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1	Three-dimensional reconstruction of irregular foodstuffs
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10	Abstract
11	3-D reconstruction of general solid food materials was performed using a reverse
12	engineering method based on a surface cross-sectional design. Digital images of cross-
13	sections of irregular multi-dimensional foodstuffs were acquired using a computer
14	vision system, and image processing was performed to obtain the actual boundaries.
15	These boundaries were then approximated by closed B-Spline curves, which were
16	assembled through a lofting technique to construct a geometrical representation of food
17	materials. Considering the reconstructed objects, a procedure based on finite element
18	method was developed to estimate the surface area and volume. The developed finite
19	element method approach was validated against experimental volume values of apples
20	and meat pieces, obtaining an estimation error less than 2%. Surface area prediction
21	equations were proposed from estimated surface area values and weight and volume
22	measurements. Good agreement was found with previously reported results.
23	Keywords: Lofting; B-Spline curves; Irregular shape; Surface area.

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#### 24 1. Introduction

25

26 Many food engineering processes, especially, those including transfer phenomena and quality evaluation, involve measurement or estimation of the surface 27 area and volume of food materials. For example, it is well known that heat and mass 28 29 transfer coefficients depend on the shape and surface area of the object being analyzed 30 In addition, volume dependent properties, like density, would be easily determined if 31 the volume was correctly measured or estimated. Therefore, estimation of surface area 32 and volume is an essential issue in the food engineering field. However, it is a tedious 33 and difficult task, moreover, when irregular shaped objects are involved. Since many of 34 food materials like grains, fruits and vegetables are approximately ellipsoidal in shape, some researchers worked on the development of an accurate and simple equation for the 35 36 estimation of the surface area for such cases (Igathinathane & Chattopadhyay, 1998a,b, 2000; Kumar & Mathew, 2003; Somsen, Capelle, & Tramper, 2004; Taylor, Garboczi, 37 Erdogan & Fowler, 2006). On the other hand, not many articles concerning shape 38 39 analysis and estimation of surface area and volume regarding irregular three-40 dimensional foodstuffs had been published.

Clayton, Amos, Banks and Morton (1995) worked on the estimation of surface area of apple's of four different cultivars. They applied various methods: sphere and ellipsoid analogies; correlation between actual surface area (estimated by tape method) and both fruit mass and volume; and the finite element method (FEM). The calculation of surface area using FEM was based on a computer software package developed previously (Cleland, Cleland, Earle & Byrne, 1984). In such method, a two-dimensional axisymmetrical coordinate grid depicting the shape of the fruit is formed. Surface area

48 is then calculated based on this grid (Clayton et al., 1995). FEM was the most accurate49 of the numerically based methods that were evaluated.

50 Some work was done regarding shape description, but not including neither solid reconstruction nor surface area and volume estimation. For instance, with the aim of 51 evaluating chilling time related shape factors, a three-dimensional laser scanning 52 53 technique was used to digitize the surface of several types of meat cuts (Crocombe, 54 Lovatt & Clarke, 1999). Three-dimensional surface data were collected from each meat 55 cut and a bicubic Hermite surface model was then fitted to each data set to give a full 56 mathematical description of the surface. From such models, Crocombe et al. (1999) determined the geometric shape factors used in the prediction of chilling, freezing and 57 thawing times. In addition, following the objective of classifying and quality grading 58 59 fruits, different shape descriptors were applied. Fourier descriptors were used to characterize the apple shape via the contour of digitized cross-sections that were 60 61 obtained by image analysis Currie, Ganeshanandam, Noiton, Garrick, Shelbourne & Oraguzie, 2000). Concerning three-dimensional shape description, Ding, Nesumi, 62 63 Takano and Ukai (2000) worked on *Citrus* species using spherical harmonic descriptors; 64 Beyer, Hahn, Peschel, Harz and Knoche (2002) described fruit shape in sweet cherry 65 using image analysis and standard software.

66 Sabliov, Boldor, Keener and Farkas (2002) developed an image processing 67 based method to measure volume and surface area of ellipsoidal agricultural products 68 (eggs, lemons, limes and peaches). The method assumes that each product has an 69 axisymmetric geometry and is a sum of superimposed elementary frustums of right 70 circular cones. The product volume and surface area are calculated as the sum of the 71 volumes and surface areas of individual frustums. Lee, Eifert, Zhan and Westover 72 (2003) developed a computer vision technique combining laser triangulation and a

73 distance transform to improve the 3-D measurement accuracy obtained by only applying 74 laser triangulation, for objects with irregular shapes. Eifert, Sanglay, Lee, Sumner and 75 Pierson (2006) utilized a machine vision system using radial projection technique (Lee, Xu, Eifert & Zhan, 2006) to measure the surface area of fresh foods: apples, 76 cantaloupes, strawberries and tomatoes. A sequence of 30 images taken at the same 77 78 angular interval was recorded for image processing for an object. Each image was treated as a slice of the cross-section of the object taken at a specific angular position. 79 80 Then, location of boundary points on each image slice was extracted to create a 3D 81 wire-frame model for surface area estimation by commercial software. Finally, they proposed prediction equations for the surface area of each food shape from weight 82 measurement. More recently, Zheng, Sun and Du (2006), and Du and Sun (2006) 83 84 developed image processing techniques to estimate the surface area and volume of beef 85 joints and hams, respectively. In both works, shape of samples was fitted to ellipsoidal geometry. Surface area and volume calculations were based on the concept of summing 86 87 a finite number of regular conical sections, which axis were obtained through computer 88 vision.

89 State of the art shows that previous articles were focused on estimation of surface area, or shape description of objects, having relatively high sphericity or being 90 91 symmetrical in some way. However, most of foodstuffs do not present these 92 geometrical properties. Therefore, there is an absence of accurate methods to estimate 93 the surface area of food materials with arbitrarily irregular shapes. The overall objective 94 of the present work is to simulate food preservation processes in irregular three-95 dimensional domains. To achieve this objective, it is first necessary to develop a method 96 to obtain an irregular 3D representation of the real shape of foodstuffs. This paper presents the results of geometry modelling obtained by reverse engineering techniques. 97

98 Furthermore, a procedure based on finite element method was developed to estimate the
99 surface area and volume of irregular food materials. The application of the resulting
100 object reconstruction will be used as domain in simulation of preservation processes,
101 which will be discussed in a future work

102

#### 103 **2. Method description**

104

105 Reverse engineering is a technology to establish CAD (Computer Aided Design) geometry models from samples, prototypes, moulds or manufactured parts by 106 digitization. A CAD technique called "skinning" or "lofting" could be employed for the 107 reverse engineering applications (Lin, Liou & Lai, 1997). Skinning is a special case of 108 cross-sectional design of surfaces (Piegl, 1991). Briefly, surface skinning is a process of 109 passing a smooth surface through a set of so called cross-sectional curves (Piegl & 110 111 Tiller, 1996). The most used mathematical description of free-shaped curves and surfaces is the well-known Non-Uniform Rational B-Splines (NURBS) representation 112 113 (Moustakides, Briassoulis, Psarakis & Dimas, 2000). For further information about 114 cross-sectional design, the reader should be referred to Woodward (1987, 1988).

115

#### 116 **2.1. Object reconstruction**

117

118 Object reconstruction is a computational representation of the real food material 119 geometry in its actual dimensions. The entire method was implemented in MATLAB<sup>®</sup> 120 and COMSOL Multiphysics<sup>TM</sup> (version 3.2). The basic steps are described in the 121 follows:

122 1. An axis was manually selected, along which the object would be sliced, by 123 simple visual inspection. The sectioning axis was mainly chosen in order to obtain filled 124 regions without interior holes, that is, to capture an image with a single closed 125 boundary. Also, this axis should correspond to the direction presenting the minor 126 irregularity of the object.

2. Sample sectioning was performed along the selected axis using a mechanical cut apparatus to ensure a controlled width for each section. The width of slices depends on the size and shape variability of the sample along its sectioning axis. That is, as more irregular is the sample, thinner slices must be taken to improve the approximation to the real shape. Afterwards, the sample was reconstructed by manually assembling the cut slices. Thus, the original spatial orientation and alignment of the samples was respected, which is essential for computational reconstruction accuracy.

3. Acquisition of images was done using a computer vision system (CVS), i.e. a 134 135 PC equipped with a digital camera. The images were taken using a white or black background plate, depending on the sample colour. Choosing background colour is 136 137 important in order to perform efficient boundary detection: as more contrast between 138 sample and background is obtained, a better procedure of sample contour extraction will 139 be done. Acquisition was performed as follows: the background plate was placed 140 between the first and second slices, and the lens was situated orthogonally to the first slice. Therefore, the first slice was "isolated" from the entire sample without losing the 141 142 original alignment. After image recording, the first slice was extracted and the 143 background plate was placed between the second and third slices. This procedure was 144 repeated until image of each slice was recorded.

145 4. The irregular contour was extracted from the images of slices, as follows:

146

4.1. Conversion of original RGB images to grey-scale format.

147 4.2. Noise reduction through a 3 x 3 median filter to enhance image quality.

- 4.3. Segmentation through a threshold value which was obtained analyzing the
  grey-scale image histogram. A binary image was obtained where black colour
  (pixel value equal to 0) represented the background and white colour the slice
  (pixel value equal to 1).
- 4.4. Boundary detection and interpolation of a subset of boundary pixels by a
  closed B-Spline curve (a continuous approximation to the discrete boundary
  of binary images).

155 Finally, the B-Spline curves representing the real boundaries of slices were correctly assembled by means of a lofting technique in COMSOL Multiphysics: a closed NURBS 156 surface was constructed through B-Spline cross-section curves. The resulting surface 157 158 was then transformed in a 3D solid object It is worth to note that the number of 159 segments of each B-Spline curve must be the same in all extracted boundaries to 160 perform lofting. For further information about lofting technique implemented in COMSOL Multiphysics, the reader should be referred to COMSOL Multiphysics User's 161 162 Guide.

A conversion factor, computed from a reference object, was used to convert the object dimensions from pixels to SI units during the image acquisition stage. The computational representation of the food material may be used to estimate its surface area and volume (see section 2.2), and as a geometry model in an engineering process modelling and simulation (and eventual optimization).

- 169 **2.2. Surface area and volume estimation**
- 170

171 A FEM approach method was developed to estimate the volume and surface area 172 of reconstructed foodstuffs. These determinations, together with visual results, can be 173 used to assess the reconstruction accuracy. The FEM approach method consists in approximating the surface area and volume of real foodstuffs as a sum of such 174 properties of finite elements obtained by meshing the reconstructed object Firstly, a 175 176 mesh was generated using curved mesh elements to make the best approximation to the 177 irregular shape. These elements are distorted simplices (tetrahedrons) that can 178 approximate the boundary better than ordinary, straight mesh elements (COMSOL 179 Multiphysics). In other words, the mesh elements are curved at the boundary, and thus come closer to the true geometric boundary. Delaunay algorithm was used to generate 180 the mesh, which size and number of elements is determined by various properties such 181 182 as maximum element size and curvature mesh size. These parameters are directly related to time calculation and computer capability, i.e. as more finer the mesh is, more 183 184 time and PC memory are needed

Secondly, a general variable (u) was set equal to one in all mesh nodes. This is equivalent to solve a partial differential equation (PDE) which solution would be u = 1. Thirdly, a numerical integration for u was made over all boundary ( $\Gamma_i$ ) and domain ( $\Omega_i$ ) elements to obtain the estimated surface area and volume values, respectively (Eq. (1)-(2)).

190

$$191 \qquad \tilde{S} = \sum_{i} \iint_{\Gamma} u \, d\Gamma_{i} \tag{1}$$

192 
$$\tilde{V} = \sum_{i} \iiint_{\Omega_{i}} u \, d\Omega_{i}$$
(2)

193

#### 194 **3. Materials and methods**

195

The samples used to evaluate the proposed method were 12 apples (6 from Red
Delicious variety and 6 from Granny Smith variety), and 8 meat pieces (*semitendinosus*muscle). The CVS was a digital camera (Professional Series Network IP Camera Model
550710, Intellinet Active Networking, USA) connected to a PC (AMD Sempron 2200+,
768 MB RAM).

The volume of each sample was experimentally determined by liquid 201 displacement method in a single measurement. The goodness of the developed FEM 202 203 approach method was evaluated by comparison between experimental sample volume (V) and estimated volume ( $\tilde{V}$ ) values of each reconstructed object. The parameters used 204 for this aim were the percentage volume relative error  $(RE_V)$ , the percentage volume 205 206 mean absolute relative error  $(MARE_V)$  and the correlation coefficient (r). No experimental procedure was implemented to obtain actual values of the surface area, 207 since the difficulty to manually measure this parameter. 208

209

 $RE_V(\%) = 100 \frac{\tilde{V} - V}{V}$ 

211 
$$MARE_{V}(\%) = \frac{100}{N} \sum_{i=1}^{N} \left\| \frac{\tilde{V}_{i} - V_{i}}{V_{i}} \right\|$$

212

- 213 4. Results and discussion214
- 215 **4.1. Lofting technique**

216

(3)

(4)

The CVS and the cut directions chosen for the samples are shown in Figures 1 217 218 and 2, respectively (see section 2.1). Image processing stages employed to approximate 219 the boundary of slices are depicted in Figure 3. As can be seen, correct selection of 220 background allowed performing a good segmentation process. This was translated in an accurate boundary approximation. Graphic results of object reconstruction and meshing 221 222 over samples are shown in Figures 4 and 5. From visual inspection, the implemented 223 technique correctly reproduced the shape of real food materials. The lofting method 224 produced smooth and irregular surfaces, similar to the natural ones.

225 Since each contour of the cross-section segmented images consisted of a large 226 number of data points, a small subset of those boundary points was used to construct a closed B-Spline curve, in order to obtain a simpler but still appropriated representation 227 228 of the real boundary. To perform the lofting procedure, the number of points in such 229 subset must be equal in all slices. The size of this subset influenced the accuracy of the 230 lofting and subsequent FEM approach method. The amount of points in the subset is 231 directly proportional to the approximation degree to the actual boundary. However, 232 when the number of points was very large, since the boundary was represented digitally, 233 (i.e. by pixels) the obtained B-Spline curve presented a sharp trajectory. These 234 characteristics of the B-Spline curve are translated to the constructed NURBS surface 235 and the computational requirements for the meshing step. Non smooth slices produced 236 sharp surfaces (and solids), which involved a large amount of finite elements (Figure 6). 237 Another important feature of the skinning technique is the number of cross-238 sections used. As more slices were considered, best approximations to the real objects 239 were obtained. However, in some cases where the modelled object presented smooth 240 shape, the amount of cross-sections could be reduced, and so the computational costs. 241 The applied slicing method presented one drawback: there existed a minimum thickness

242 for the slices to obtain undamaged shape in cross-sections. This problem could be 243 solved by using a non invasive slicing method, such as NMR (Nuclear Magnetic 244 Resonance). This technique, widely used in medicine field, allows obtaining very thin slices without sample destruction in a fast and easy way. Also, recorded images present 245 less experimental noise and high contrast between the sample and background, which is 246 247 reflected in a better segmentation process. The main disadvantage of NMR method is its 248 high cost and equipment availability. NMR technique is now being implemented and 249 will be published in a future work.

Although the developed method is destructive and could be laborious, it needs not expensive laboratory equipment and it could be applied in another software environment. In addition, the method allows working with samples presenting high degree of irregularity. This is, objects with protrusions or cavities in surface, interior holes and shapes with very low sphericity. These kinds of morphological characteristics would be difficult to register using the non destructive methods previously reported, since they work with projections of the entire sample.

257

#### 258 4.2. Volume and surface area estimation

259

The surface area and volume values of the reconstructed objects were calculated using Gaussian integration of 4<sup>th</sup> order. As was discussed above, a number of boundary points for slices representation must be selected. Therefore, an analysis of the influence of the size of boundary subset on surface area and volume estimation procedure was carried out. Several solids of one (representative) sample of meat piece were obtained using different point numbers in the boundary subset. The number of cross-sections was fixed to 11, the maximum obtained for the tested sample. As the number of considered

boundary points was increased, the relative error when volume was estimated tended asymptotically to zero (Figure 7). For more than 33 boundary points, the estimation error was less than 1% (in absolute terms). Therefore, the size of the boundary subset was set to 33 points, for all tested samples, since low error was obtained and computational costs were acceptable.

Also, the effect of number of cross-sections in the approximation was analyzed using the same meat sample as above. For this aim, the first and last cross-sections were fixed and the intermediate cross-sections were successively included All solids were reconstructed using 33 points in the boundary subset of each slice. The same asymptotical behaviour as with boundary points was observed for the number of crosssections (Figure 8). When this number was greater than 7, the estimation error of volume was lower than 1%.

When comparing the volume estimated by the FEM approach method with 279 280 experimental results, high correlation was found for all tested samples (Figure 9). All 281 results were summarized in Table 1. As can be seen, the FEM approach method 282 provided results with low error dispersion being the mean estimation error less than 2% 283 in absolute terms, in all cases. Also, mean relative error was calculated finding negative values: -1.25% for Granny Smith apple, -1.01% for Red Delicious apple, and -0.95% 284 285 for meat pieces. These results indicated underestimation in volume prediction by FEM 286 approach. Underestimation may be due to two facts: (i) the lofting technique uses a 287 finite number of cross sections, therefore the reconstructed solid is an approximation to 288 the real food; (ii) in spite of the use of curved simplices, these can not be highly 289 distorted in order to follow the exact curvature of the real geometry, therefore a small part of the object is not filled with finite elements. 290

291 The developed FEM approach method exactly estimated the volume and surface 292 area of objects formed with only planar faces, such as general polyhedrons (results not 293 shown). In these cases, the finite elements used are straight, not distorted simplices, and the volume and surface area could be exactly predicted. Bearing in mind the good 294 performance of the FEM approach method to estimate the volume of samples tested 295 296 here, it is expected that the method can approximate the actual surface area of foodstuffs 297 with high accuracy. So, to generalize the obtained results for each tested object, the estimated values of the surface area were correlated with the weight and volume of 298 299 samples. For this aim, the following equations based on dimensional analysis (expressing S, W and V in terms of a characteristic length L) were proposed: 300

301

$$302 S = {}_{0}W^{\frac{2}{3}} (5)$$

$$303 S = {}_{0}V^{\frac{2}{3}} (6)$$

304

The fitting performance and the estimated parameter for the Eq. (5) and (6) are shown in Table 2. Both correlations fitted well the calculated surface area to experimental values of weight and volume, for all tested samples, as can be seen in Figure 10.

Prediction equations for surface area of apples reported by Clayton et al. (1995), obtained from experimental values (tape method), were compared against the FEM approach method results. Values of  $R^2$  were 0.96 and 0.97, for Red Delicious and Granny Smith varieties, respectively. Also, Clayton et al. (1995) compared the experimental values with their FEM based method. They obtained  $R^2$  values equal to 0.96 and 0.99, for Red Delicious and Granny Smith varieties, respectively. Furthermore, Eifert et al. (2006) reported an equation to predict the surface area of apples from

315	weight meas	urement. It was a linear equation, with $R^2$ equal to 0.47. In the present
316	work, Eq. (5)	) was obtained with $R^2$ greater than 0.93, in the apple cases.
317		
318	5. Conclusio	ns
319		
320	The a	pplied lofting technique allows obtaining an accurate representation of the
321	real shape of	f irregular multi-dimensional foodstuffs. Furthermore, the developed FEM
322	approach me	thod demonstrated its ability to correctly predict volume and surface area
323	of general ob	bjects, even presenting low symmetry and sphericity. The application of the
324	resulting obj	ect reconstruction will be used as domain in simulation of preservation
325	processes in a	a separate paper.
326		
327	Nomenclatu	re
328		
329	MARE <sub>V</sub>	volume mean absolute relative error (%)
330	r	correlation coefficient
331	$RE_V$	percentage volume relative error (%)
332	$R^2$	determination coefficient
333	S	surface area, cm <sup>2</sup>
334	u	general scalar dependent variable
335	V	experimental volume, cm <sup>3</sup>
336	$\widetilde{V}$	estimated volume, cm <sup>3</sup>
337	W	weight, g
338	Greek symb	ols
339	$a_0$	parameter of Eq. (5)

340	$\beta_0$ parameter of Eq. (6)
341	
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343	
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#### 417 **Table 1.** Experimental volume values and estimated values of surface area and volume

418 of samples.

	Number o	of Average	Measured	Measured	Estimated	Absolute	Estimated	D '/
	cross	thickness of	weight	volume	volume	relative	surface area	Density
	sections	slices (mm)	(g)	(cm <sup>3</sup> )	(cm <sup>3</sup> )	error (%)	$(cm^2)$	(g/cm <sup>2</sup> )
	14	4 5.6	227.4	295	289.37	1.91	221.29	0.771
	10	) 8.9	242.7	320	315.88	1.29	233.38	0.758
Cronner	11	8.2	265.2	360	347.10	3.58	248.07	0.737
Smith	18	3 4.8	272.4	375	368.93	1.62	261.27	$\begin{array}{c} .7 \\ 0.726 \\ 0.737 \end{array}$
Apple	18	3 4.9	280.1	380	375.38	1.22	261.91	0.737
Apple	18	3 5.2	304.1	415	423.67	2.09	284.91	0.733
					$MARE_V$	1.95	Averag	e density
					r	0.9917		0.744
	13	3 5.6	211.5	260	249.63	3.99	200.98	0.813
	15	5 5.7	232.2	265	258.76	2.35	208.58	0.876
Dad	15	5 5.7	235.7	275	273.92	0.39	216.43	0.857
Delicious	1.	5 5.7	251.9	290	286.08	1.35	223.67	0.869
apple	1.	5 5.9	286.5	330	334.70	1.42	243.92	0.868
appro	15	5 5.7	288.2	330	332.04	0.62	248.71	0.873
				-	MARE <sub>V</sub>	1.69	Averag	e density
					r	0.9978		0.859
	10	) 12.8	494.5	470	458.36	2.48	401.56	1.052
	10	) 15	554.0	515	515.62	0.12	418.00	1.076
	10	) 16	579.1	550	553.89	0.71	428.07	1.053
	(*) 1	1 16	580.0	545	539.95	0.93	421.46	1.064
Meat	12	2 13.1	594.5	565	547.21	3.15	437.73	1.052
pieces	11	I 15	604.4	560	563.07	0.55	422.35	1.079
	13	3 12.6	758.3	705	706.74	0.25	498.35	1.076
	12	2 16	822.7	770	749.19	2.70	532.80	1.068
					$\overline{MARE_V}$	1.36	Averag	e density
					r	0.9954		1.065

419 (\*) Sample used to analyze the influence of cross-sections and boundary points numbers

<sup>420</sup> on the approximation error.

#### 421 Table 2. Regression analysis data (Eq. (5)-(6)) between estimated surface area and

#### 422 weight and volume measurements.

Sample	$a_0$	$R^2$	$\beta_0$	$R^2$
Granny Smith apple	6.1117	0.9336	5.0085	0.9725
Red Delicious apple	5.6312	0.9828	5.0961	0.9582
Meat piece	6.1068	0.9460	6.3729	0.9644

423

#### 425 Figure captions

426

427 **Figure 1.** Schematic representation of the employed computer vision system.

428

- 429 Figure 2. Schematic representation of the sectioning axis and slices for (a) apples and
- 430 (b) meat pieces.

431

Figure 3. Example of the stages involved in image processing and boundary approximation over a meat slice. (a) Original RGB image of the transversal cut. (b) Grey-scale representation of the RGB image. (c) Grey-scale image histogram. (d) Binary image obtained by thresholding. (e) B-Spline approximation to a subset of binary image boundary points. (f) Original image and its approximated boundary.

437

Figure 4. Visual results of the reconstruction technique and meshing procedure appliedto meat sample.

440

441 Figure 5. Visual results of the reconstruction technique and meshing procedure applied442 to Red Delicious apple.

443

Figure 6. Solids constructed by two apple slices, with different number of boundary
points: (a) 33 boundary points; (b) 376 boundary points. Enlarged regions show in detail
the smoothness of each solid.

447

**Figure 7.** Effect of boundary points number on reconstruction performance of a single representative meat sample. (a) Surface area ( $\Box$ , cm<sup>2</sup>) and volume variation ( $\diamondsuit$ , cm<sup>3</sup>)

with number of boundary points. (b) Volume estimation error (O) as a function of
boundary points number.

452

Figure 8. Effect of cross-sections number on reconstruction performance of a single representative meat sample. (a) Surface area  $(\Box, cm^2)$  and volume variation  $(\diamondsuit, cm^3)$ with number of cross-sections. (b) Volume estimation error  $(\bigcirc)$  as a function of crosssections number.

457

**Figure 9.** Correlation between experimental and estimated volume values for reconstructed solids: ( $\Box$ ) meat pieces; ( $\triangle$ ) Granny Smith apples; ( $\bigcirc$ ) Red Delicious apples.

461

462 Figure 10. Surface area variation with weight (a) and volume (b) of samples.  $(\Box)$  Meat

463 pieces; ( $\triangle$ ) Granny Smith apples; ( $\bigcirc$ ) Red Delicious apples. Solid lines represent Eq.

464 (5) and (6), in each case.

465 Fig 1:



467 Fig 2:



469 Fig 3:





471 Fig 4:





473 Fig 5:



474

475 Fig 6:



477 Fig 7:



479 Fig 8:



481 Fig 9:





482

483 Fig 10:

