nonzero natural number to its predecessor) is evaluated on the term \( \ast(\ast(0, 0)) \), which is not well-formed, it will yield \( \ast(0, 0) \) as result.
6 Future Work

The tool that we have presented allows to translate a fork specification into a logic program preserving the meaning of the original specification. This tool can be extended in many ways. At first, an interpreter that checks the correct construction of predicate arguments when consulting a program should be made; also, the stratification of specifications should be checked statically. Some simple optimizations should be made to the generated programs, that does not affect the performance of programs, but improve their reading. These optimizations are unfolding of predicates, in order to avoid the use of unnecessary predicate definitions, and the elimination of repeated predicate definitions, produced by the sharing of some subexpressions in fork specifications.

Another useful extension is the construction of a visual tool for editing fork specifications; by such an editor, the specifier could avoid dealing with the details of the generated code, and work entirely on a fork-algebraic environment.

References


[11] Relview System, Department of Computer Science and Applied Mathematics, University of Kiel, Germany, URL: [www.informatik.uni-kiel.de/~progsys/review.html](http://www.informatik.uni-kiel.de/~progsys/review.html).